

How Multiscale Modeling can impact Biomedical and Clinical Research

VPH/Physiome perspective

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Talk plan

Scales:

1. Population
2. Whole body
3. Cell-tissue-organ
4. Pathways & networks
5. Atomic & molecular

Charge: Look at ..

Perception/acceptance
Future biomed applications
Future clinical applications
Directions for modeling
Standards, open source
Peer review

Case studies:

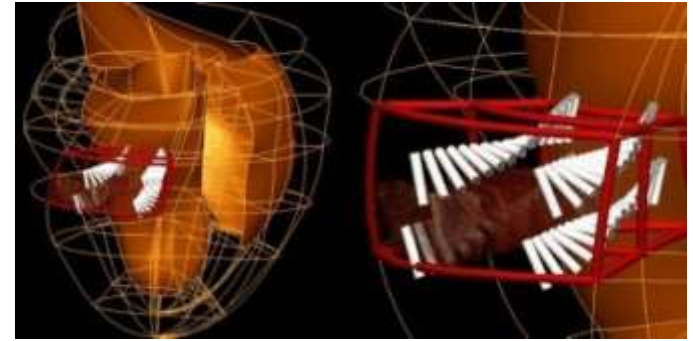
- *Cardiac models*
- *Cerebral aneurysm models*
- *Musculo-skeletal models*
- *Lens & whole eye models*

VPH/Physiome infrastructure

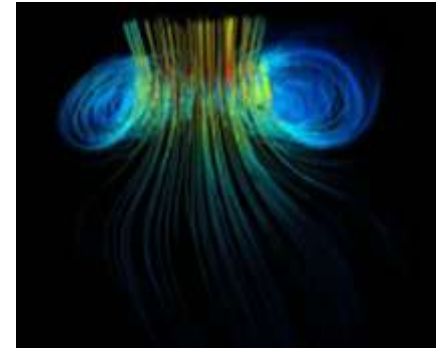
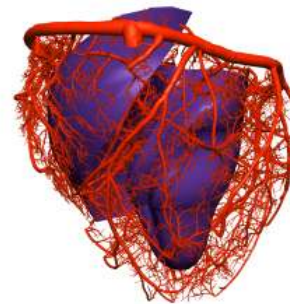
IMAG

Cardiac models

1. Myocardial mechanics

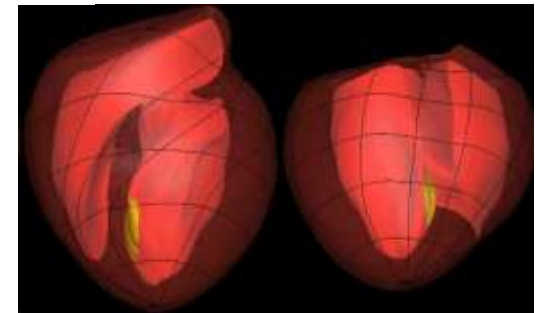
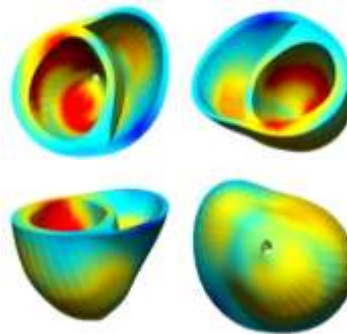


2. Fluid mechanics



3. Coronary flow

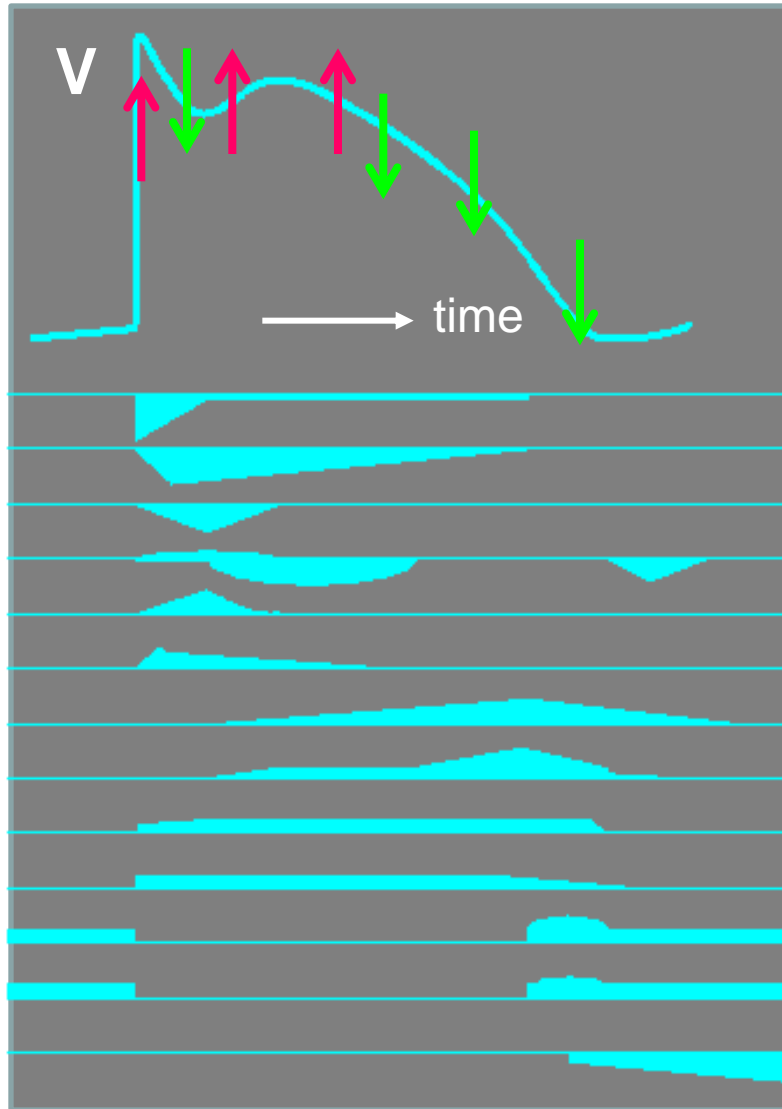
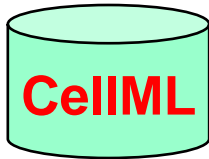
4. Myocardial activation



5. Coupling .. Mechano-electro-fluid model

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Membrane ion channels



$$\frac{dV_m}{dt} = \frac{\Sigma I_m}{C_m}$$

Probable clones

SCN5A + subunits
CACH1C

NCX
Kv4.x

KvLQT1 + minK

HERG + MiRP-1
Kv1.5

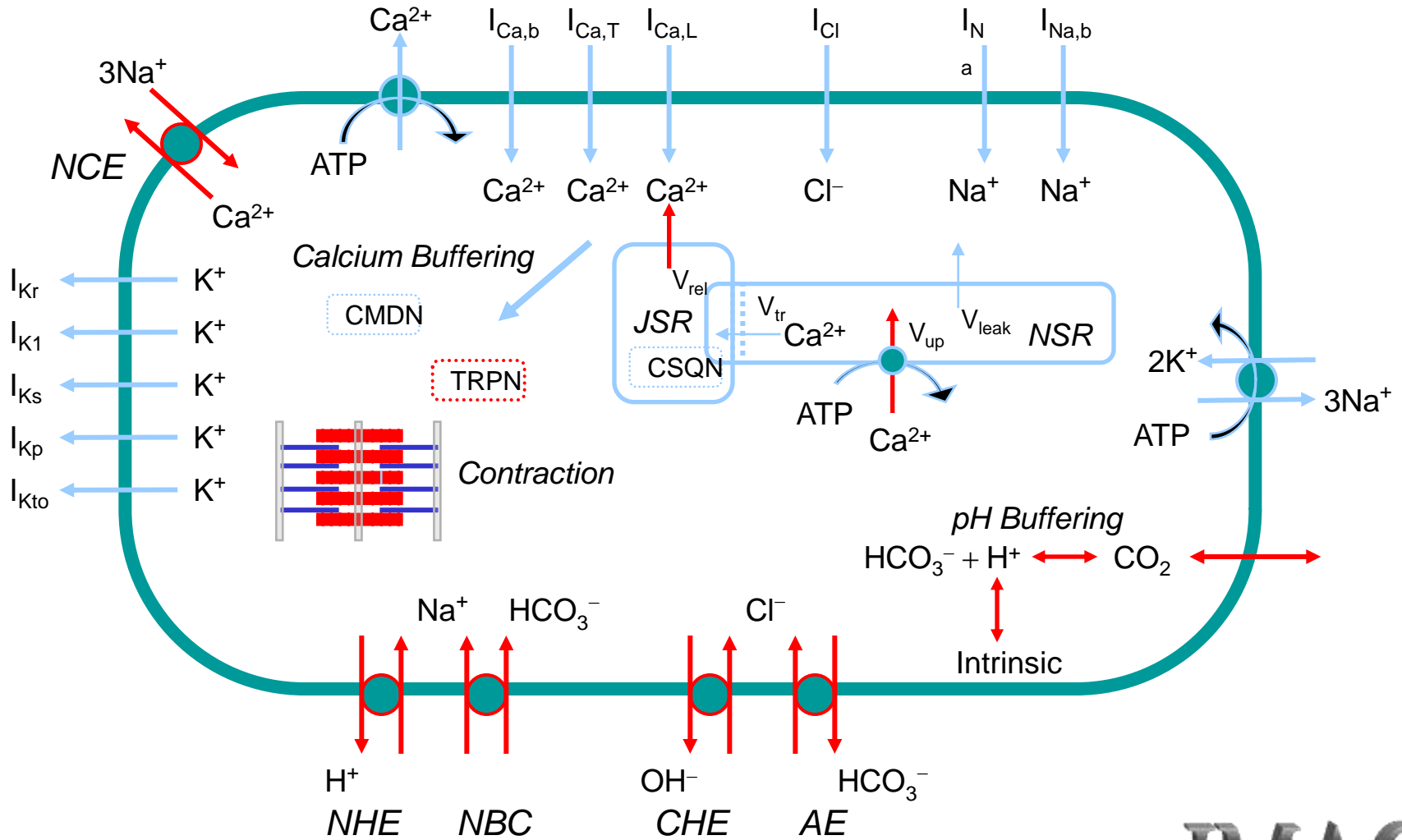
CFTR, TWIK
Kir2.x

Kir3.1/3.4, Kir6.x/SUR
hCNG

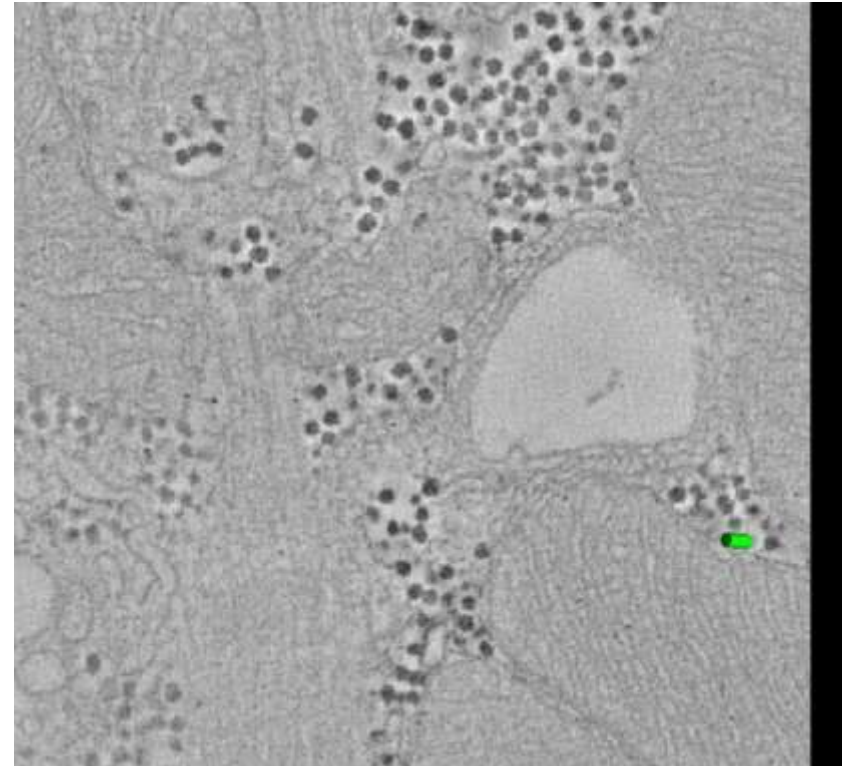
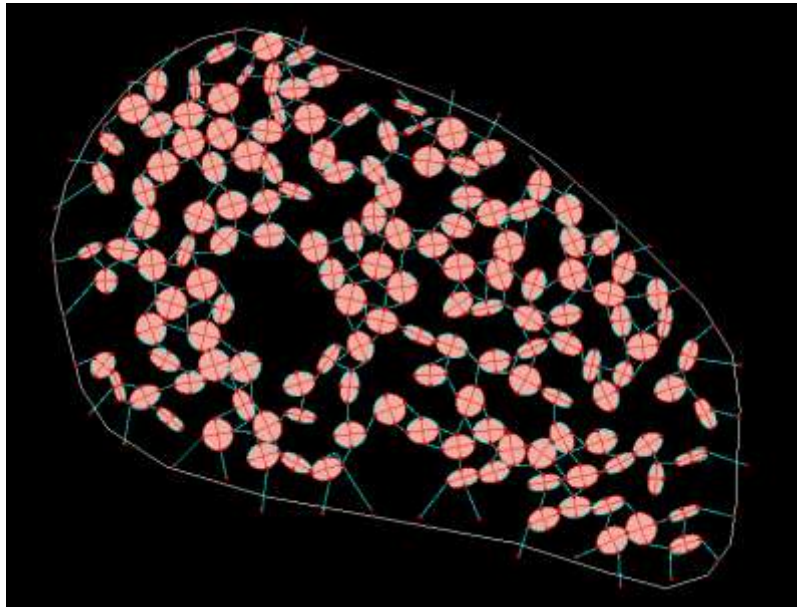
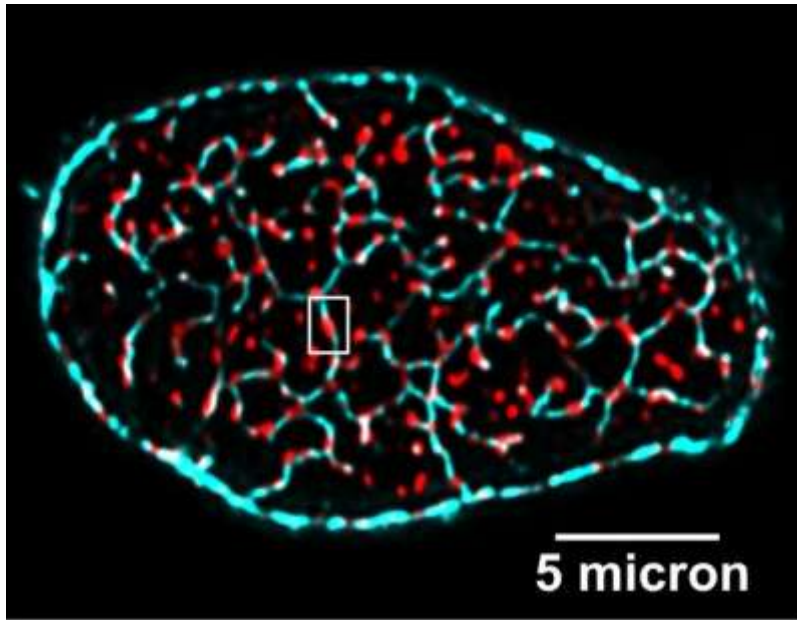
- Sodium current
- L-type calcium current
- T-type calcium current
- Na-Ca exchange
- I_{TO1} (4-AP-sensitive)
- I_{TO2} (Ca-activated)
- I_{Ks}
- I_{Kr}
- I_{Kur} or I_{Kq}
- I_{Cl} or I_{Kp}
- I_{K1} (inward rectifier)
- I_K ATP/ACh
- I_f (pacemaker)

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Cell processes



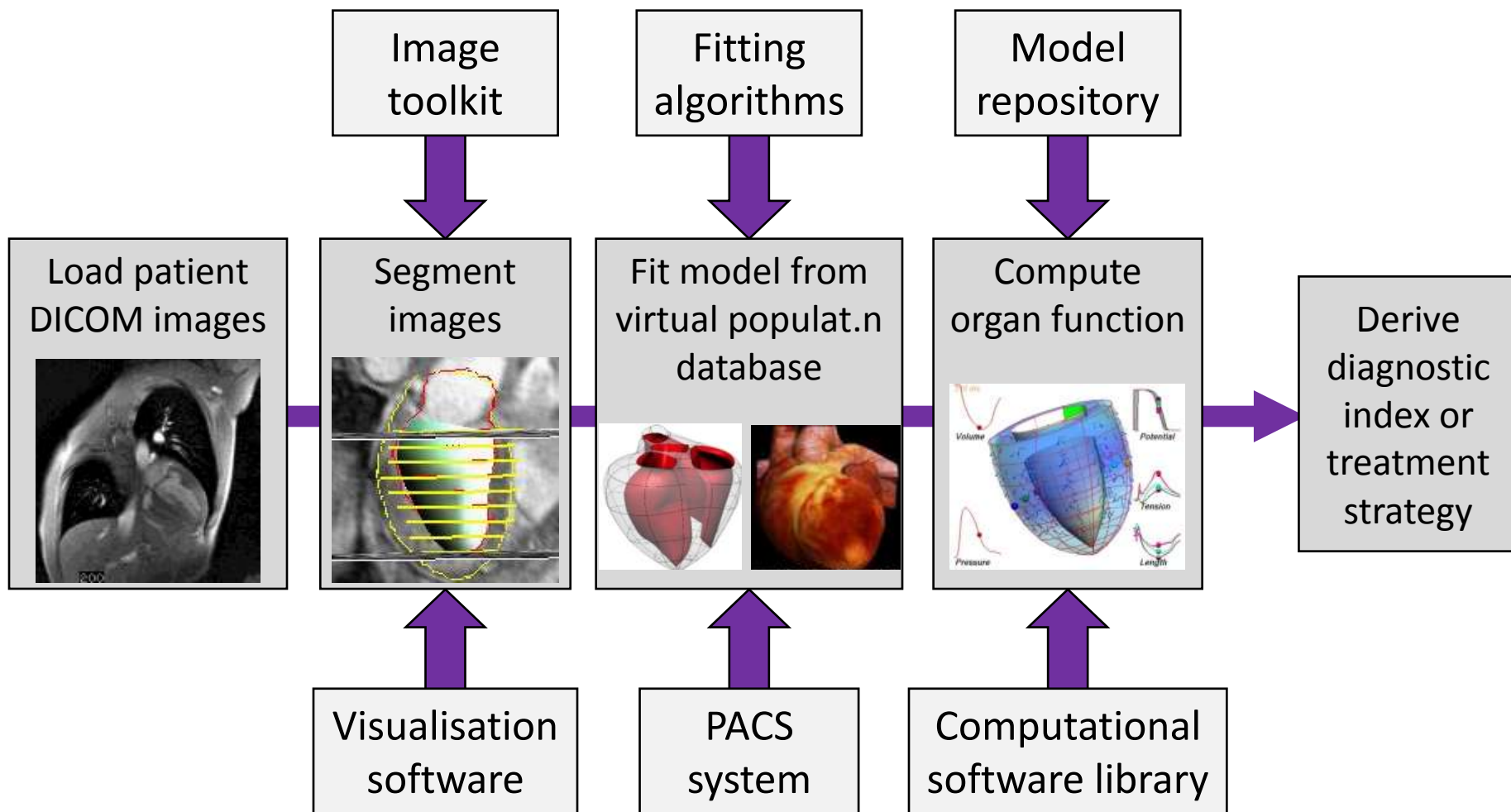
3D cardiac cell models



Vijay Rajagopal, Mark Ellisman, Peter Kohl

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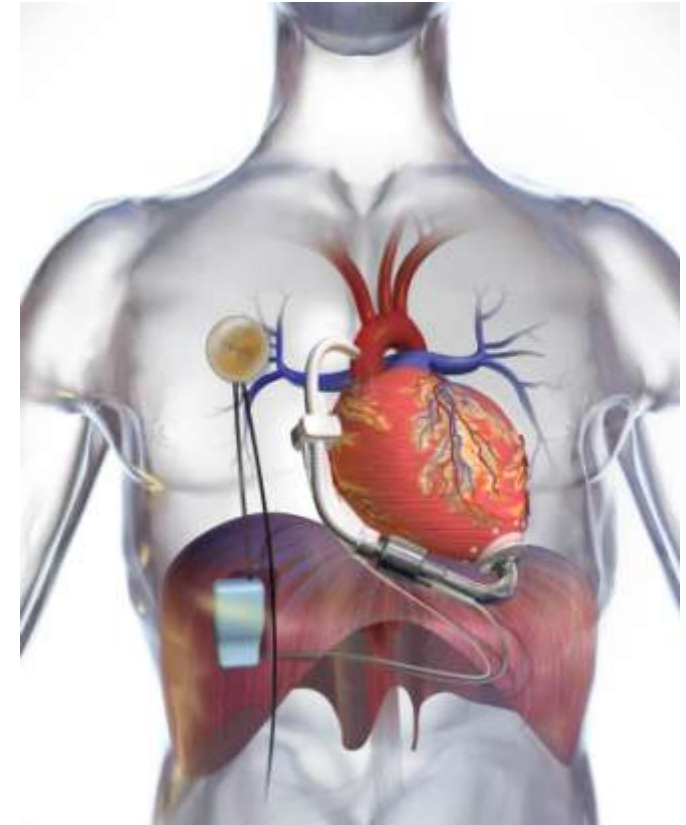
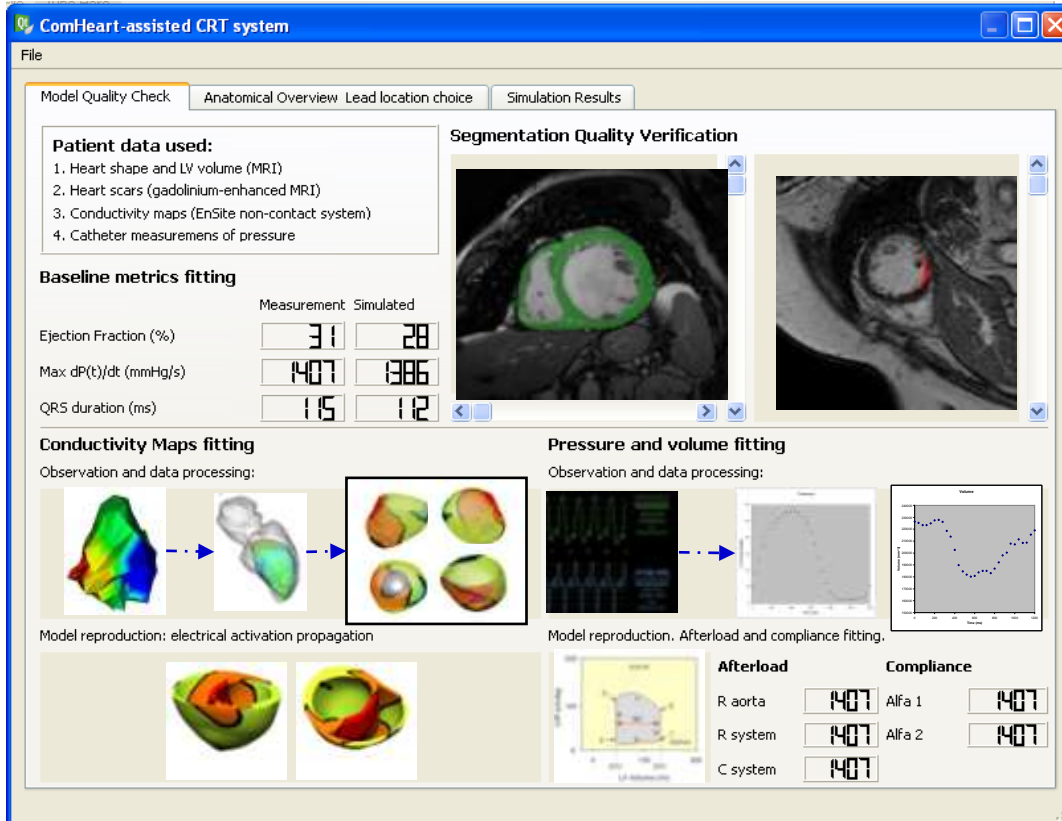
Clinical workflows



Clinical applications

euHeart: Philips Technologie GmbH

Berlin Heart



Personalised models, Multi-scale, Population databases

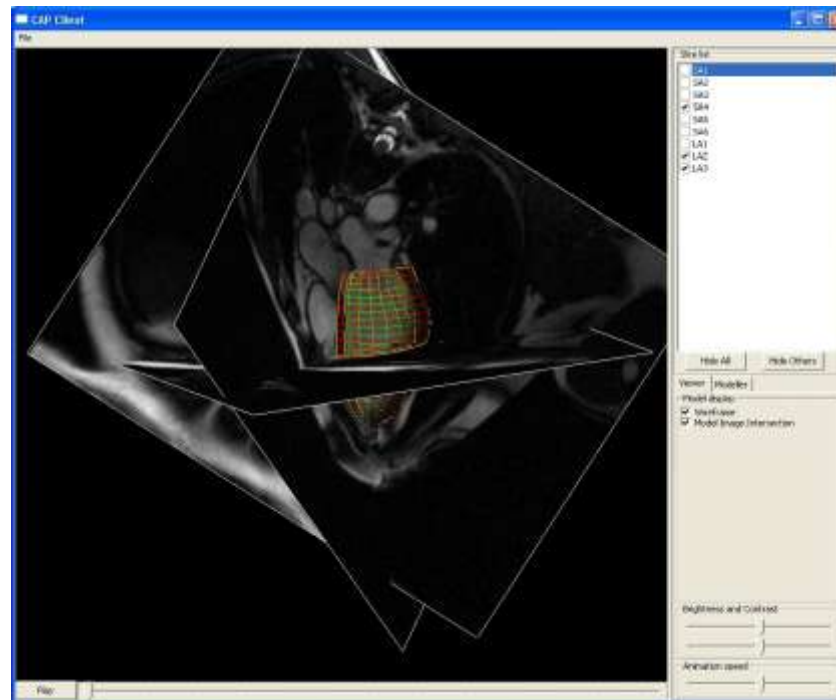
Aim for clinical trials within next few years

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Cardiac Atlas Project (NIH funded)




- www.cardiacatlas.org
- Structural and functional atlas of the heart
- Cardiac MRI examinations
- Fit model to each case and then derive subject specific functional analyses and associated clinical variables



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CAP database



Folder
Trash
Audit Repository
Logout

w/o studies
 latest studies first

Displaying studies 1 to 19 of 19 matching studies.

Result Filter: Studies

Patient Name:	Patient ID:	Study ID:	Study/ Birth Date	Modality:
Sex: M v F	Image Type: -all-	Scan Sequence: -all-	Sequence Variant: -all-	Scan Options: -all-
Repetition Time:	Echo Time:	Trigger Time:	Magn. Field Strength:	Temporal Resolution:
Nominal Interval:	Heart Rate:	Cardiac # Images:	Trigger Window:	Reconstr. Diameter:
Sequence Name:	Phase Encoding Direction: -all-	Phase Encoding Steps:	Vendor: -all-	Model:

Patient	Name:	Patient ID:	Birth Date:	Sex:	Acc. No.:	Ref. Physician:	Status:	NoS:	NoI:
Study	Date/Time:	Study ID (@Media):	Modality:	Study Description/ Study Instance UID :		Vendor/Model:	PPS Status:		NoI:
Series	Date/Time:	Series No (@Media):	Modality:	Series Description/Body Part/ Series Instance UID :					
-		CAP000001	1936/11/30	F					
2002/11/30 13:46:28	1		MR					26	424
2002/11/30 13:53:42	1		MR	scout_multi/		SIEMENS/Sonata		9	
2002/11/30 13:54:26	2		MR	scout_axials/		SIEMENS/Sonata		20	

INSTANCE DICOM attributes in DB.

0018	0020	Scanning Sequence	CS	2	1	SE
0018	0021	Seq Variant	CS	4	1	NONE
0018	0022	Scan Options	CS	2	1	CT
0018	0023	MR Acquisition Type	CS	2	1	2D
0018	0024	Sequence Name	SH	10	1	*tfiseg2d1
0018	0025	Angio Flag	CS	2	1	N
0018	0080	Repetition Time	DS	4	1	400
0018	0081	Echo Time	DS	4	1	1.15
0018	0083	Number of Averages	DS	2	1	1
0018	0084	Imaging Frequency	DS	10	1	63.649481
0018	0085	Imaged Nucleus	SH	2	1	1H
0018	0086	Echo Number(s)	IS	2	1	0
0018	0087	Magnetic Field Strength	DS	6	1	1.494
0018	0088	Spacing Between Slices	DS	2	1	32
0018	0089	Number of Phase Encoding Steps	IS	4	1	128
0018	0091	Echo Train Length	IS	2	1	1
0018	0093	Percent Sampling	DS	2	1	50
0018	0094	Percent Phase Field of View	DS	4	1	100
0018	0095	Pixel Bandwidth	DS	4	1	1150
0018	1060	Trigger Time	DS	6	1	517.5
0018	1062	Nominal Interval	IS	4	1	776
0018	1090	Cardiac Number of Images	IS	2	1	1
0018	1251	Transmit Coil Name	SH	4	1	Body

Opening DICOM.zip

You have chosen to open

DICOM.zip
 which is a: PC ZIP Archive
 from: <http://130.216.208.78:8080>

What should Firefox do with this file?

Open with Stuffit Expander (default)

Save File

Do this automatically for files like this from now on.

2.16.124.113543.6006.99.07811231122169914580

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Cerebral aneurysm models

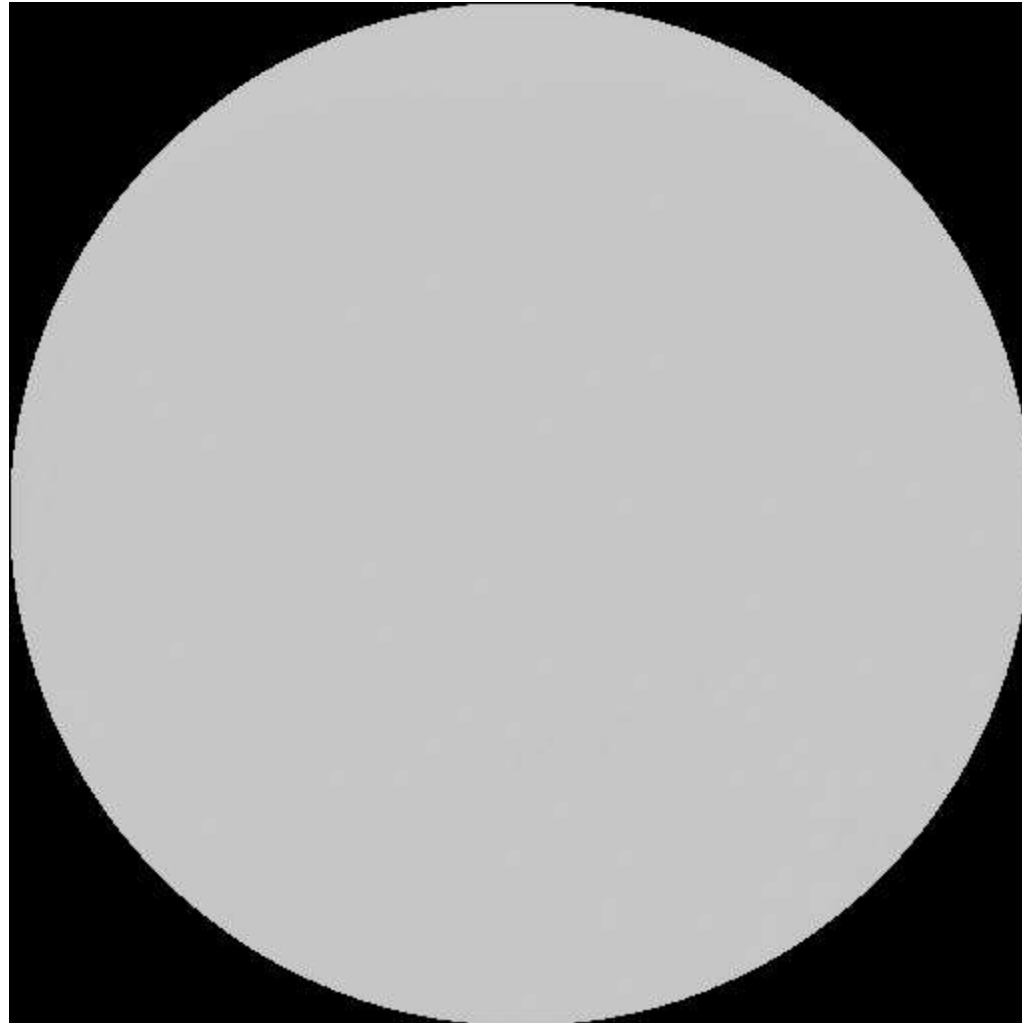
An intracranial aneurysm with CTA scanning
(55 yr old male patient)



How should this aneurysm be treated?

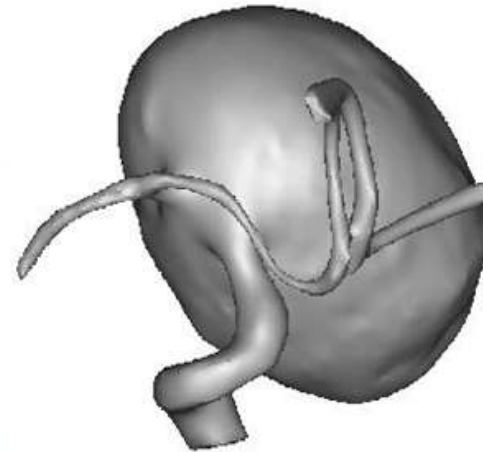
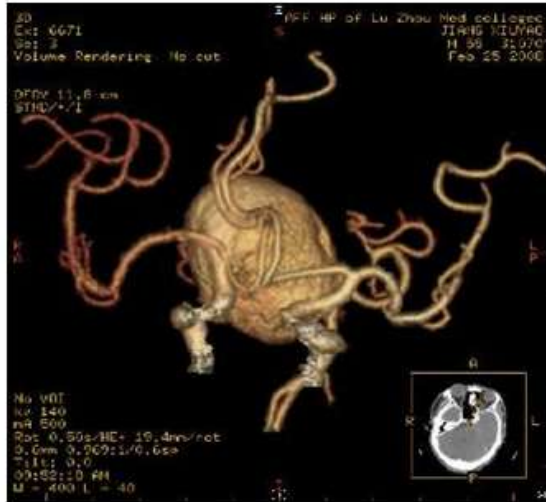
- Clipping?
- Endovascular treatment?
- Others (e.g. ligature)?

Blood perfusion with Digital Subtraction Angiography (DSA)

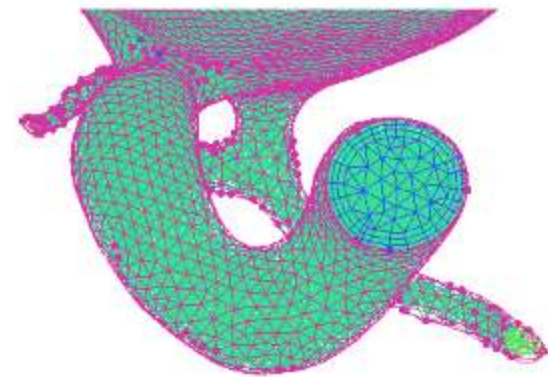
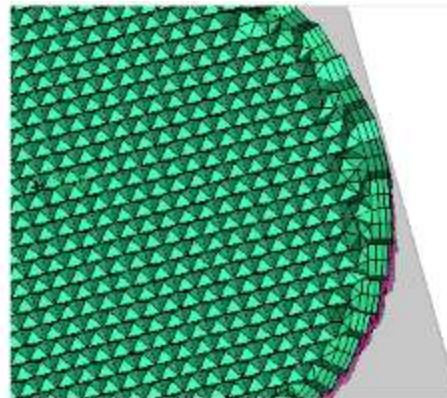
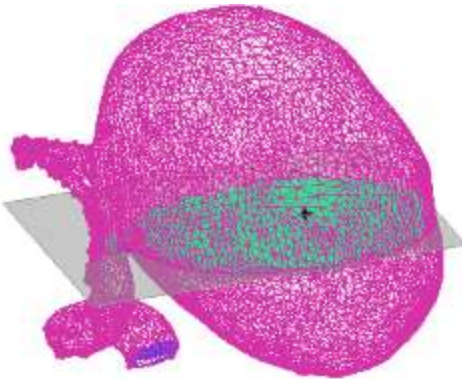


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Aneurysm model construction

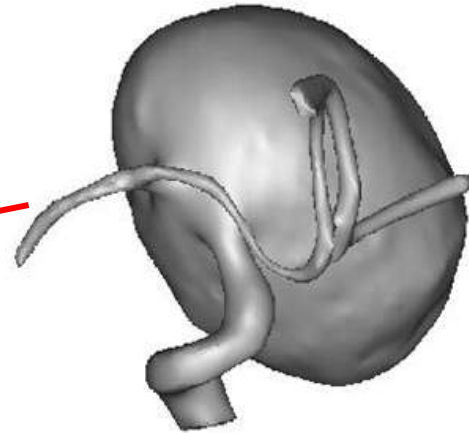
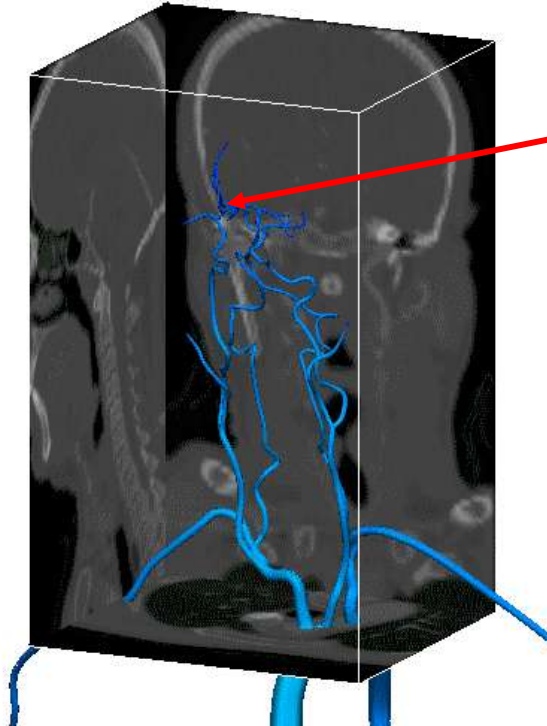
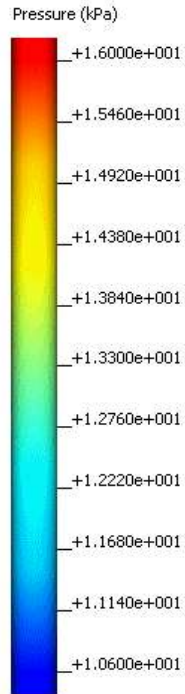


Volume image → **surface model**

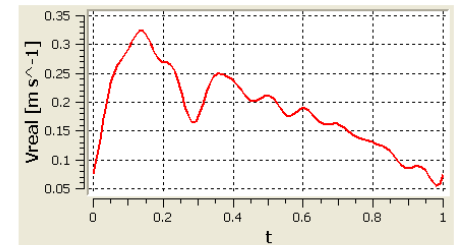
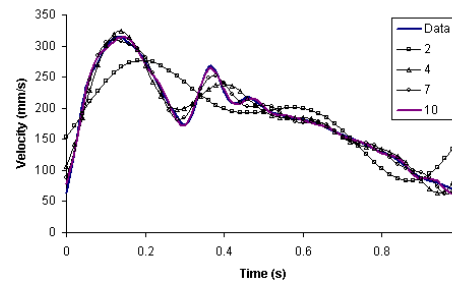


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Define boundary conditions

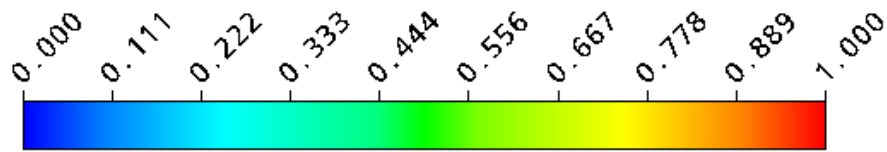
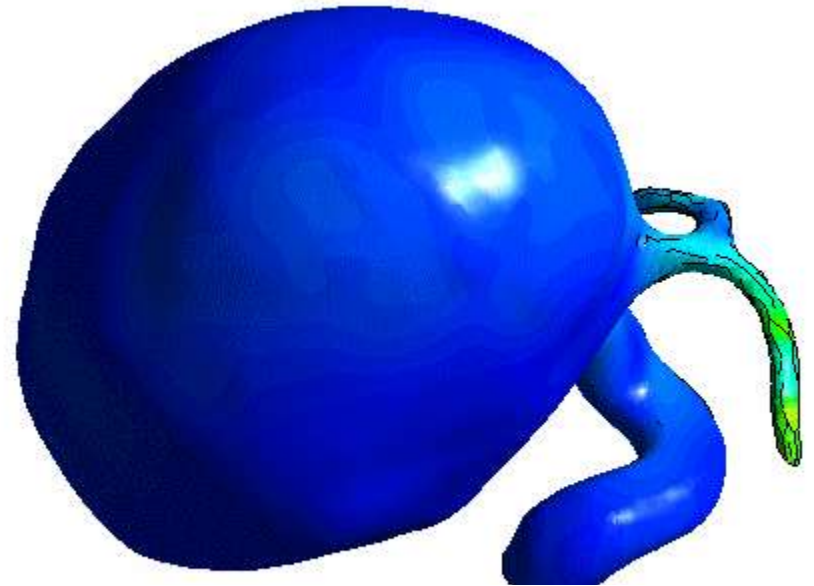
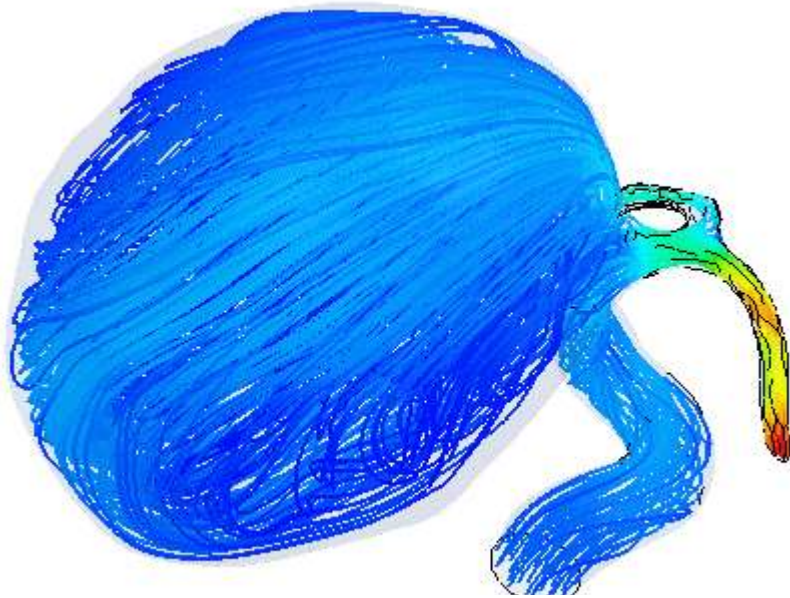


Inflow: pulsatile velocity

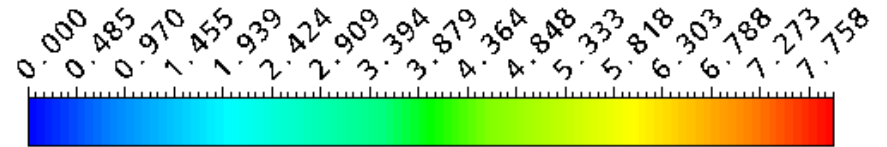


Particle streamlines

Wall shear stress



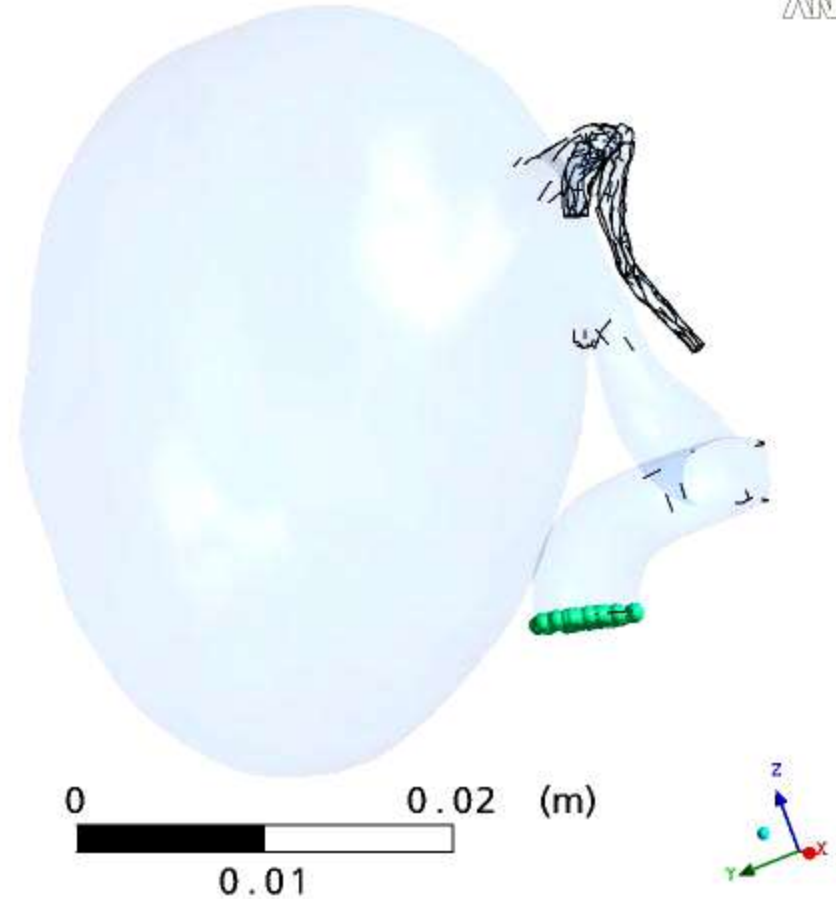
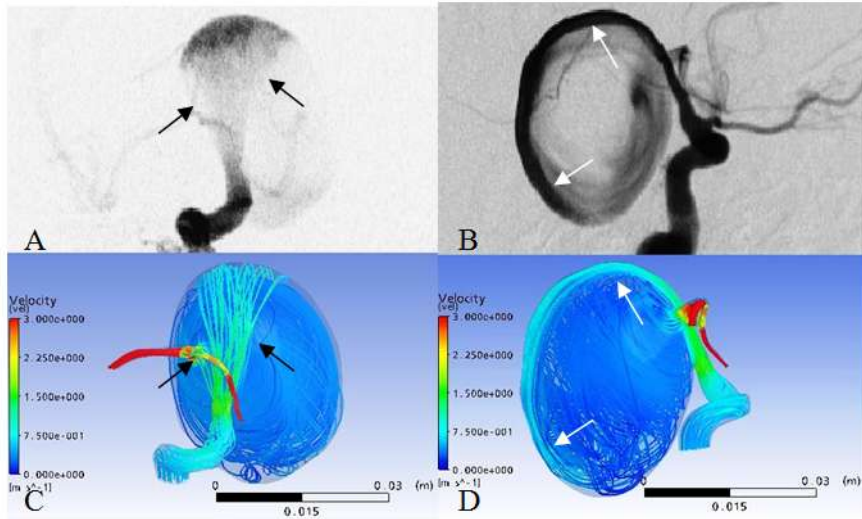
Velocity (Velocity Streamline)
[m s⁻¹]



Wall Shear (WSS)
[Pa]

Validation: flow patterns

ANSYS



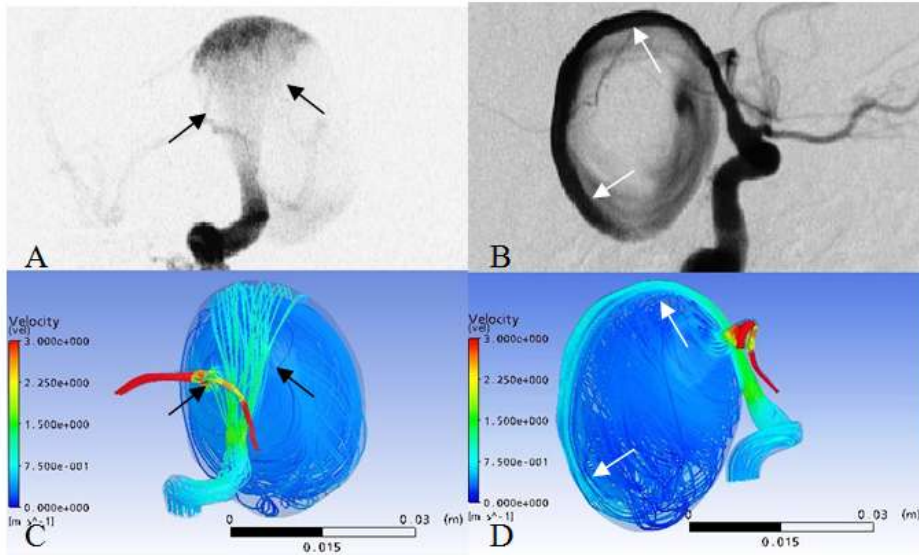
Particle tracking:

Particle size: $20\mu\text{m}$

Density: 2300kg/m^3

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Wall mechanics



Shear Stress



Compensatory Vascular Tone

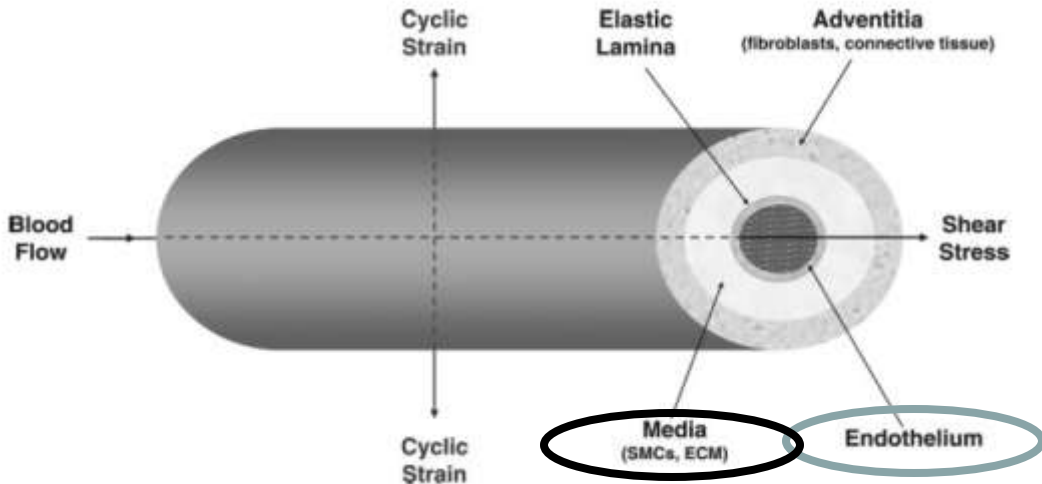


Growth and Remodelling

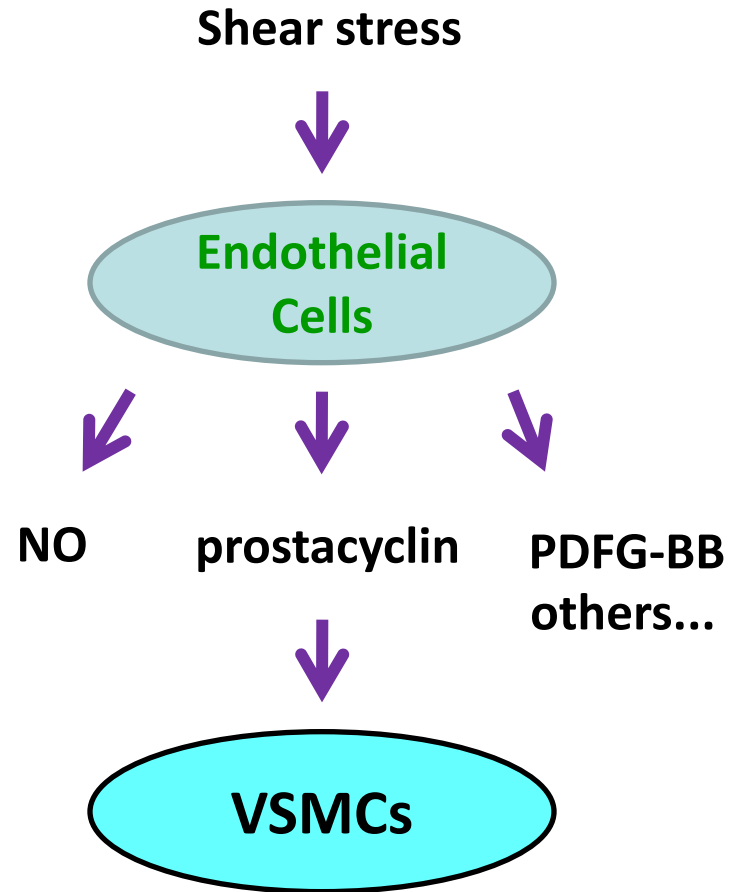


Aneurysm

Tissue to cellular



Cummins et al. (2007) *Am J Physiol Heart Circ Physiol*:292, Fig 1.

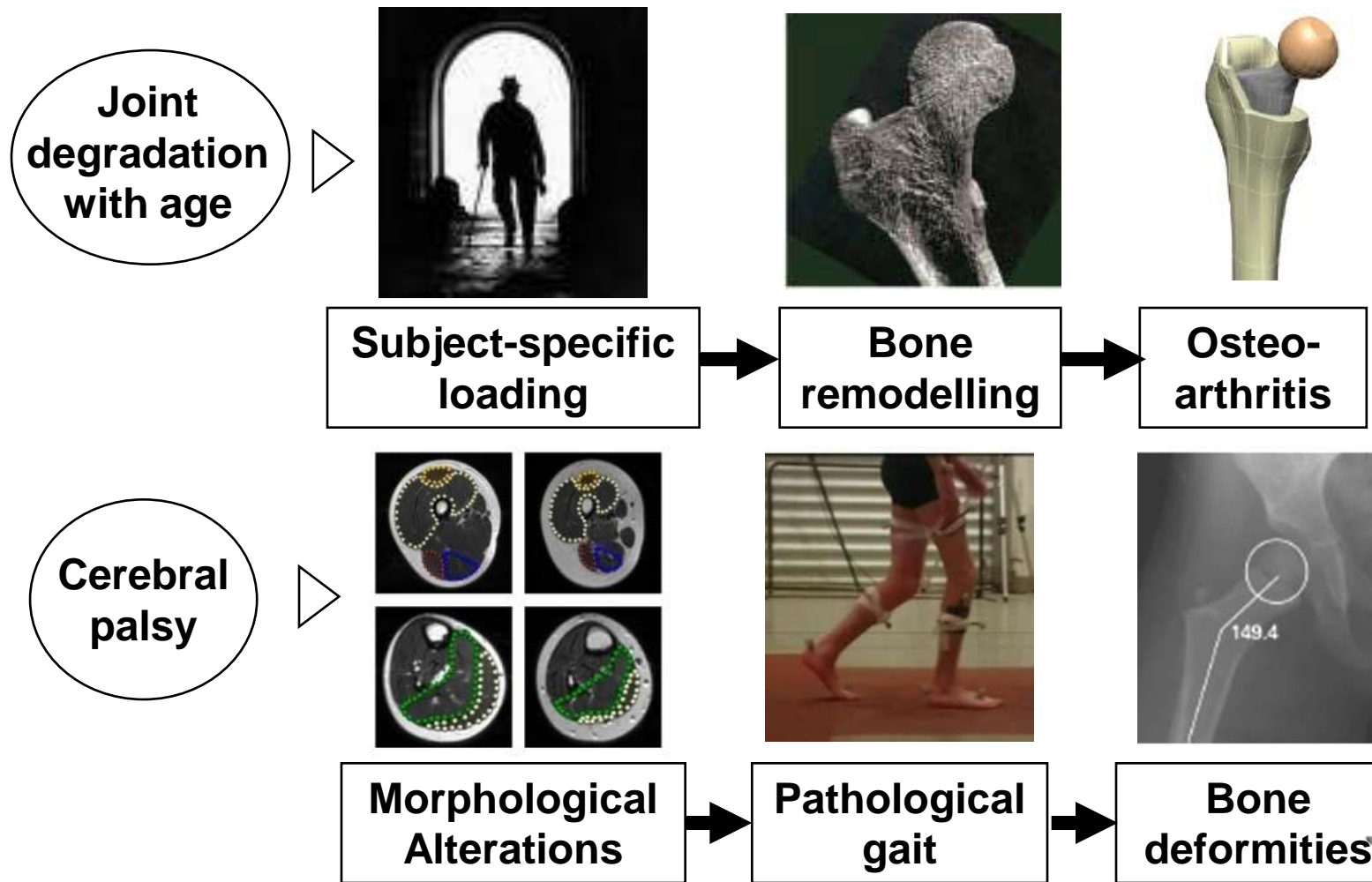


Approach

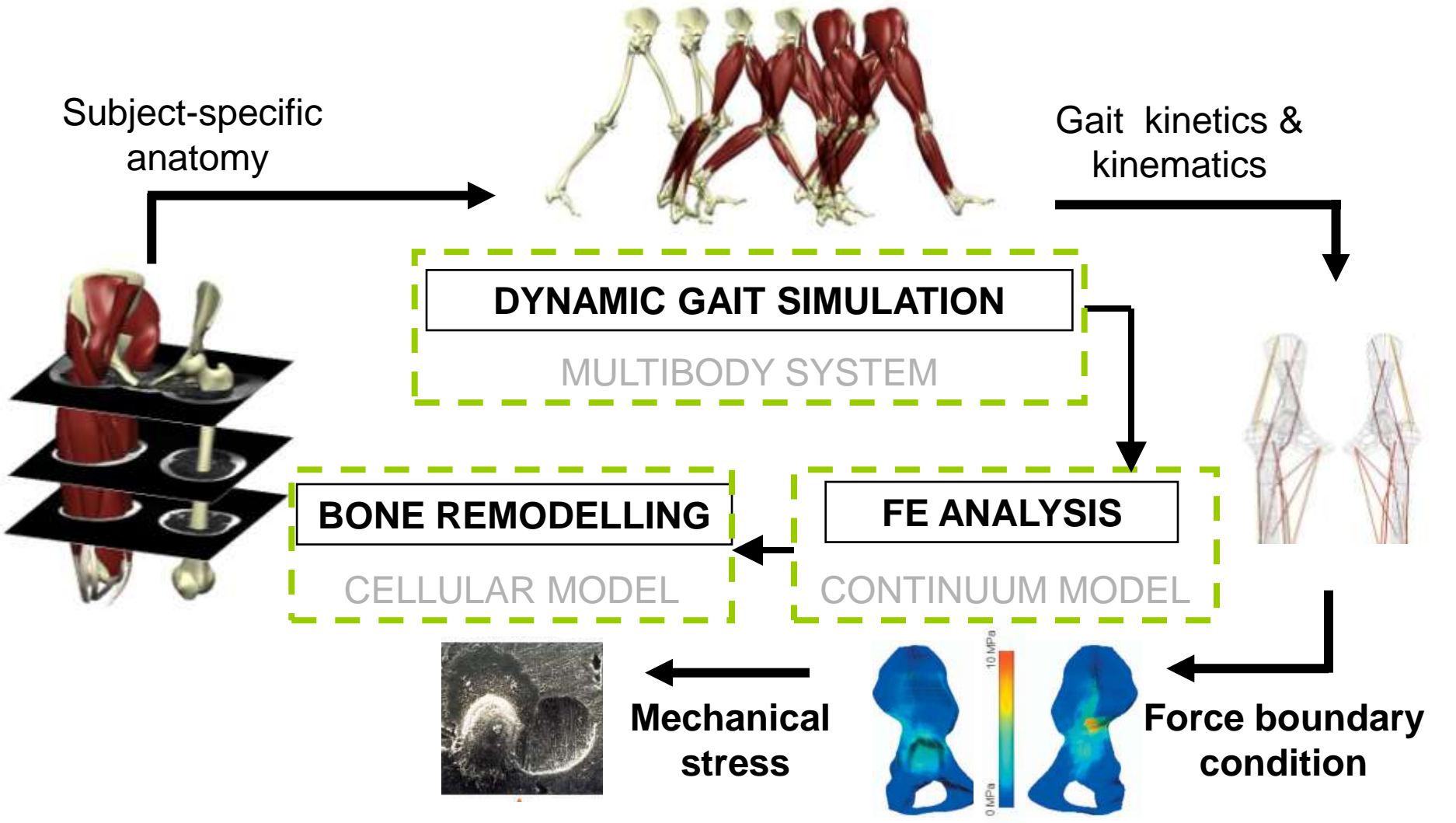
- **Multiple pathways with significant crosstalk**
- **Multiple cell types**
- **Multiple networks on multiple time scales**
- **Emergent properties important**
 - **Biophysically-based systems biology approach necessary**
- **Library of biochemical module models**
- **Reparameterised and reused**

Musculo-skeletal models

Subject-specific modelling of gait dynamics in orthopaedic research



Workflow



Gait Analysis

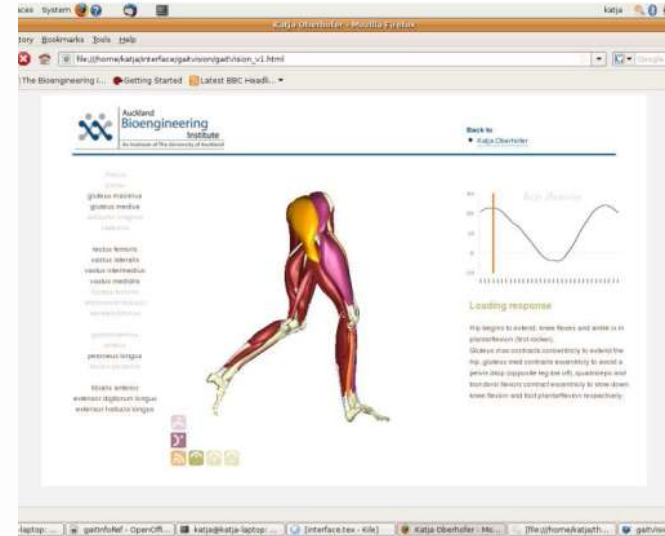
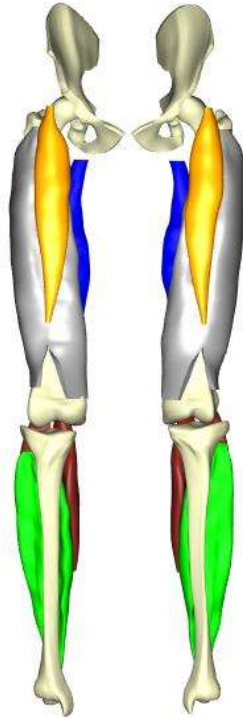
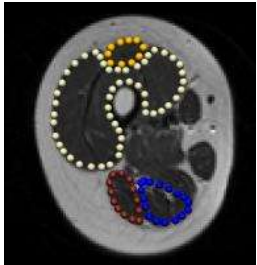


from measurement

to simulation

ABI Gait research

© MMVIII Auckland Bioengineering Institute



**Muscle architecture
in CP¹**

**Muscle deformation
during walking²**

**Medical education
www.gaitworld.com**

¹Oberhofer et al., *Clinical Biomechanics*, **2009**, online first

²Oberhofer et al., *The Visual Computer*, **2009**, 25(9), 843-851

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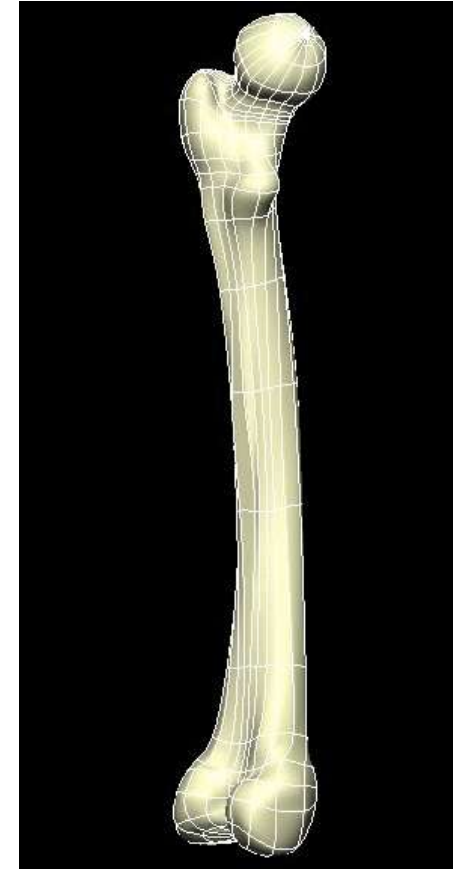
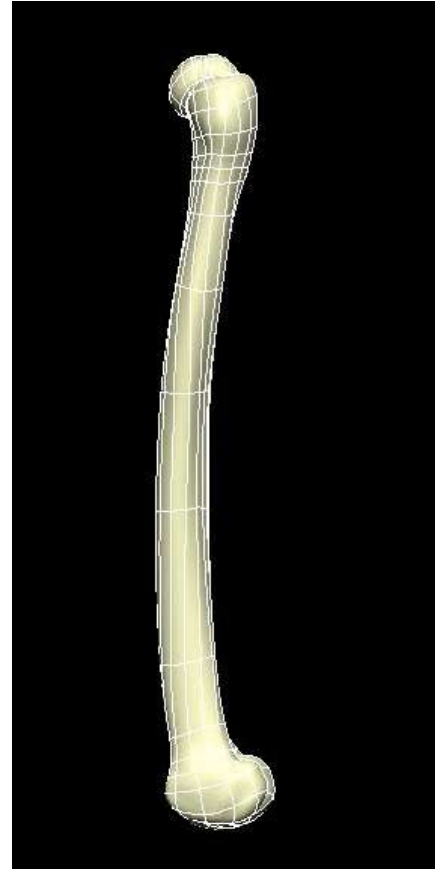
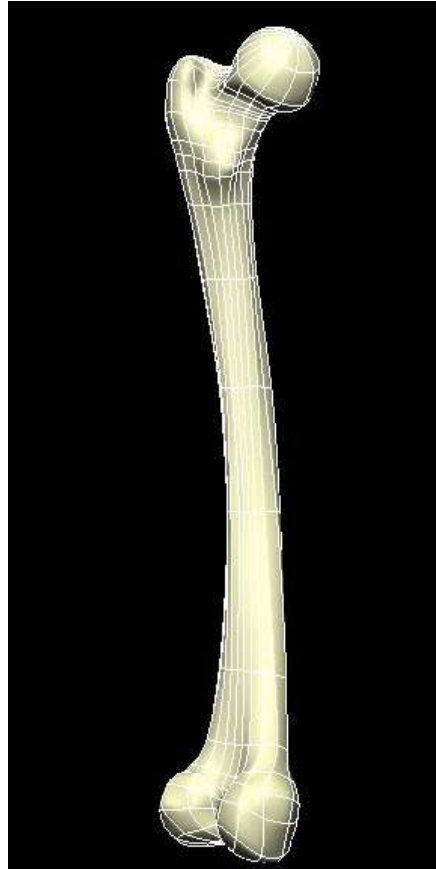
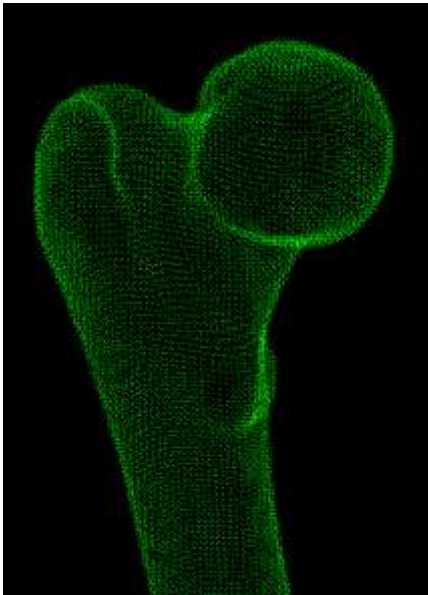
Principal component analysis

PC1 - 97%

PC2 - 0.94%

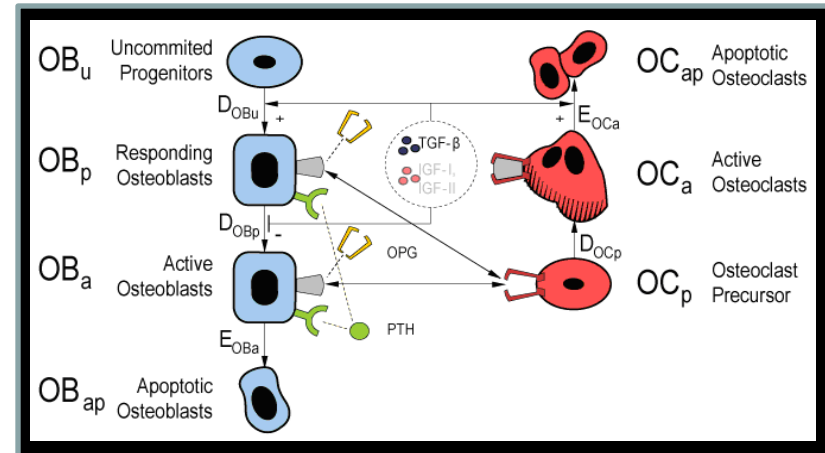
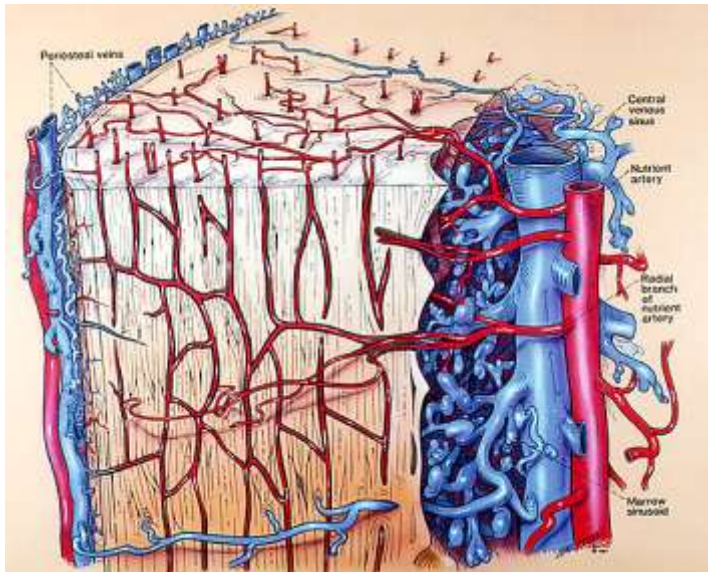
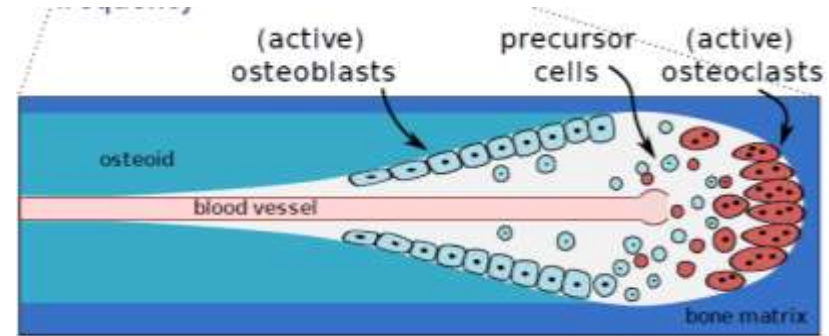
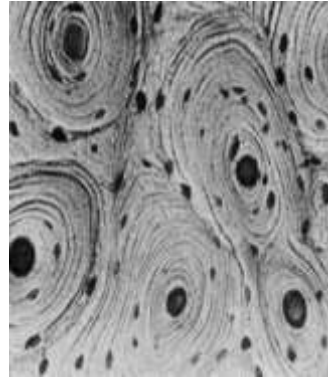
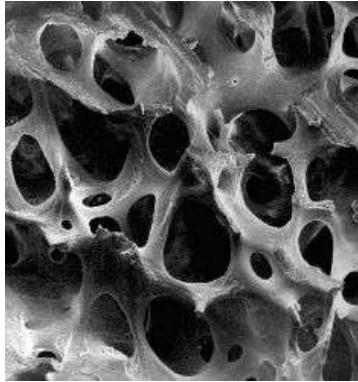
PC3 - 0.82%

17 left femurs



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Multiscale modeling of bone



Lens & eye models

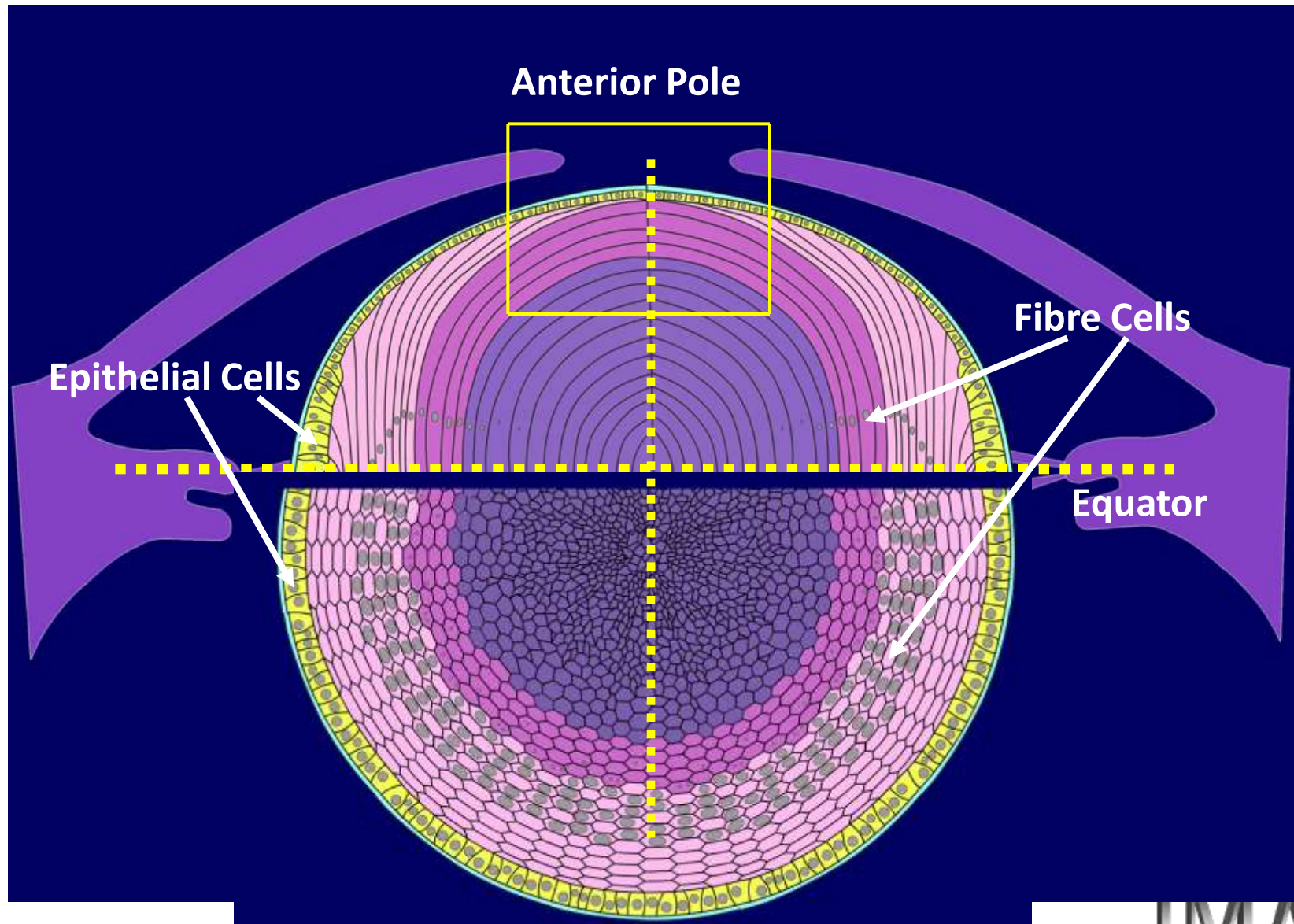
Medical therapies for cataracts



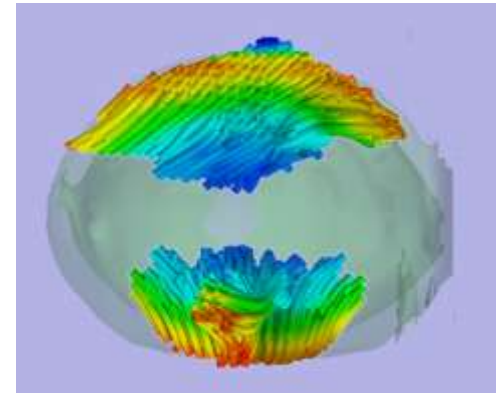
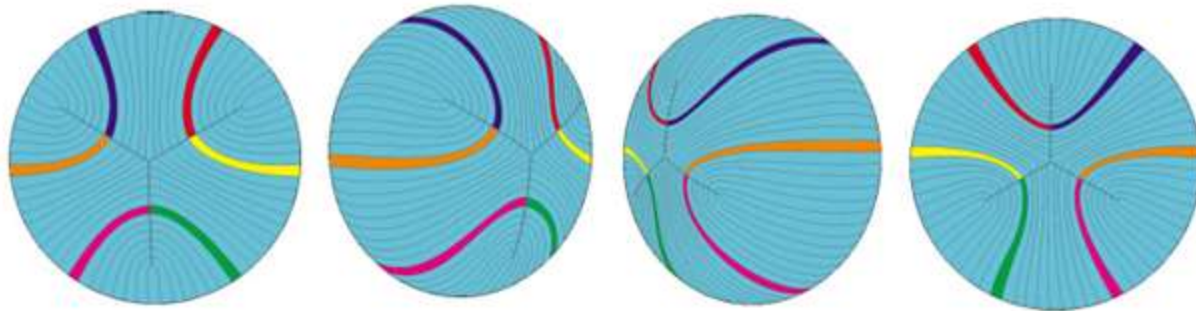
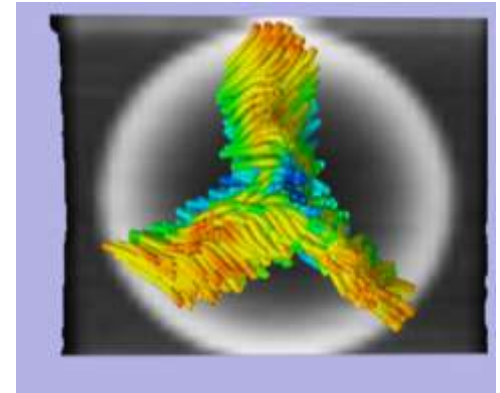
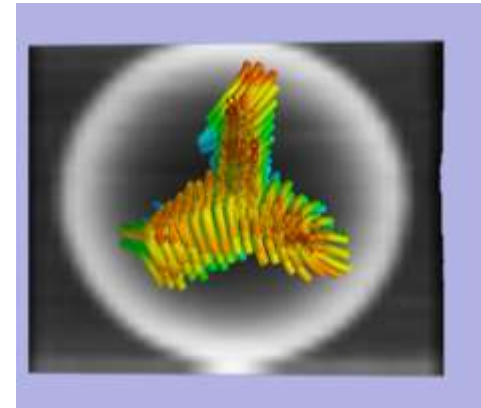
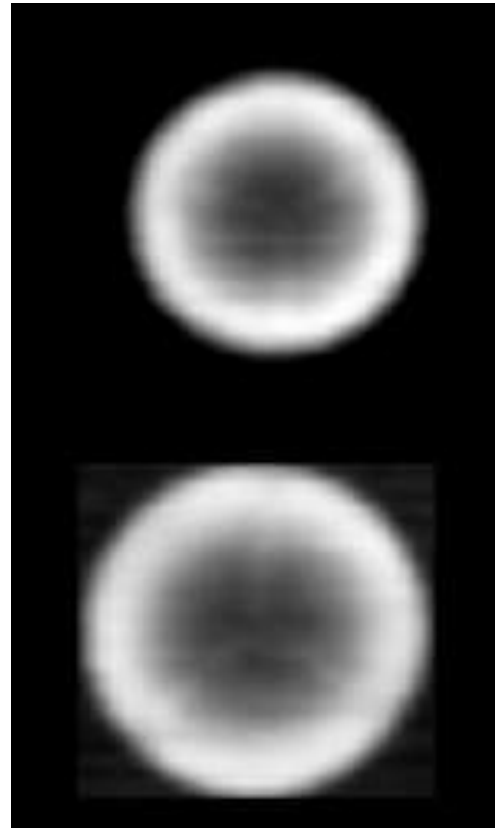
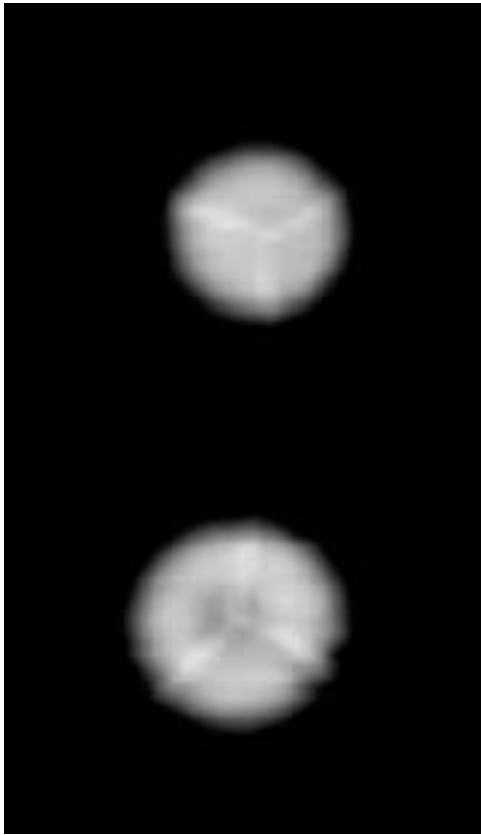
Paul Donaldson, Marc Jacobs and Ehsan Vaghefi

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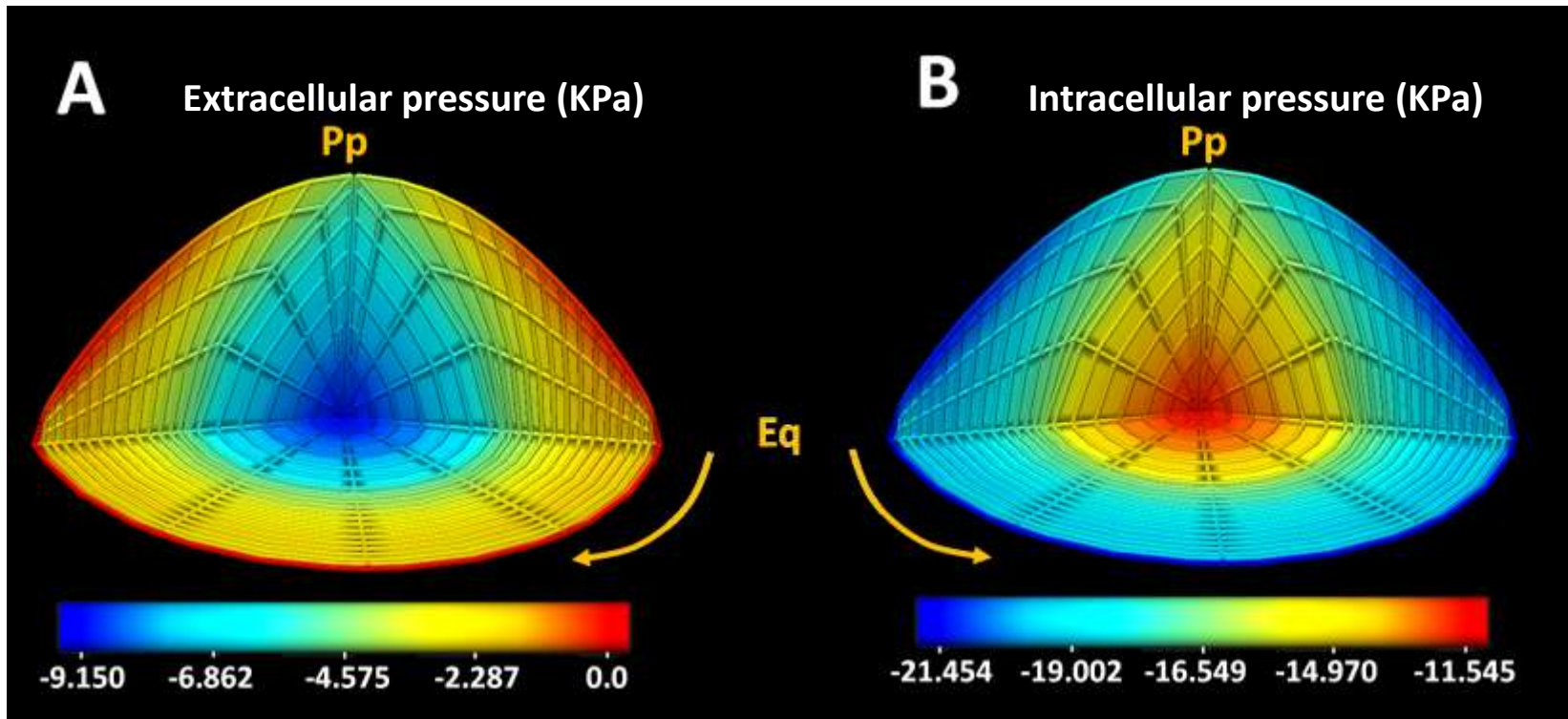
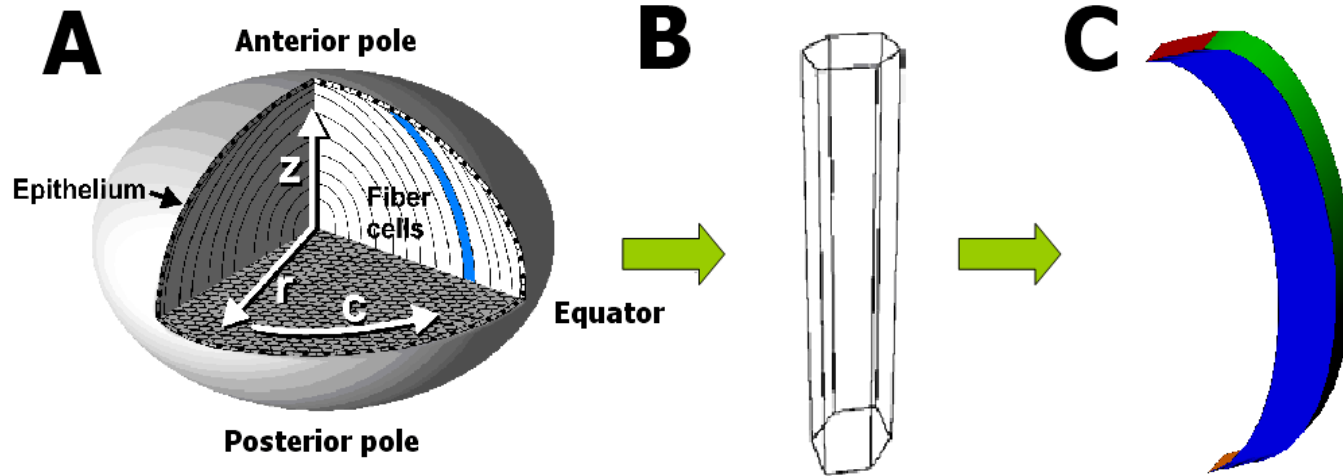
Lens structure



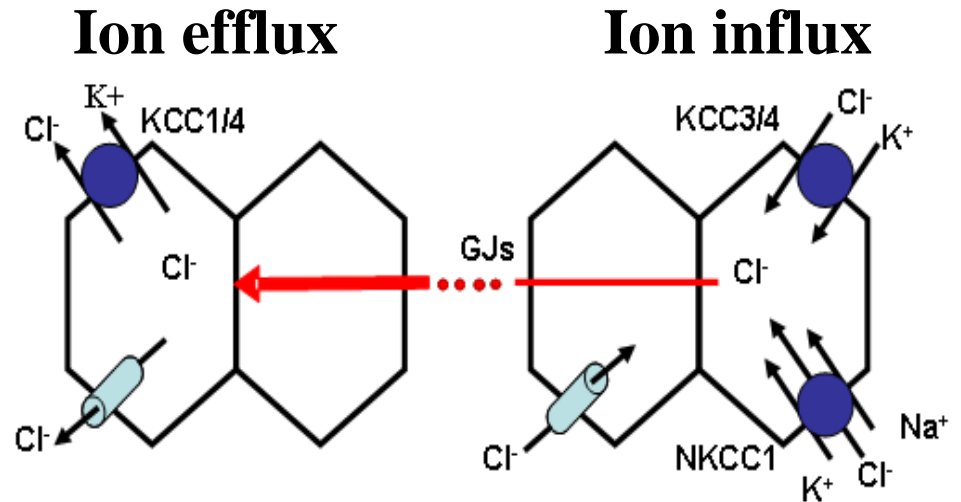
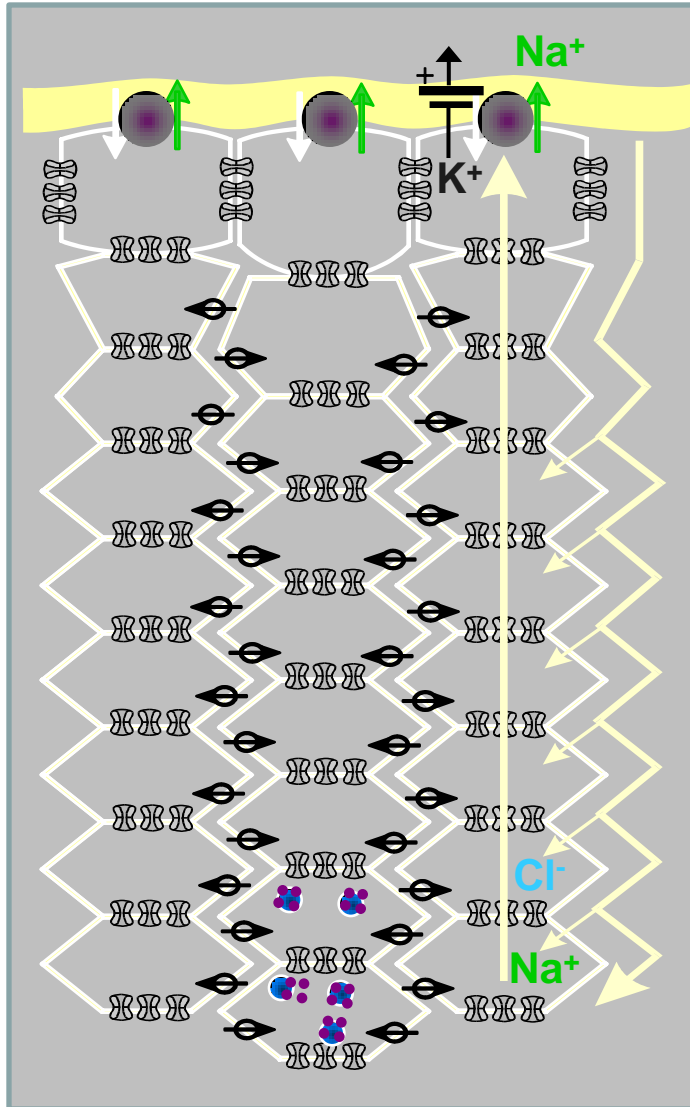
3D structure of lens sutures using diffusion tensor imaging



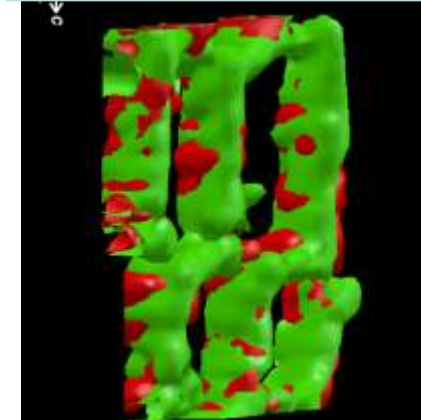
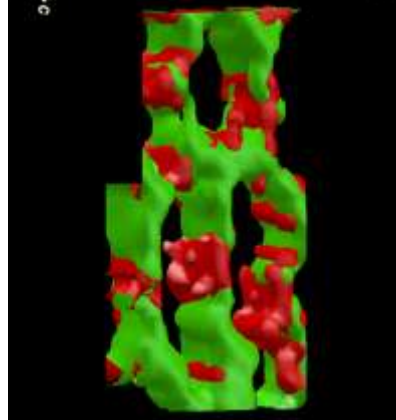
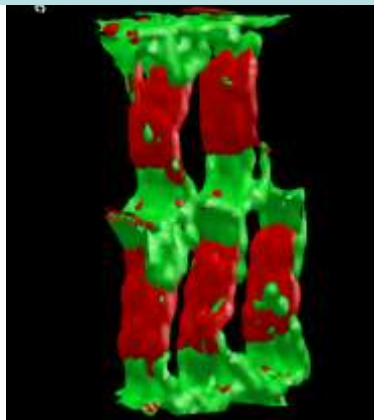
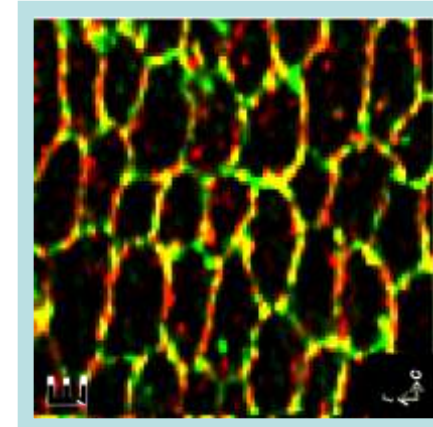
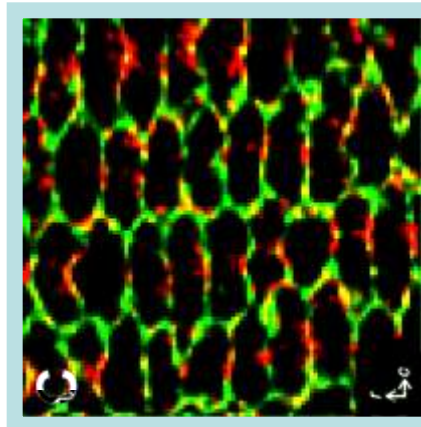
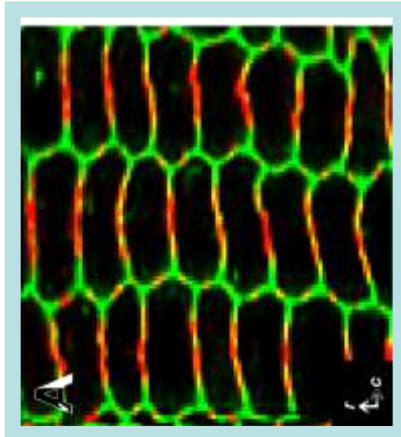
Modeling mechanics of lens shape changes



Lens function: the internal circulation system



Differentiation dependent changes in the subcellular distribution of gap junctions

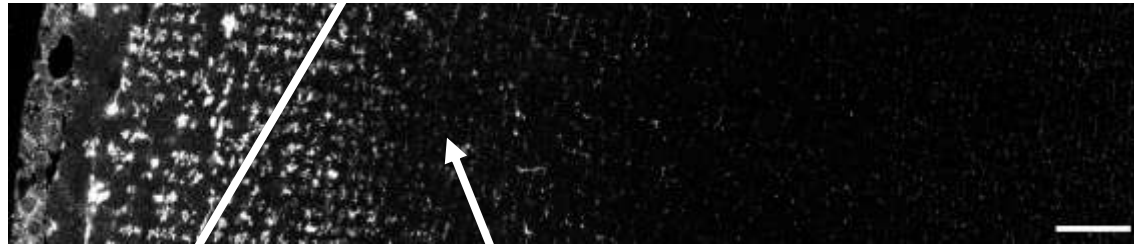


Osmotic stress changes the subcellular distribution of P2X₄

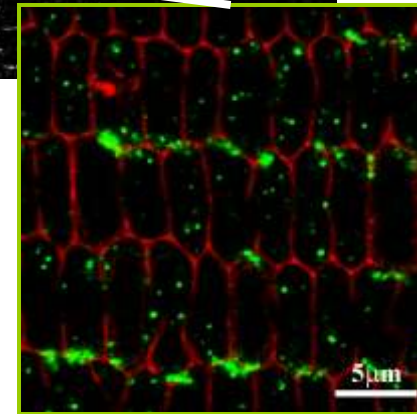
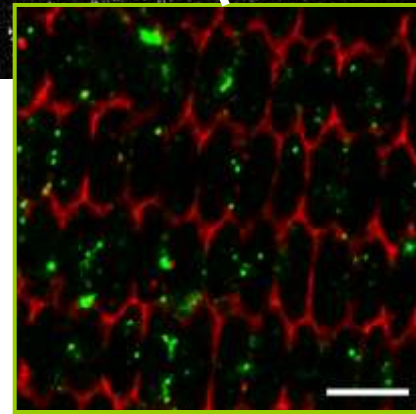
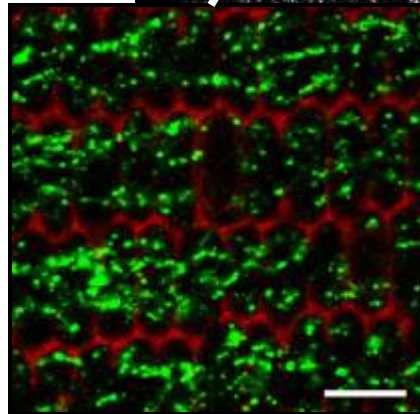
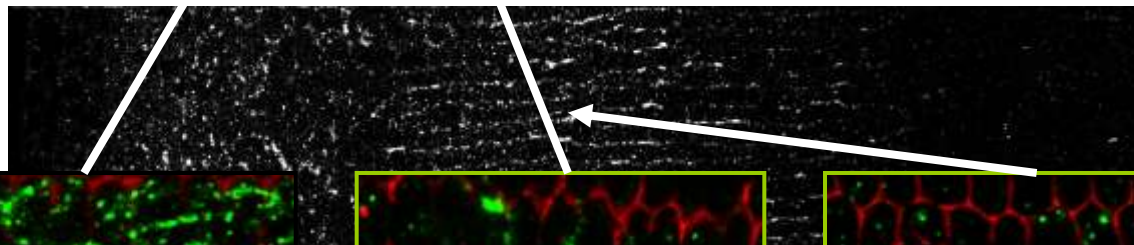
Isotonic condition
(Normal)



Hypertonic condition
(Cell shrinkage)

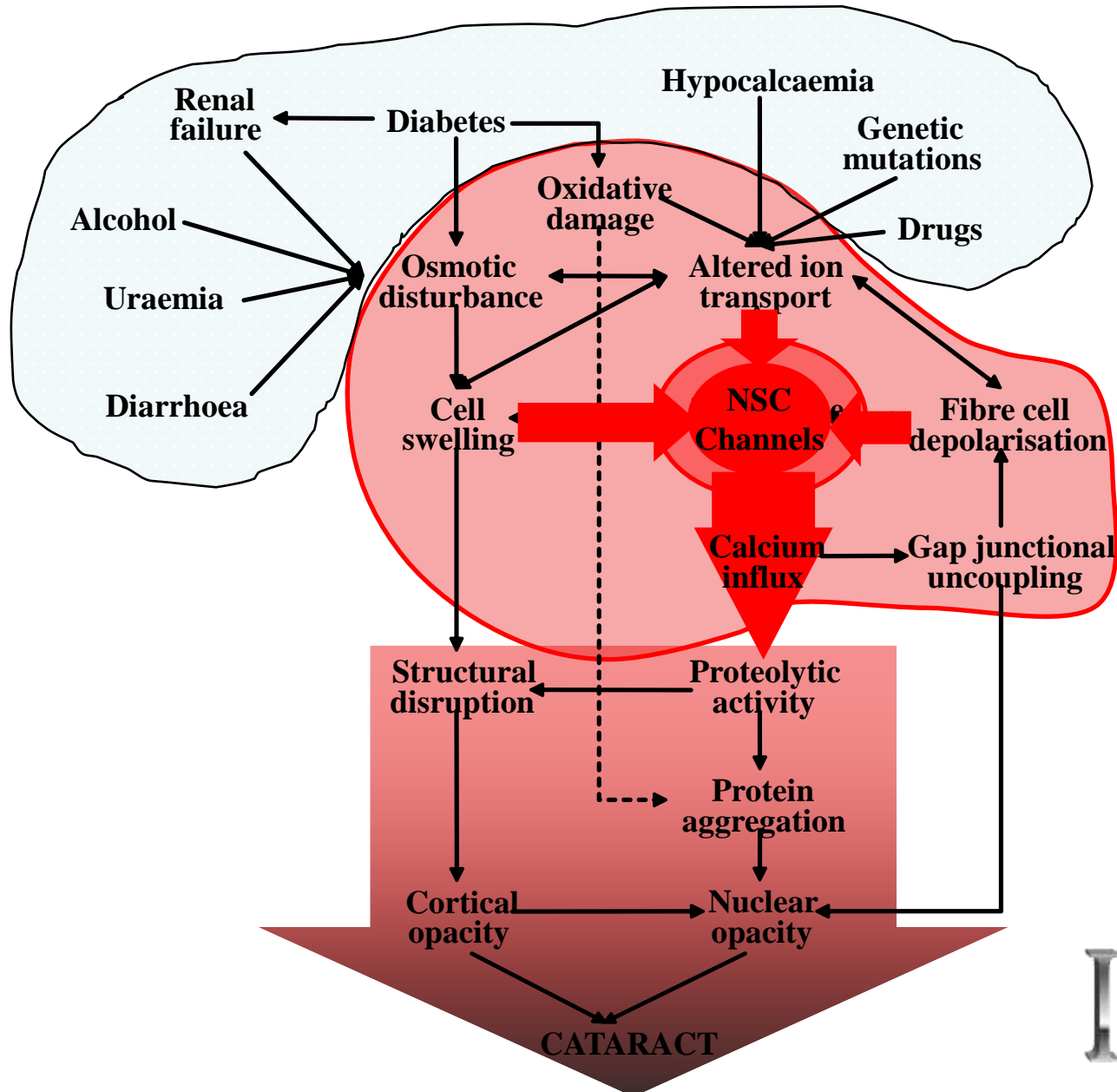


Hypotonic condition
(Cell swelling)

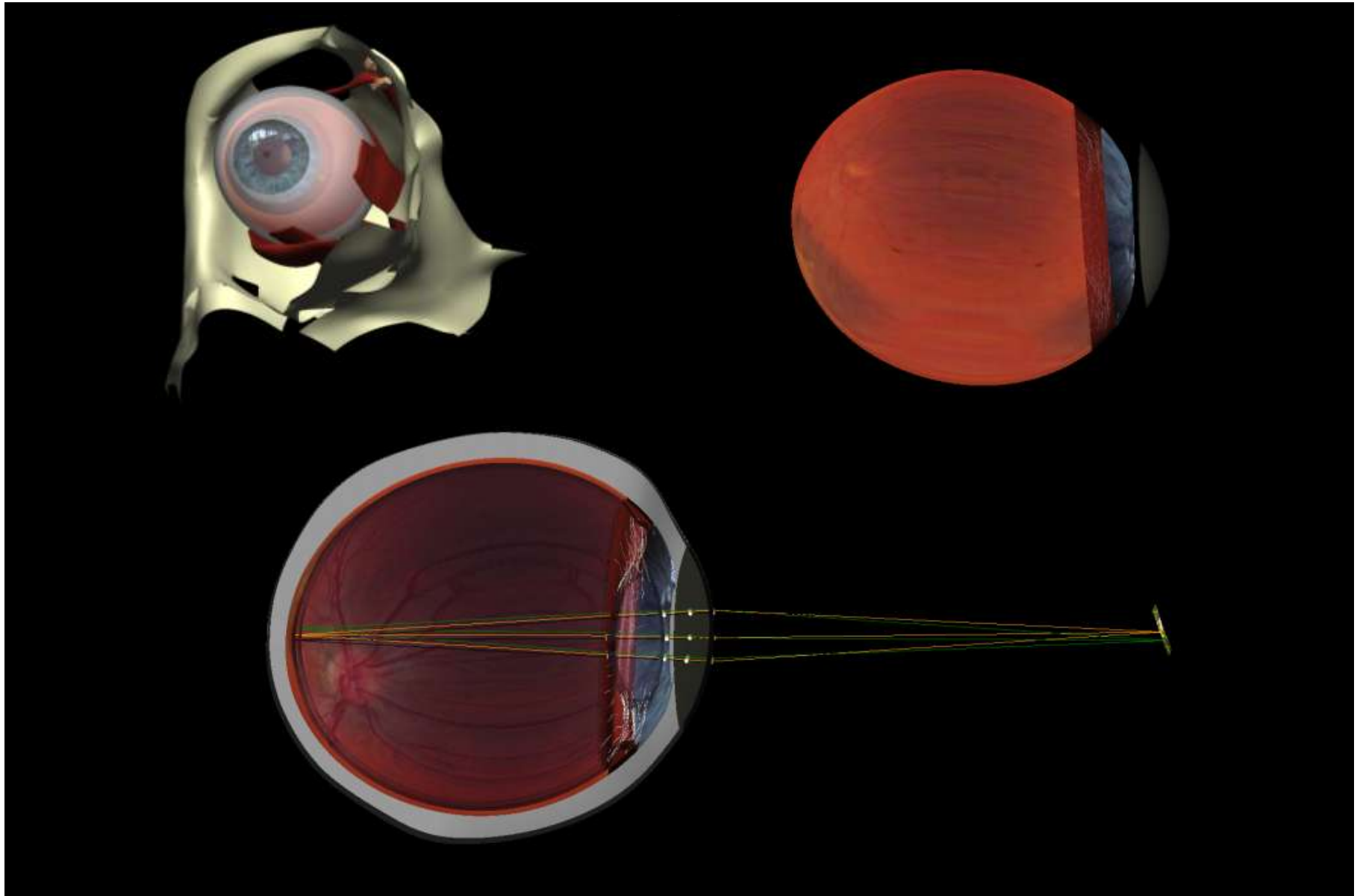


AG

Calcium influx and initiation of cataract



An integrated eye model



VPH/Physiome infrastructure

Modeling multiple cell processes

Individual models

- **Pandit et al. (2001): Cardiac electrophysiology**
 - ion channels, pumps, sarcoplasmic reticulum
- **Hinch et al. (2004): Calcium regulation**
 - LCC channels, dyadic space and RyR complexes
- **Niederer et al. (2006): Myofilament mechanics**
 - calcium binding to troponin, tropomyosin kinetics and cross-bridge dynamics.

Pandit et al. Model of cardiac action potential

Pandit SV, Clark RB, Giles WR, et al. A mathematical model of action potential heterogeneity in adult rat left ventricular myocytes. *Biophys J* 81(6):3029-51, 2001.

www.cellml.org/models/pandit_clark_giles_demir_2001_version11

[overview](#) [edit](#) [view math](#) [model metadata](#) [curation](#) [view cellml](#) [data](#) [procedural code](#)

A Mathematical Model of Action Potential Heterogeneity in Adult Rat Left Ventricular Myocytes



Download Model (151Kb)	Solve model in: (help)
Curation Status: ★☆☆	PCEnv ★☆☆ JSim ★☆☆ COR ★☆☆
	PCEnv Session (What's this?)

Model Documentation

Model Status

This CellML version of the model represents the epicardial cell. A number of inconsistencies in units and errors in equations from version 07 were fixed in this version. In addition to the formulation given by the paper and the author's later Corrections document, the IStim current has been adjusted to produce 1 Hz stimulations for 10 seconds.

Model Structure

Over the past decade electrophysiological studies have revealed transmural heterogeneity, or differences in the action potential waveforms recorded in cells isolated from the epicardial and the endocardial tissues in the left ventricles of mammalian hearts.

The adult rat has been widely used as an experimental model to investigate the electrical heterogeneity in the left ventricle under normal conditions and pathophysiological states. From this biophysical, experimental data, derived from patch clamp experiments, Sandeep V. Pandit, Robert B. Clark, Wayne R. Giles and Semahat S. Demir have developed a mathematical model of action potential heterogeneity in adult rat left ventricular myocytes (see the figure below). The mathematical models for the epicardial and endocardial cells of the rat left ventricle are based on the classical formulation of Hodgkin and Huxley (please see the CellML version of The Hodgkin-Huxley Squid Axon Model, 1952 for more details), and are therefore similar to previous computational work carried out by this research group (see Demir *et al.* Sinoatrial Node Model 1994 and Demir *et al.* Sinoatrial Node Model 1999). The endocardial cell model is based on the epicardial formulation with only slight modifications in certain parameters and equations.

The complete original paper reference is cited below:

[A Mathematical Model of Action Potential Heterogeneity in Adult Rat Left Ventricular Myocytes](#), , Sandeep V. Pandit, Robert B. Clark, Wayne R. Giles and Semahat S. Demir, 2001, [Biophysical Journal](#), 81, 3029-3051. ([Full text](#) and [PDF](#) versions of the article are available for Journal Members on the Biophysical Journal website.) [PubMed ID: 11720973](#)

File Tools View Help

Value Units

Type	Value	Units
V	-90.50146	millivolt
R	8314.5	millijoule_per_mole_kelvin
T	295	kelvin
F	96487	coulomb_per_mole
C_m	0.0001	microF
stim_start	0.1	second
stim_end	10	second
stim_period	1	second
stim_duration	0.005	second
stim_amplitude	-0.6	nanoA
g_{Na}	0.8	microS
m	0.004164108	dimensionless
h	0.6735613	dimensionless
j	0.6729362	dimensionless
g_{Ca_L}	0.031	microS
E_{Ca_L}	65	millivolt
d	0.000002171081	dimensionless
f_{11}	0.9999529	dimensionless
f_{12}	0.9999529	dimensionless
Ca_{inact}	0.9913102	dimensionless
$\tau_{Ca_{inact}}$	0.009	second
g_I	0.035	microS
a	0.886	dimensionless
b	0.114	dimensionless
r	0.002191519	dimensionless
s	0.9842542	dimensionless
s_{slow}	0.6421196	dimensionless
g_{SS}	0.007	microS



Start time point: 0 (second)

Point density_{max}: 100000 (points/graph)

End time point: 10 (second)

Absolute z: 1E-6

Relative s: 1E-6

Variable Scale Factor: 1.0

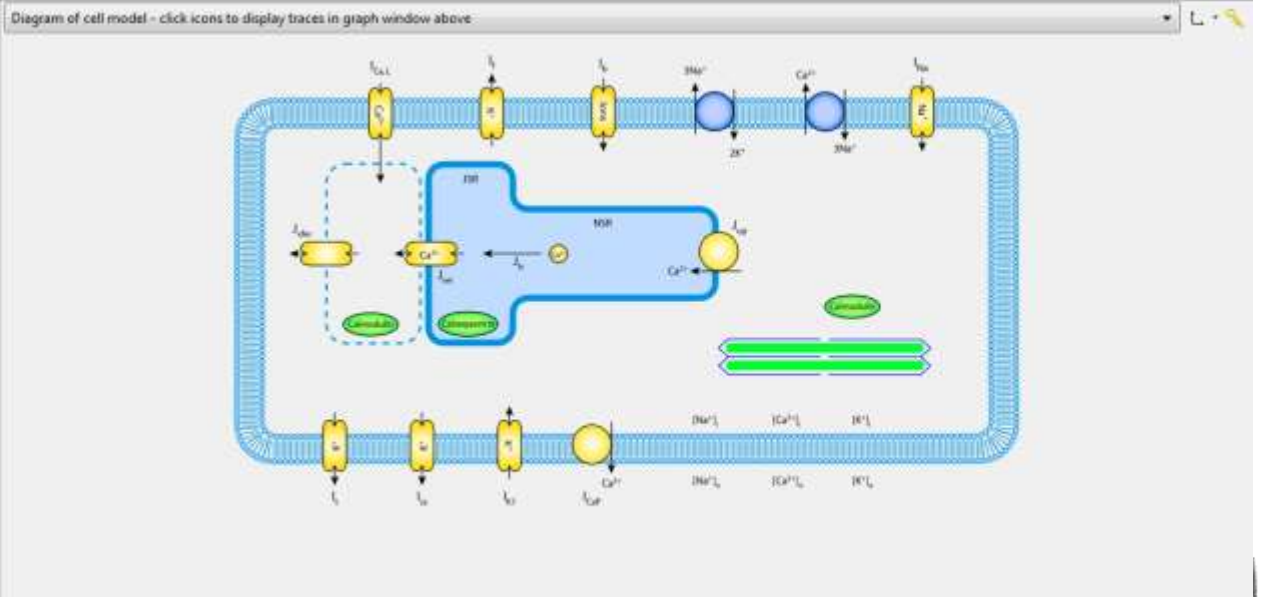
Rate Scale Factor: 0.0

Maximum step size: 0.001 (second)

Algorithm: BDF1-5 with solve

Integration Complete

Export CSV



Script Message: Displaying flux of I_f, I_h, I_NaP, I_Na, I_CaT, I_K, I_Ca_P



Hinch et al. Model of Ca-induced Ca release

Hinch R, Greenstein JR, Tanskanen AJ, et al. A simplified local control model of Ca-induced Ca release in cardiac ventricular myocytes. *Biophys J* 87:3723-3736, 2004.

www.cellml.org/models/hinch_greenstein_tanskanen_xu_winslow_2004_version02

[overview](#) [edit](#) [view math](#) [model metadata](#) [curation](#) [view cellml](#) [data](#) [procedural code](#)

A Simplified Local Control Model of Calcium-Induced Calcium Release in Cardiac Ventricular Myocytes



Download Model (113Kb)	Solve model in: (help)
Curation Status: ★★☆☆	PCEnv ★★☆☆ JSim ★☆☆☆ COR ★★☆☆
	PCEnv Session (What's this?)

Model Documentation

Model Status

This model is known to run in PCEnv and COR to reproduce the output shown in the publication. A PCEnv session file is also associated with this model.

Model Structure

This CellML model was based on the December 2004 paper:

"A Quantitative Analysis of Cardiac Myocyte Relaxation: A Simulation Study" by Hinch, Greenstein, Tanskanen, Xu and Winslow.

The following is the abstract of this paper:

Calcium (Ca²⁺)-induced Ca²⁺ release (CICR) in cardiac myocytes exhibits high gain and is graded. These properties result from local control of Ca²⁺ release. Existing local control models of Ca²⁺ release in which interactions between L-Type Ca²⁺ channels (LCCs) and ryanodine-sensitive Ca²⁺ release channels (RyRs) are simulated stochastically are able to reconstruct these properties, but only at high computational cost. Here we present a general analytical approach for deriving simplified models of local control of CICR, consisting of low-dimensional systems of coupled ordinary differential equations, from these more complex local control models in which LCC-RyR interactions are simulated stochastically. The resulting model, referred to as the coupled LCC-RyR gating model, successfully reproduces a range of experimental data, including L-Type Ca²⁺ current in response to voltage-clamp stimuli, inactivation of LCC current with and without Ca²⁺ release from the sarcoplasmic reticulum, voltage-dependence of excitation-contraction coupling gain, graded release, and the force-frequency relationship. The model does so with low computational cost.

The complete original publication reference is cited below:

[A Simplified Local Control Model of Calcium-Induced Calcium Release in Cardiac Ventricular Myocytes](#), R. Hinch, J.R. Greenstein, A.J. Tanskanen, L. Xu, R.L. Winslow, 2004 [Biophysical Journal](#), Volume 87 pp.3723-3736, PubMed ID: 15465866

Niederer et al. Model of myofilament mechanics

Niederer SA, Hunter PJ, Smith NP. A quantitative analysis of cardiac myocyte relaxation: a simulation study. *Biophys J* 90(5):1697-722, 2006.

www.cellml.org/models/niederer_hunter_smith_2006_version02

[overview](#) [edit](#) [view math](#) [model metadata](#) [curation](#) [view cellml](#) [data](#) [procedural code](#)

A quantitative analysis of cardiac myocyte relaxation: a simulation study

Download Model (52Kb)	Solve model in: (help)
Curation Status: ★★☆☆	PCEnv ★★☆☆ JSim ★☆☆☆ COR ★★☆☆
	PCEnv Session (What's this?)

Model Documentation

Model Status

This model is known to run in PCEnv and COR to reproduce the output shown in the publication. A PCEnv session file is also associated with this model.

Model Structure

This CellML model was based on the March 2007 paper:

"A Quantitative Analysis of Cardiac Myocyte Relaxation: A Simulation Study" by S.A. Niederer, P.J. Hunter and N.P. Smith.

The following is the abstract of this paper: The determinants of relaxation in cardiac muscle are poorly understood, yet compromised relaxation accompanies various pathologies and impaired pump function. In this study, we develop a model of active contraction to elucidate the relative importance of the $[Ca^{++}]_i$ transient magnitude, the unbinding of Ca^{++} from troponin C (TnC), and the lengthdependence of tension and Ca^{++} sensitivity on relaxation. Using the framework proposed by one of our researchers, we extensively reviewed experimental literature, to quantitatively characterize the binding of Ca^{++} to TnC, the kinetics of tropomyosin, the availability of binding sites, and the kinetics of crossbridge binding after perturbations in sarcomere length. Model parameters were determined from multiple experimental results and modalities (skinned and intact preparations) and model results were validated against data from length step, caged Ca^{++} , isometric twitches, and the half-time to relaxation with increasing sarcomere length experiments. A factorial analysis found that the $[Ca^{++}]_i$ transient and the unbinding of Ca^{++} from TnC were the primary determinants of relaxation, with a fivefold greater effect than that of length-dependent maximum tension and twice the effect of tension-dependent binding of Ca^{++} to TnC and length-dependent Ca^{++} sensitivity. The affects of the $[Ca^{++}]_i$ transient and the unbinding rate of Ca^{++} from TnC were tightly coupled with the effect of increasing either factor, depending on the reference $[Ca^{++}]_i$ transient and unbinding rate.

The complete original publication reference is cited below:

[A Quantitative Analysis of Cardiac Myocyte Relaxation: A Simulation Study](#), Steven Niederer, Peter Hunter, Nicholas Smith, 2006 [Biophysical Journal](#), 90 1697-1722 [PubMed ID: 16339881](#)

Type	Value	Units
TRPN	0.067593139865	mM
z	0.014417937837	dimensionless
alpha_0	8e-3	per_ms
alpha_1	2e-3	per_ms
alpha_2	1.75e-3	per_ms
n_Rel	3	dimensionless
K_z	0.15	dimensionless
n_Hill	3	dimensionless
Ca_50ref	1.05e-3	mM
z_p	0.85	dimensionless
beta_1	-4	dimensionless
Ca_TRPN_Max	70e-3	mM
k_on	100	per_mM_per_ms
k_Ref_off	0.2	per_ms
gamma_trpn	2	dimensionless
beta_0	4.9	dimensionless
T_ref	56.2	N_per_mm2
a	0.35	dimensionless
Q_1	0	dimensionless
Q_2	0	dimensionless
Q_3	0	dimensionless
A_1	-29	dimensionless
A_2	138	dimensionless
A_3	129	dimensionless
alpha_1	0.03	per_ms
alpha_2	0.13	per_ms
alpha_3	0.625	per_ms

Start time point: 0 (ms)

Point density_{max}: 10000 (points/graph)

End time point: 1000 (ms)

Absolute ϵ : 1E-6

Relative ϵ : 1E-6

Variable Scale Factor: 1.0

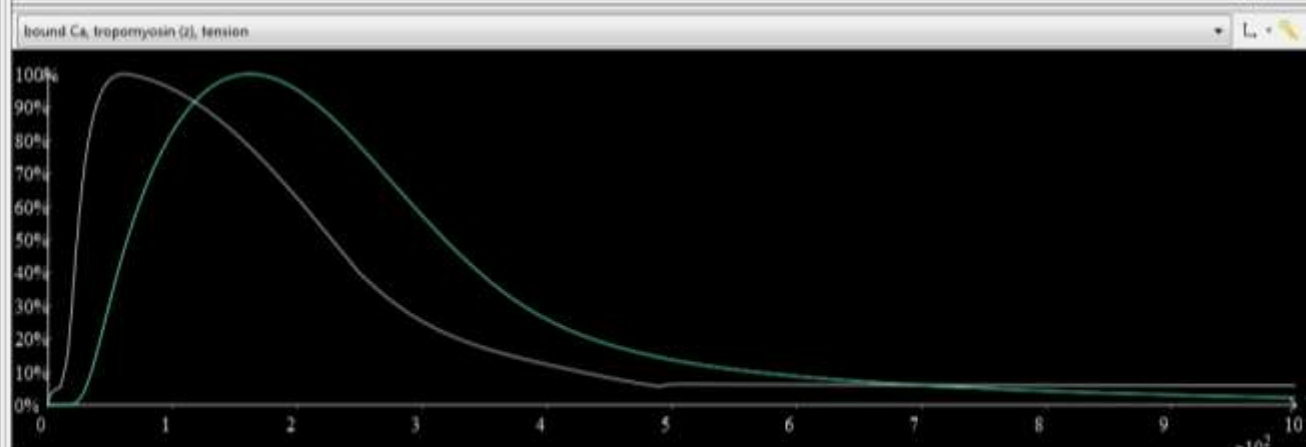
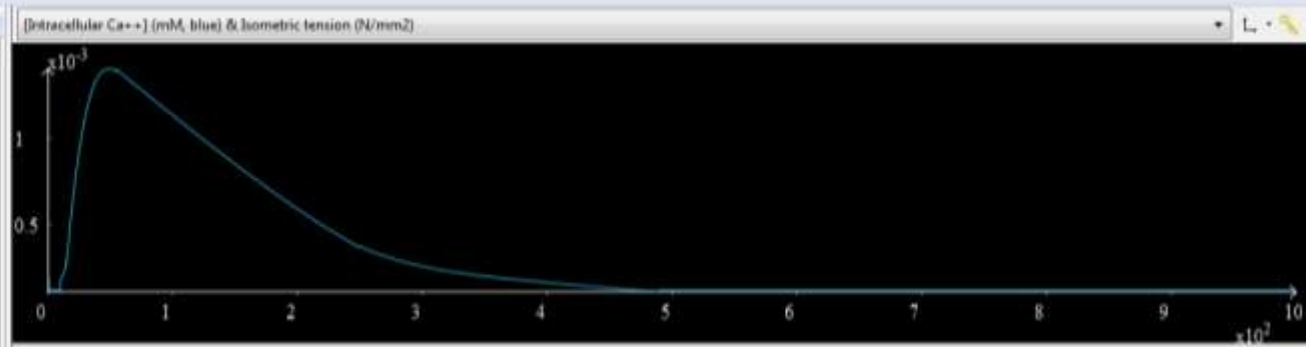
Rate Scale Factor: 0.0

Maximum step size: 0.1 (ms)

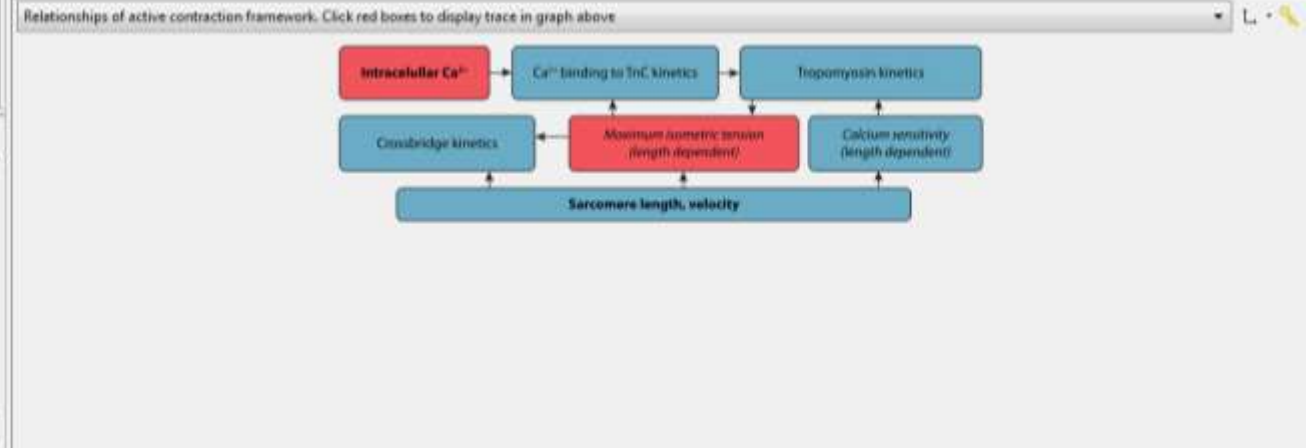
Algorithm: BDF 1-5 with solve

Integration Complete

Export CSV



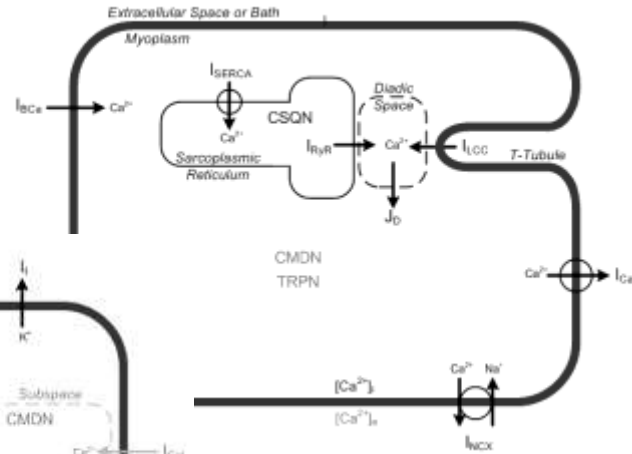
Model: V X Type



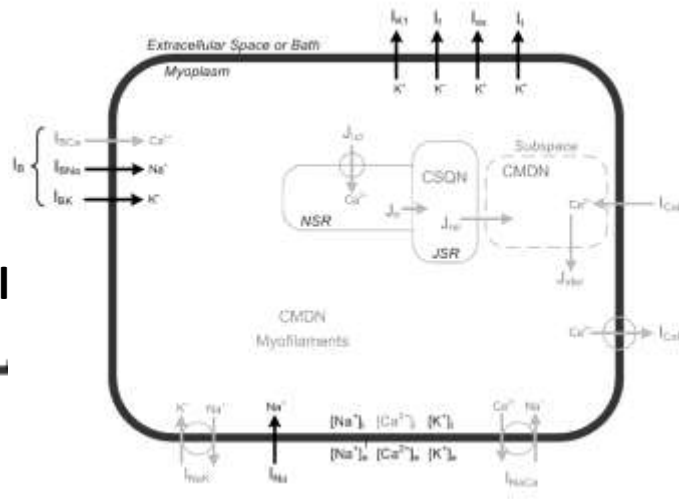
Integrated model of excitation-contraction coupling

CellML1.1 imports

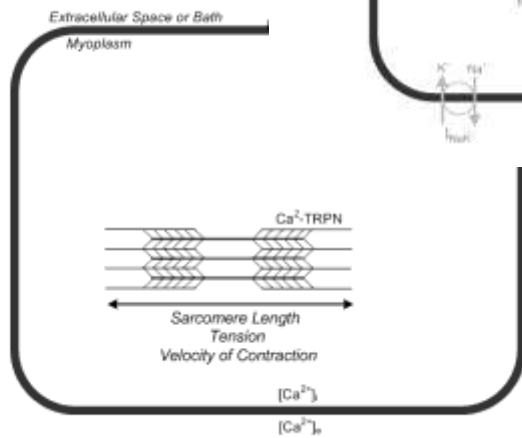
Hinch et al



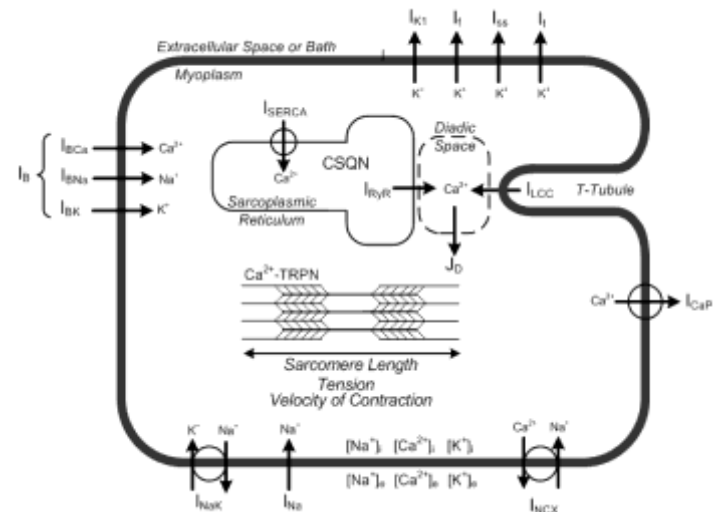
Pandit et al



Niederer et al



Complete model



Terkildsen, J.R., Niederer, S., Crampin, E.J., Hunter, P.J. and Smith, N.P. *Experimental Physiology* 93, pp919-929, 2008.

IMAG

Terkildsen et al. Integrated model of e-c coupling

Terkildsen JR, Niederer S, Crampin EJ, Hunter PJ, Smith NP. Using Physiome standards to couple cellular functions for cardiac excitation-contraction. *Experimental Physiology* 93, 919-929, 2008.

www.cellml.org/models/terkildsen_niederer_crampin_hunter_smith_2008_version02

overview edit view math model metadata curation view cellml data procedural code

Using Physiome standards to couple cellular functions for rat cardiac excitation-contraction

Download Model (220Kb)	Solve model in: (help)
Curation Status: ★★☆☆	PCEnv ★★☆☆ JSim ★★☆☆ COR ★★☆☆ PCEnv Session (What's this?)

Model Documentation

Model Status

Since this is the exact same model encoding which was used to create the results presented in the paper, this CellML model is known to accurately represent the published article.

Model Structure

ABSTRACT: Scientific endeavour is reliant upon the extension and reuse of previous knowledge. The formalization of this process for computational modelling is facilitated by the use of accepted standards with which to describe and simulate models, ensuring consistency between the models and thus reducing the development and propagation of errors. CellML 1.1, an XML-based programming language, has been designed as a modelling standard which, by virtue of its import and grouping functions, facilitates model combination and reuse. Using CellML 1.1, we demonstrate the process of formalized model reuse by combining three separate models of rat cardiomyocyte function (an electrophysiology model, a model of cellular calcium dynamics and a mechanics model) which together make up the Pandit-Hinch-Niederer et al. cell model. Not only is this integrative model of rat electromechanics a useful tool for cardiac modelling but it is also an ideal framework with which to demonstrate both the power of model reuse and the challenges associated with this process. We highlight and classify a number of these issues associated with combining models and provide some suggested solutions.

[Using Physiome standards to couple cellular functions for rat cardiac excitation-contraction](#), Jonna R. Terkildsen, Steven Niederer, Edmund J. Crampin, Peter Hunter and Nicolas P. Smith, 2008, [Experimental Physiology](#), 93, 919-929. ([Full text](#) and [PDF](#) versions of the article are available to journal subscribers on the *Experimental Physiology* website.)
[PubMed ID: 18344258](#)



Type	Value	Units
V	-78.8	mV
R	8314.5	m Ω _per_mole_K
T	295	kelvin
F	96487	C_per_mole
Cm	0.0001	μ F
stim_durati...	10	ms
stim_amplit...	-0.6e-3	μ A
V_myo	25.85e3	μ m 3
V_SR	2.098e3	μ m 3
V_myo_ul	25.85e-6	μ L
V_SR_ul	2.098e-6	μ L
g_Na	0.8e-3	mS
m	0.0054828	dimensionless
h	0.6095126	dimensionless
j	0.60876276	dimensionless
g_T	0.035e-3	mS
a_endo	0.583	dimensionless
b_endo	0.417	dimensionless
r	0.002542	dimensionless
s	0.8823	dimensionless
s_slow	0.42756	dimensionless
g_ss	0.007e-3	mS
r_ss	0.0033545	dimensionless
s_ss	0.266596	dimensionless
g_K1	0.024e-3	mS
g_f	0.00145e-3	mS
f_Na	0.2	dimensionless
y	0.0026369	dimensionless

Start time point: 0 (ms)

Point density_{max}: 10000 (points/graph)

End time point: 5000 (ms)

Absolute ϵ : 1E-6

Relative ϵ : 1E-6

Variable Scale Factor: 1.0

Rate Scale Factor: 0.0

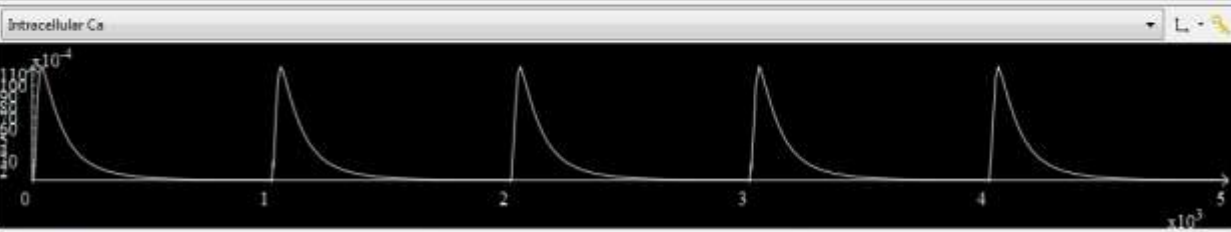
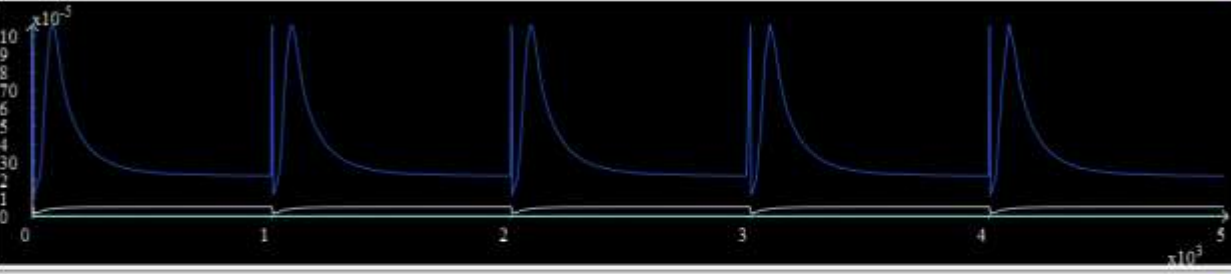
Maximum step size: 0.1 (ms)

Algorithm: BDF 1-5 with solve

Integration Complete

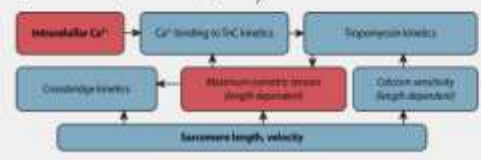
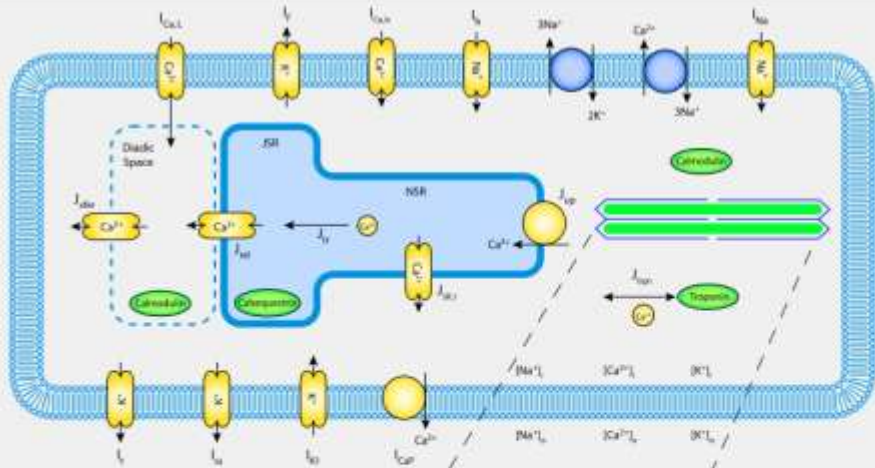
Export CSV

Currents (microA), fluxes (mM/ms), concentrations (mM), isometric tension (N/mm 2)



Model Y X Type

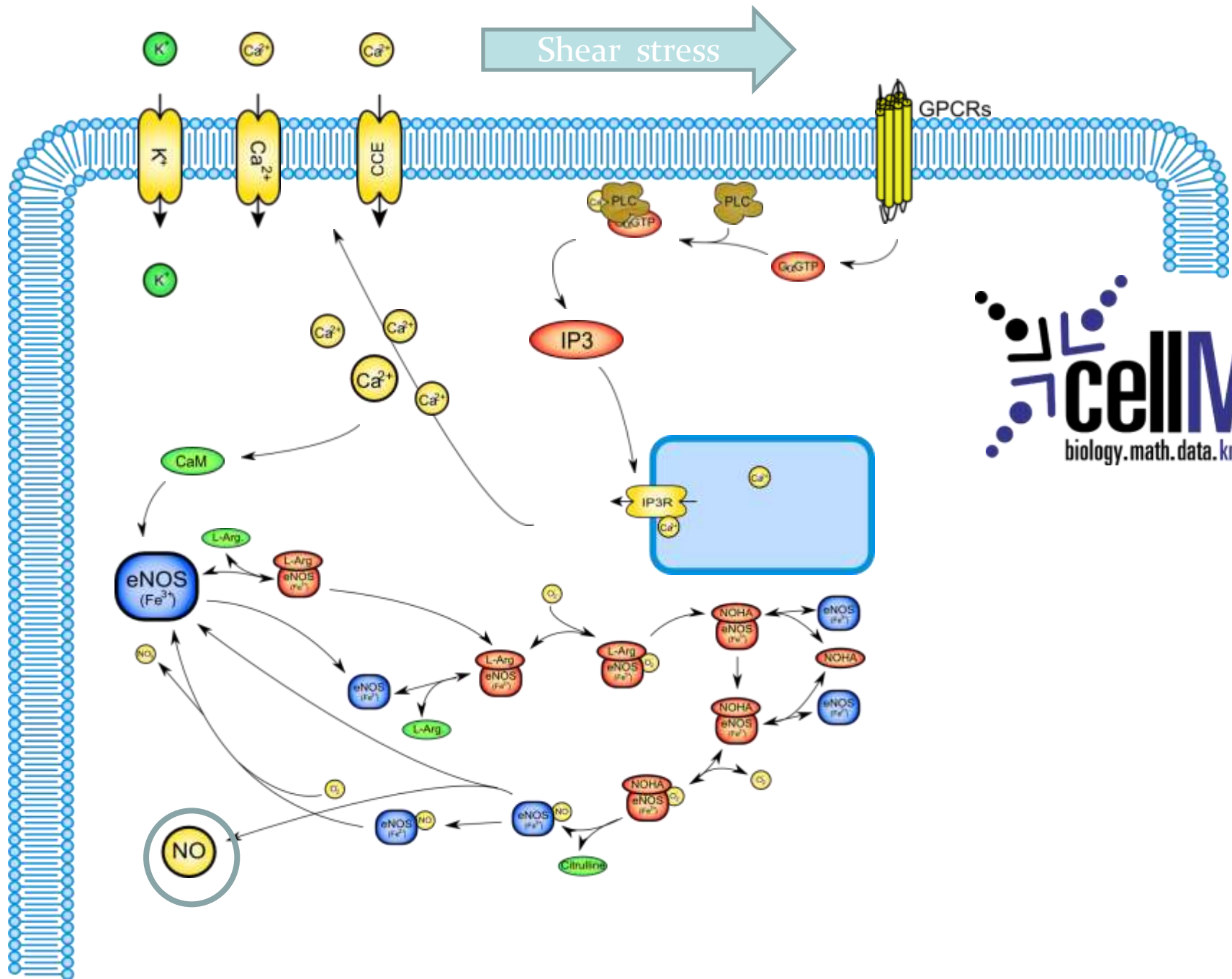
Cell model (Pandit-Hinch) and active contraction framework (Niederer) - click icons to display traces in graph window above



Example of module reuse

NO production in Endothelial Cells

- **Stretch activated channels → Ca²⁺ → NO (< 1 min)**
- **Additional signalling pathways (1 min – 1 hr)**
 - **GPCRs → IP3 → Ca²⁺ → NO**
 - **Glycocalyx → NO?**
 - **PI3K → Akt → NO**
 - **Stretch activated channels → PKC → MAPK → NO**
 - **PI3K → MAPK → NO**
 - **Integrins (tensegritous) → MAPK → NO**
- **Gene regulation effects (1- 6 hours)**



Key requirements for modeling infrastructure

- 1. Minimum information standards**
- 2. Markup languages for models and data**
- 3. ML standard for the simulation experiment**
- 4. Models and data repositories**
- 5. Meta data standards for annotating the models**
- 6. Tools for authoring models, running simulations, visualising models and data**
- 7. Mechanisms for handling the reference description of a model**

1. Minimum information standards

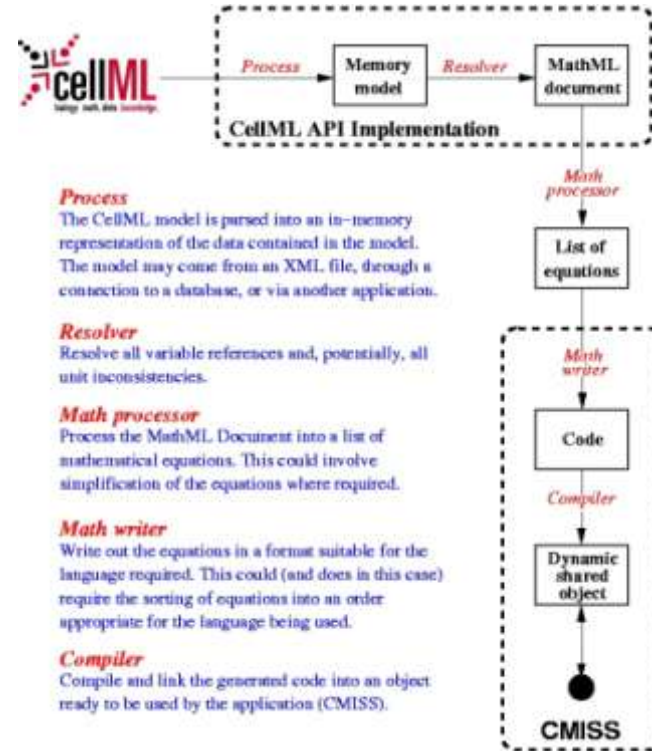
1. MIRIAM for models

www.ebi.ac.uk/miriam/main/mdb?section=standard

2. MIASE for simulations

www.ebi.ac.uk/compneur-srv/miase/

2. Markup languages for models and data



- Models:** CellML www.cellml.org
SBML www.sbml.org
FieldML www.fieldml.org
- Data:** DICOM, BioSignalML, ...





You are here: [Home](#)

The CellML project

The CellML language is an open standard based on the XML markup language. CellML is being developed by the Auckland Bioengineering Institute at the University of Auckland and affiliated research groups.

The purpose of CellML is to store and exchange computer-based mathematical models. CellML allows scientists to share models even if they are using different modelling tools. It also enables them to reuse components from one model in another, thus accelerating model development. [Read more...](#)

About CellML

Find out about the CellML language; what it can be used for, its history, and future directions.

Tools

The CellML community is committed to providing freely available tools for creating, editing, and using CellML models.

Specifications

Read the CellML specifications - core language and a variety of metadata specifications are available.

Getting Started

New to CellML? This section collates information about CellML and tutorials that will help get you up and running with CellML.

Model repository

The model repository is a resource where modelers can collaborate with each other to build and share models with the rest of the world.

Community

CellML is built around open source science and software. The cellml.org website is a community hub for all things CellML.

CellML at IUPS2009

Members of the CellML project will run a tutorial at IUPS2009 to provide hands-on experience of CellML and other Physiome Project software. - [Resources](#) for tutorial attendees



Photo: [flowzim](#)

Featured articles

- [Modelling Tools: PCEnv, COR & OpenCell](#)
- [CellML Workshop 2009 report](#)
- [CellML scope](#)
- [CellML publications listing](#)
- [OpenCell basic model building tutorial](#)
- [Frequently Asked Questions](#)

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- [CellML tutorial at IUPS2009](#)
- [IUPS2009 CellML workshop announcement](#)
- [CellML Tools page updated](#)
- [Notification: Representation of e-notation in CellML Repository models will be changing](#)
- [Request for details of CellML-related publications](#)
- [Friendfeed for CellML SBGN SBO BioPAX MIASE Workshop](#)
- [PCEnv 0.6 and CellML API 1.6 Released](#)
- [Request for model translations into CellML](#)

[More...](#)

Funding agencies

Thanks to our [funding partners](#): VPH NoE, Maurice Wilkins Centre for Molecular Biodiscovery, aneurIST, IUPS Physiome Project, Wellcome Trust.



3. ML standard for simulation experiments

SED-ML: www.ebi.ac.uk/compneur-srv/sed-ml/

SED-OM is object model defined in UML

Top-level SED-OM classes:

- Model
- Simulation
- Task
- DataGenerator
- Output

SED-ML is XML serialization of SED-OM

Ontology is KiSAO :

www.ebi.ac.uk/compneur-srv/kisao/

IMAG

4. Models and data repositories

CellML www.cellml.org/models

SBML www.biomodels.org

JSIM nsr.bioeng.washington.edu/jsim/models

You are here: [Home](#)

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- [Resources](#) for tutorial attendees











Photo: [flowzim](#)

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-  [Frequently Asked Questions](#)

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-  [Friendfeed for CellML SBG SBO BioPAX MIASE Workshop](#)
-  [PEnv 0.6 and CellML API 1.6 Released](#)
-  [Request for model translations into CellML](#)

[More...](#)

Funding agencies

Thanks to our [funding partners](#): VPH NoE, Maurice Wilkins Centre for Molecular Biodiscovery, aneurIST, IUPS Physiome Project, Wellcome Trust.

www.cellml.org/models

CellML Model Repository

Main Model Listing

The list of processed model exposures (formats: [100 per page](#) | [full list](#)), which are models that have documentation pages generated from the metadata they contain. Alternatively, you may start browsing via the categories that are listed below:

Please note: Comments about the functional status or curation status of the models within this repository are the opinions of the CellML Model Repository curators. We do our best to accurately represent these models, but please [contact us](#) if you have a query or issue with comments made on this site.

Browse by category

- [Calcium Dynamics](#)
- [Cardiovascular Circulation](#)
- [Cell Cycle](#)
- [Cell Migration](#)
- [Circadian Rhythms](#)
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- [Signal Transduction](#)
- [Synthetic Biology](#)

Searching

Searching of models can be done anywhere on the site using the search box on the upper right hand corner.



Electrophysiology


Electrophysiology

 [Adrian, Chandler, Hodgkin, 1970](#)

Voltage clamp experiments in striated muscle fibres

 [Albrecht, Colegrove, Friel, 2002](#)


Differential Regulation of ER Ca²⁺ Uptake and Release Rates Accounts for Multiple Modes of Ca²⁺-induced Ca²⁺ Release

 [Albrecht, Colegrove, Hongpaisan, Pivovarova, Andrews, Friel, 2001](#)

Multiple Modes of Calcium-induced Calcium Release in Sympathetic Neurons I: Attenuation of Endoplasmic Reticulum Ca²⁺ Accumulation at Low [Ca²⁺]_i during Weak Depolarisation

 [Beeler, Reuter, 1977](#)

Reconstruction of the action potential of ventricular myocardial fibres

 [Bernus, Wilders, Zemlin, Verscelde, Panfilov, 2002](#)

A computationally efficient electrophysiological model of human ventricular cells

 [Bertram, Previte, Sherman, Kinard, Satin, 2000](#)

The Phantom Burster Model for Pancreatic Beta Cells

 [Bertram, Satin, Zhang, Smolen, Sherman, 2004](#)

Calcium and Glycolysis Mediate Multiple Bursting Modes in Pancreatic Islets (a)

 [Bertram, Sherman, 2004](#)

A Calcium-based Phantom Bursting Model for Pancreatic Islets

 [Bertram, Smolen, Sherman, Mears, Atwater, Martin, Soria, 1995](#)

A role for calcium release-activated current (CRAC) in cholinergic modulation of electrical activity in pancreatic beta-cells

 [Bondarenko, Szigeti, Bett, Kim, Rasmusson, 2004](#)


A Computer Model for the Action Potential of Mouse Ventricular Myocytes (a)

 [Boyett, Zhang, Garny, Holden, 2001](#)


Control of the pacemaker activity of the sinoatrial node by intracellular Ca²⁺. Experiments and modelling

 [Butera, Rinzel, Smith, 1999](#)


Models of Respiratory Rhythm Generation in the Pre-Botzinger Complex. I. Bursting Pacemaker Neurons

 [Chang, Fujita, 1999](#)

A kinetic model of the thiazide-sensitive Na-Cl cotransporter (a)

 [Chang, Fujita, 1999](#)

A kinetic model of the thiazide-sensitive Na-Cl cotransporter (b)

 [Chang, Fujita, 1999](#)

A numerical model of the renal distal tubule

 [Chang, Fujita, 2001](#)





A numerical model of acid-base transport in rat distal tubule (renal_anion_exchanger_model)



Modulatory effect of calmodulin-dependent kinase II (CaMKII) on sarcoplasmic reticulum Ca²⁺ handling and interval-force relations: a modelling study.

General Information

PMR1 Curation

Curation Status: 
OpenCell: 
JSim: 
COR: 

Access model via:

[Download](#)
[Solve using OpenCell](#)
[Solve using OpenCell Session File](#)

Source:

Derived from workspace [Iribe](#), Kohl, Noble, 2006 at changeset [1b57f226158b](#).

Documentation

Model Status

This model was created by Penny Noble of Oxford University. An unsupported predefined operator diff error in component intracellular_calcium_concentration was fixed to allow the model to run in PCEnv (19/04/07, James Lawson.) A stimulus protocol was then added to allow simulation of trains of action potentials (JL, 15/06/07.) This file is known to run COR and PCEnv. A PCEnv session file is also associated with this model.

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Modulatory effect of calmodulin-dependent kinase II (CaMKII) on sarcoplasmic reticulum Ca²⁺ handling and interval-force relations: a modelling study.

by [Iribe](#) G, Kohl P, Noble D

Philos Transact A Math Phys Eng Sci. 2006 May 15;364(1842):1107-33

ABSTRACT:

We hypothesize that slow inactivation of Ca²⁺/calmodulin-dependent kinase II (CaMKII) and its modulatory effect on sarcoplasmic reticulum (SR) Ca²⁺ handling are important for various interval-force (I-F) relations, in particular for the beat interval dependency in transient alternans during the decay of post-extrasystolic potentiation. We have developed a mathematical model of a single cardiomyocyte to integrate various I-F relations, including alternans, by incorporating a conceptual CaMKII kinetics model into the SR Ca²⁺ handling model. Our model integrates I-F relations, such as the beat interval-dependent twitch force duration, restitution and potentiation, positive staircase phenomenon and alternans. We found that CaMKII affects more or less all I-F relations, and it is a key factor for integration of the various I-F relations in

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Modulatory effect of calmodulin-dependent kinase II (CaMKII) on sarcoplasmic reticulum Ca²⁺ handling and interval-force relations: a modelling study.



Mathematics

Component: transient_outward_current_r_gate

$$\frac{dr}{dt_{\text{time}}} = 333 \left(1 / \left(1 + e^{-(V+4)/5} \right) - r \right)$$

Component: L_type_Ca_channel

$$i_{\text{Ca}_L\text{Ca}} = 4dfP_{\text{Ca}_L\text{Ca}}(V - 50)F/RT \left(1 - e^{-2(V-50)F/RT} \right) \left(\text{Ca}_{\text{ie}}^{100F/RT} - \text{Ca}_{\text{oe}}^{-2(V-50)F/RT} \right)$$

$$i_{\text{Ca}_L\text{K}} = 0.002dfP_{\text{Ca}_L\text{Ca}}(V - 50)F/RT \left(1 - e^{-(V-50)F/RT} \right) \left(\text{K}_{\text{ie}}^{50F/RT} - \text{K}_{\text{oe}}^{-(V-50)F/RT} \right)$$

$$i_{\text{Ca}_L\text{Na}} = 0.01dfP_{\text{Ca}_L\text{Ca}}(V - 50)F/RT \left(1 - e^{-(V-50)F/RT} \right) \left(\text{Na}_{\text{ie}}^{50F/RT} - \text{Na}_{\text{oe}}^{-(V-50)F/RT} \right)$$

$$i_{\text{Ca}_L} = i_{\text{Ca}_L\text{Ca}} + i_{\text{Ca}_L\text{K}} + i_{\text{Ca}_L\text{Na}}$$

Component: L_type_Ca_channel_d_gate

$$E0_d = V + 24 - 5$$

$$\alpha_{\text{d}} = \begin{cases} \text{speed_d} \times 120 & \text{if } |E0_d| < 0.00001 \\ \text{speed_d} \times 30 E0_d / \left(1 - e^{-E0_d/4} \right) & \text{if } |E0_d| \geq 0.00001 \end{cases}$$



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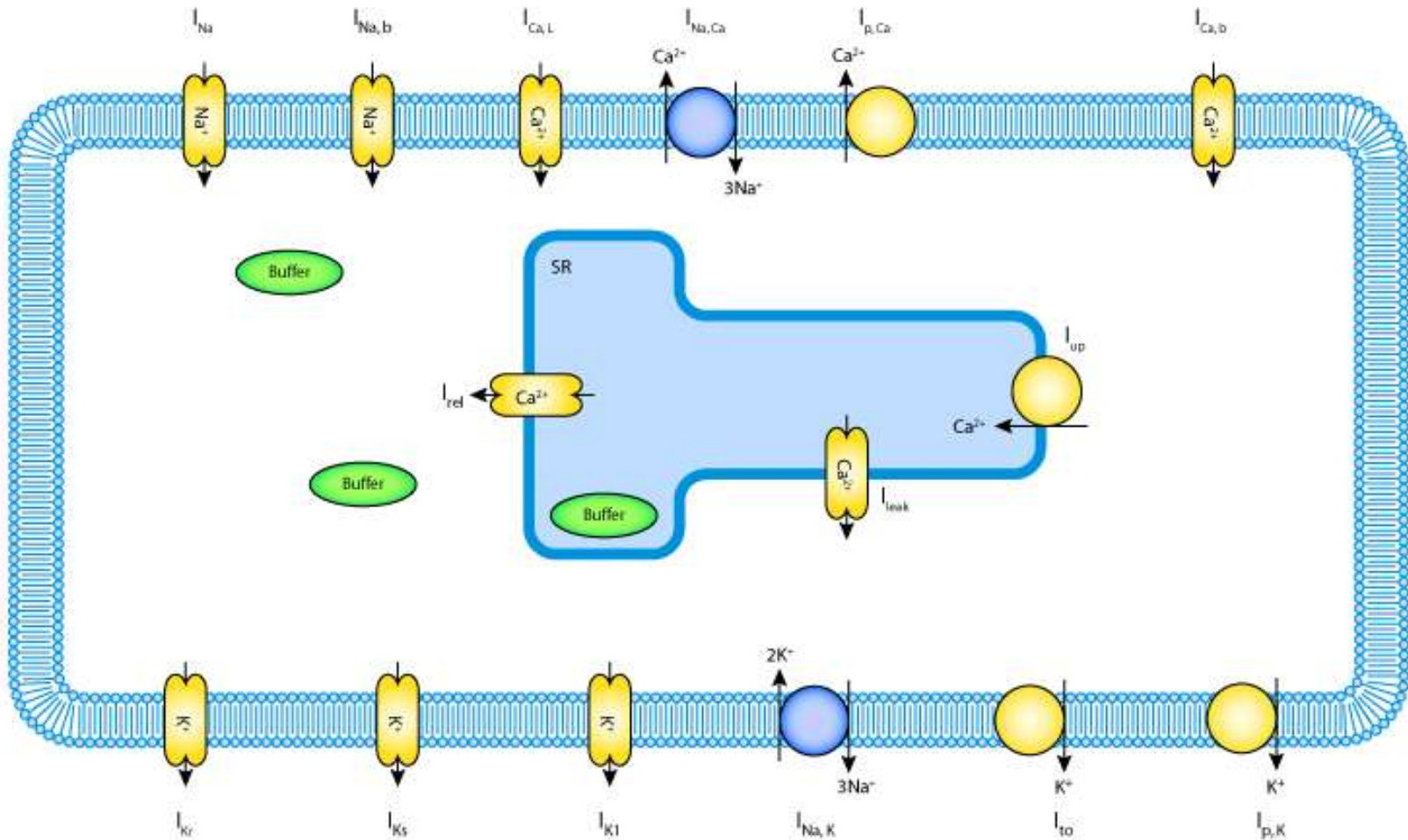
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SVG diagrams



A schematic diagram describing the ion movement across the cell surface membrane and the sarcoplasmic reticulum, which are described by the Ten Tusscher *et al.* 2004 mathematical model of the human ventricular myocyte.

5. Meta data standards for annotating models

Graphing metadata:

www.cellml.org/specifications/metadata/graphs

Other work:

SemSim from Dan Cook, U Washington, Seattle

Saint from Allyson Lister, Newcastle University

Ontologies: GO, BioPax, FMA, etc

– adhere to OBO Foundry, EBI, NCBO

IMAG

6. Tools for authoring models, running simulations, visualising models and data

OpenCell	<u>www.cellml.org/tools/opencell</u>
OpenCMISS	<u>www.cmiss.org/openCMISS</u>
CMGUI	<u>www.cmiss.org/cmgui</u>
GIMIAS	<u>www.gimias.org</u>
Continuity, MAF5, OpenSIM, etc	

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Modulatory effect of calmodulin-dependent kinase II (CaMKII) on sarcoplasmic reticulum Ca²⁺ handling and interval-force relations: a modelling study.



OpenCell simulation tool for CellML models

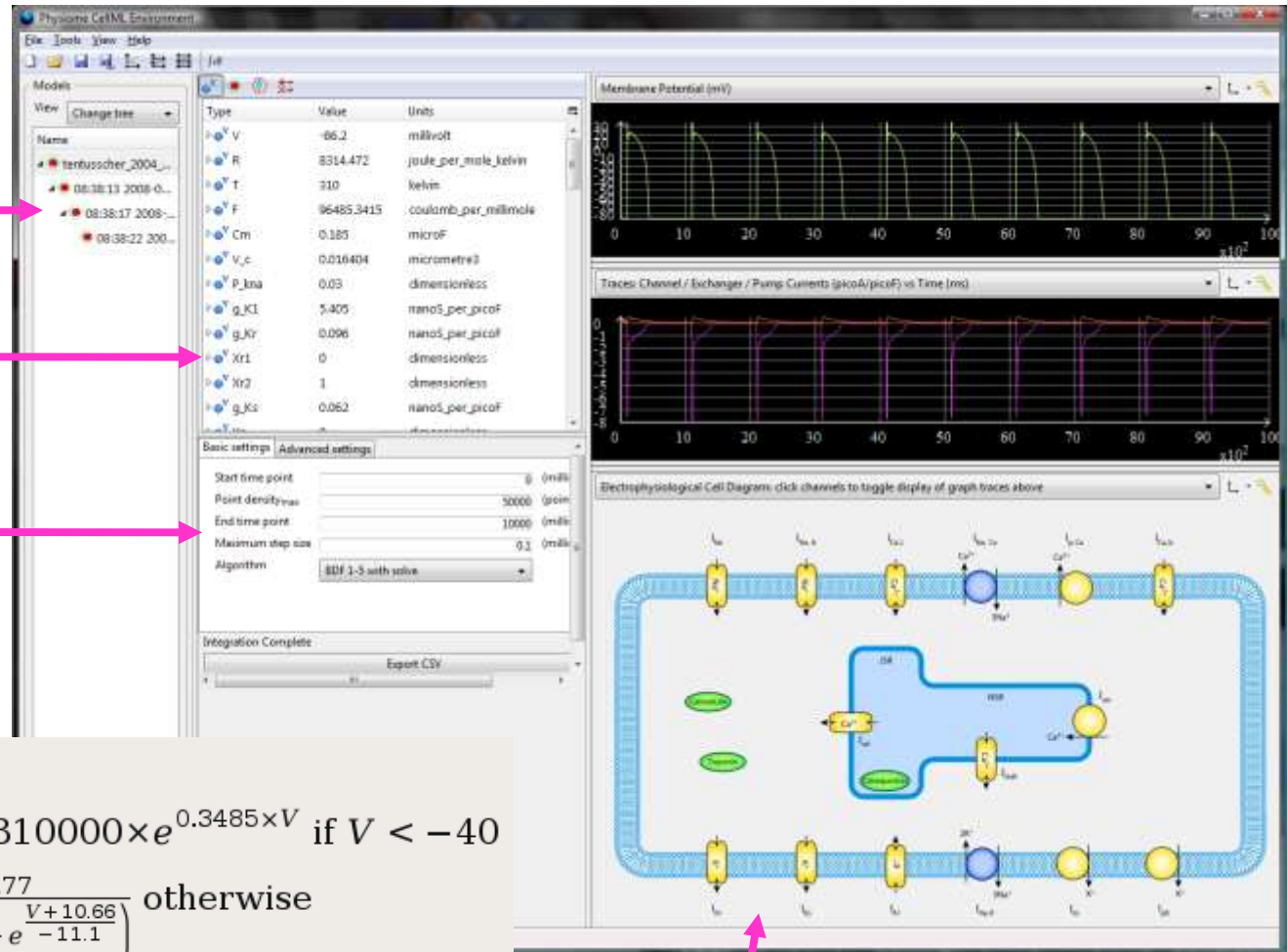
Multiple models or history of parameter changes

Parameter values & units

Parameters for control of numerical integration

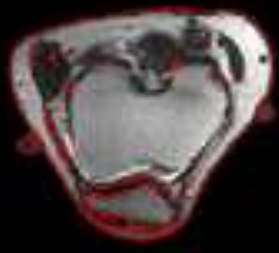
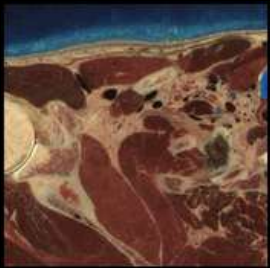
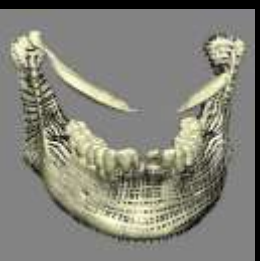
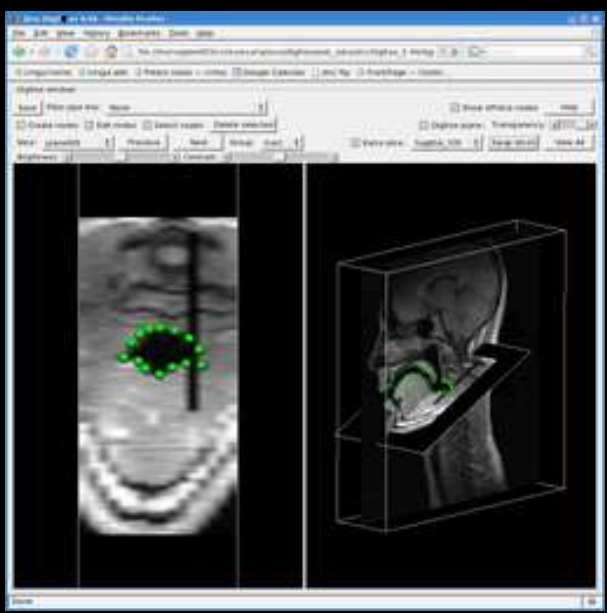
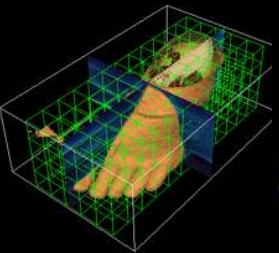
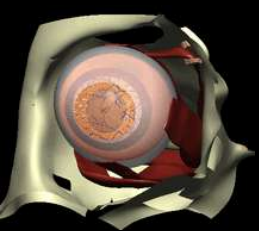
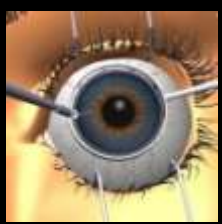
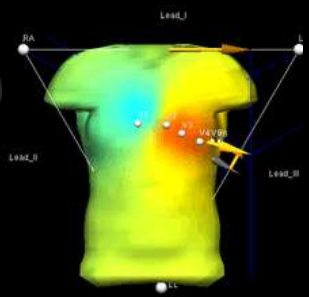
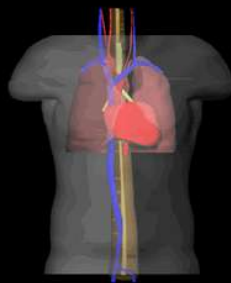
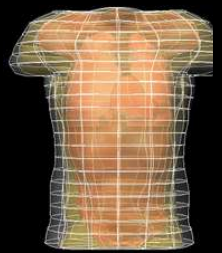
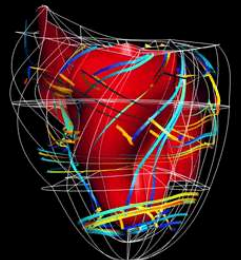
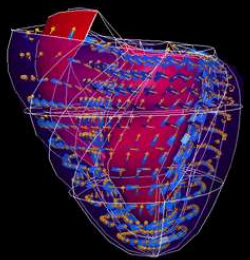
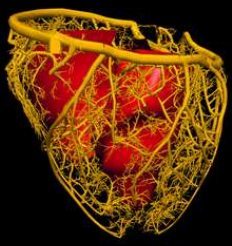
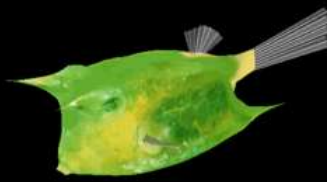
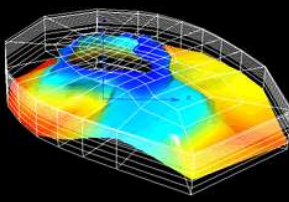
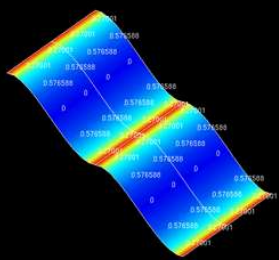
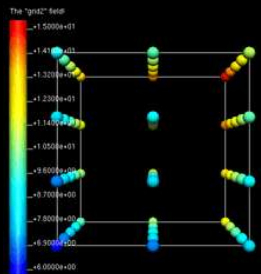
Equation for a component:

$$\text{beta}_h = \begin{cases} 2.7 \times e^{0.079 \times V} + 310000 \times e^{0.3485 \times V} & \text{if } V < -40 \\ \frac{0.77}{0.13 \times \left(1 + e^{\frac{V+10.66}{-11.1}}\right)} & \text{otherwise} \end{cases}$$



Graphical user interface for displaying model topology and controlling visibility of displayed results

FieldML & Cmgui (www.cmiss.org/cmgui)



Key points

- **Models now being built into some clinical workflows**
- **Good connection between imaging & modeling**
- **Connecting to systems biology is still not there**
- **Parameter variability in population hardly addressed**
- **Modeling standards in fairly good shape**
- **Alarming absence of data standards**
- **Model repositories OK but not yet data repositories**
- **Open source software for all scales is now available but need much more attention to multiscale/modules and automated model reduction**
- **Badly need demonstrated reproducibility of models/data i.e. Need model reference descriptions**
- **Need reference problems & competitions**