

The Multiscale Modeling Consortium
celebrates 20 years of IMAG:

June
28 & 29
2023

Natcher Conference
Center, NIH

Lessons from the past
that guide the future



Multiscale Modeling is Life

Denise Kirschner, University of Michigan Medical School

Paraphrased from Dani Rojas, Ted Lasso

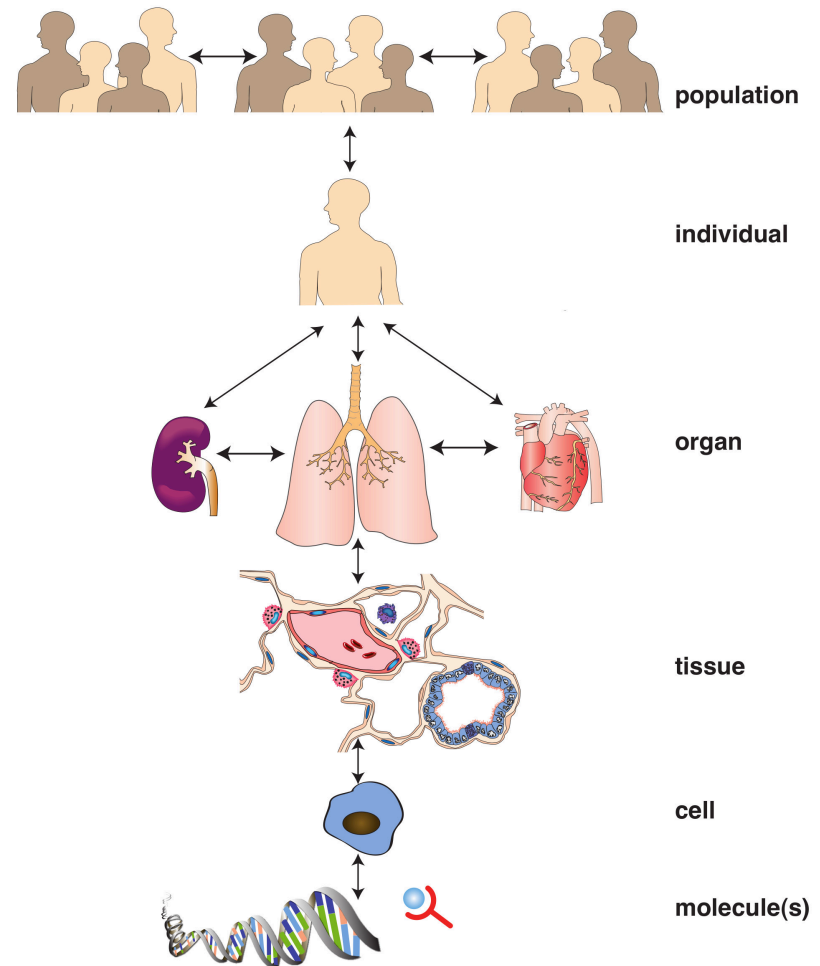


Two cautionary tales that yield advice

Be prudent when
offering
comments/advice

Never miss a
committee
meeting

Multiscale
models capture
processes
ranging over
time & space
(MSMs)



Questions for MSMs

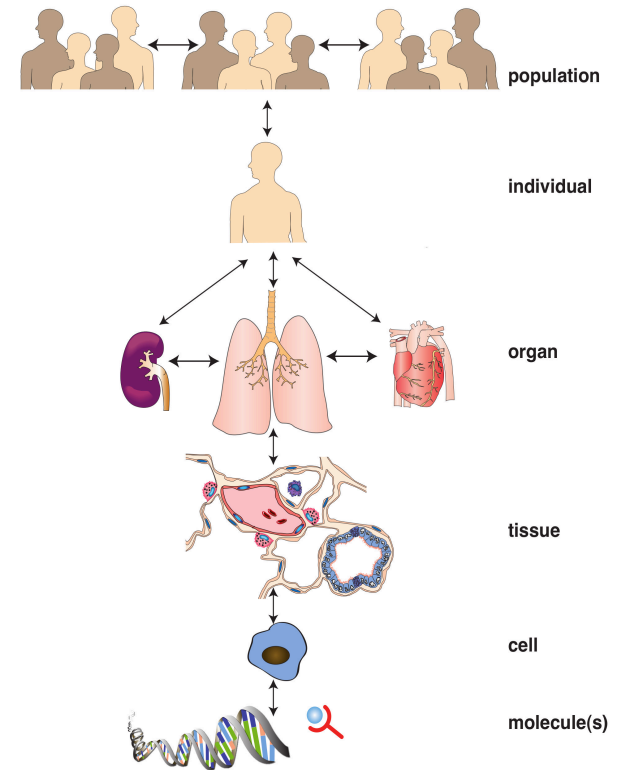
- How do we build MSMs?
- How do we link scales?
- How do we calibrate MSMs?
- How do we simulate?
- How do we ensure MSMs are robust/credible?
- How do we analyze MSMs?
- How do we validate MSMs?
- How can MSMs be useful?
- Where do we go next?



How do we build MSMs?

1) What scale do you begin?

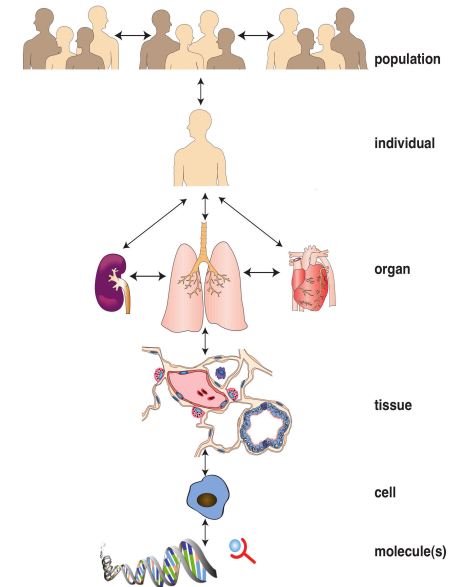
- a. Top down
- b. Bottom up
- c. Meso-scale (in-out)



2) What modeling approach is most appropriate?

How do we build MSMs?

| Biological Scale | | | Modeling Tool | |
|----------------------------|----------------|---------------------|------------------------------|----------------------|
| | <i>Time</i> | <i>Length</i> | <i>Dynamics</i> | <i>Model Type</i> |
| Genetic/ Molecular | 10^1-10^2 s | $10^{-9}-10^{-8}$ m | Deterministic, continuous | Statistical |
| Intracellular /Cellular | 10^1-10^3 s | 10^{-5} m | Deterministic, continuous | Mathematical: ODE |
| Tissue | $10^4 -10^5$ s | $10^{-3}-10^{-2}$ m | Stochastic, discrete | Algorithmic: ABM |
| Organ/ organism | 10^5-10^6 s | $10^{-2}-1$ m | Deterministic | Hybrid: ODE+ABM |



Modeling Approaches example:


- **What is the most appropriate approach to model granulomas?**
- ODEs- Wigginton J and Kirschner D. **A Model to Predict Cell-Mediated Immune Regulatory Mechanisms During Human Infection with Mycobacterium tuberculosis**, J. Immunology 166: pp 1951-1976, 2001
- PDEs-- Gammack, C.R. Doering, D.E. Kirschner, **Macrophage response to Mycobacterium tuberculosis infection** Journal of Mathematical Biology. Published online: 20 August 2003, In print: Vol 48(2) February 2004
- Metapopulations- Suman Ganguli, David Gammack, Denise E. Kirschner, **A Metapopulation Model of Granuloma Formation in the Lung During Infection with Mycobacterium Tuberculosis**, Mathematical Biosciences and Engineering, Volume 2, Number 3, Aug 2005
- ABMs/IBMs--Jose L. Segovia-Juarez, Suman Ganguli, and Denise Kirschner, **Identifying control mechanism of granuloma formation during M. tuberculosis infection using an agent based model**, Journal of Theoretical Biology. 231, Issue 3, pp 357-376, 2004

MULTISCALE MODEL. SIMUL.
Vol. 3, No. 2, pp. 312-345

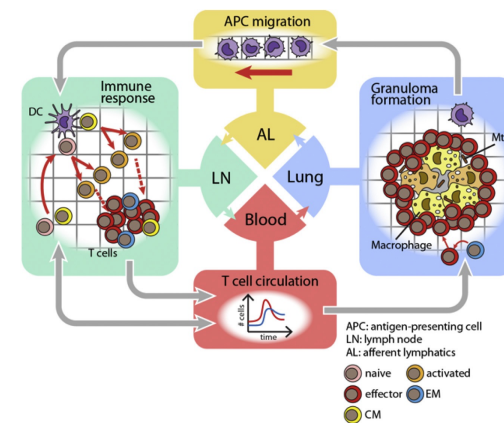
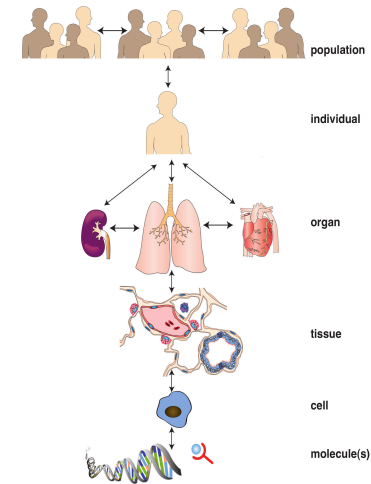
© 2005 Society for Industrial and Applied Mathematics

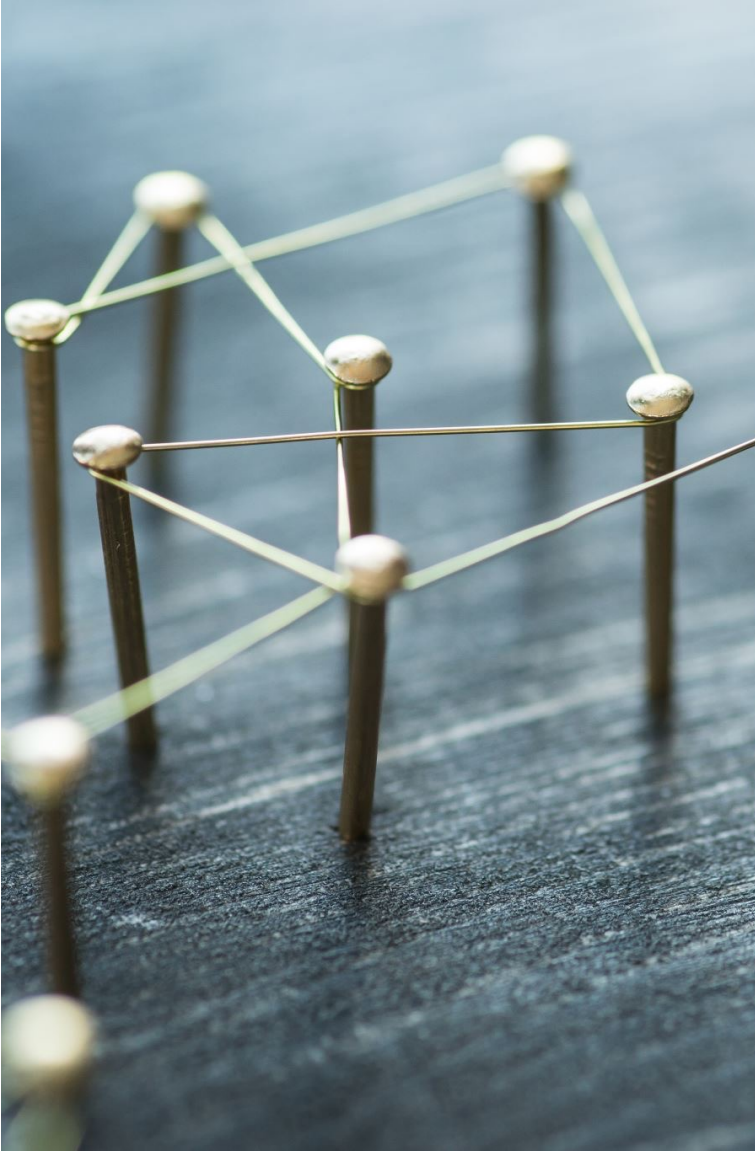
UNDERSTANDING THE IMMUNE RESPONSE IN TUBERCULOSIS
USING DIFFERENT MATHEMATICAL MODELS AND
BIOLOGICAL SCALES*

DAVID GAMMACK[†], SUMAN GANGULI[†], SIMEONE MARINO[†],
JOSE SEGOVIA-JUAREZ[†], AND DENISE E. KIRSCHNER[†]



How do we link scales and compartments?





Linking issues

- There are no standard linking methods
- Interfacing or linking independent model components that:
 - operate at different temporal or spatial granularities
 - use different modes of computation (e.g., stochastic and continuous)
- Passing parameters can link model scales
- Volumetric scaling can link compartmental transfers
- Several groups developed frameworks to modularize models to improve model linking with an eye toward efficient modeling.
 - CompuCell 3D (www.compuCell3d.org) (ask James G!)

How do
we
calibrate
MSMs?

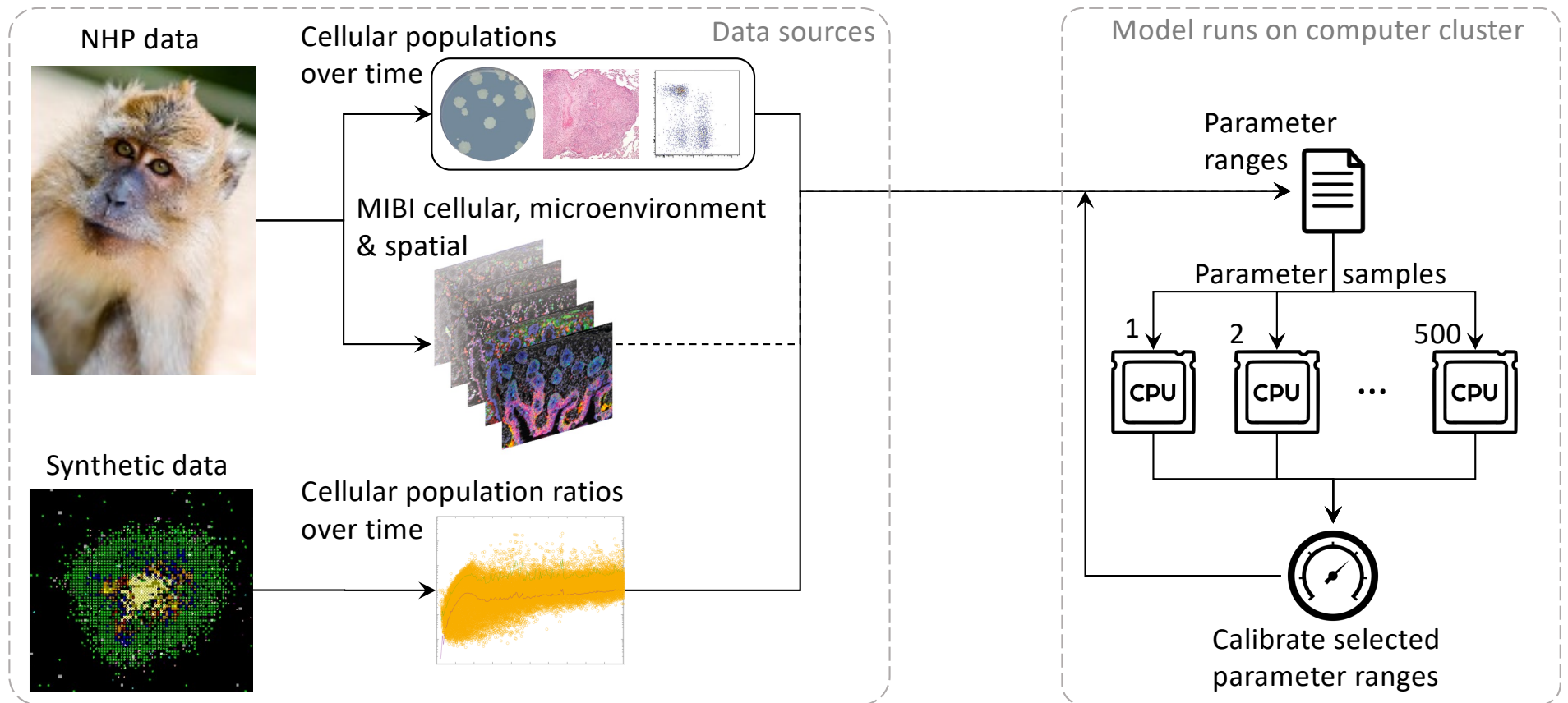


By eye with data fitting or other regression methods



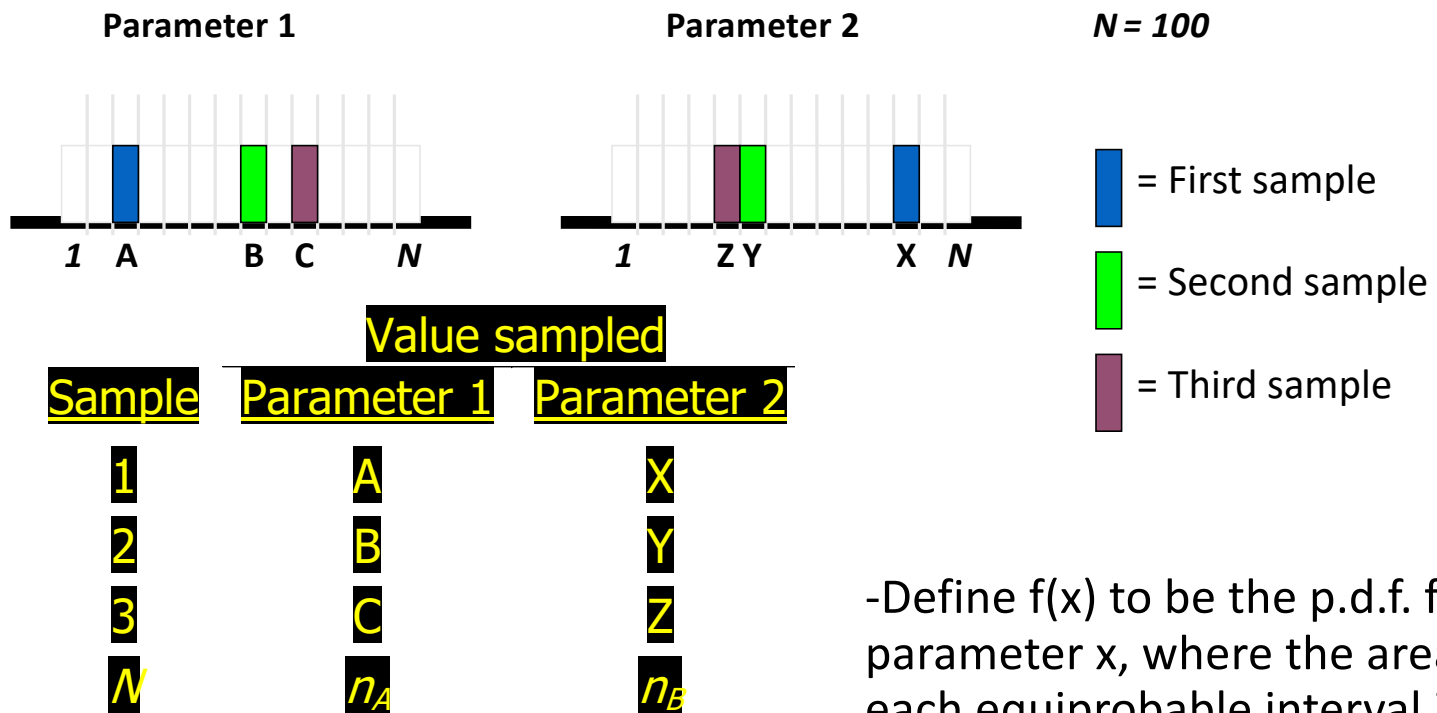
Multiple data types and space/time variations- need something else

calibration workflow to multiple types of data



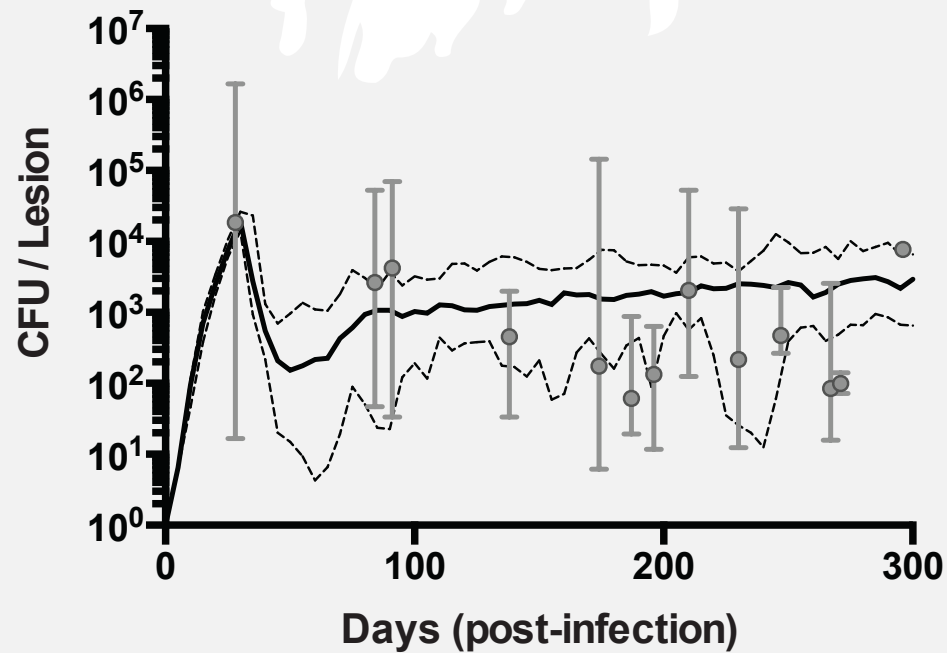
Latin hypercube sampling (LHS) for stratified searches

Recent paper on Sampling schemes (To Sobol or not to Sobol)

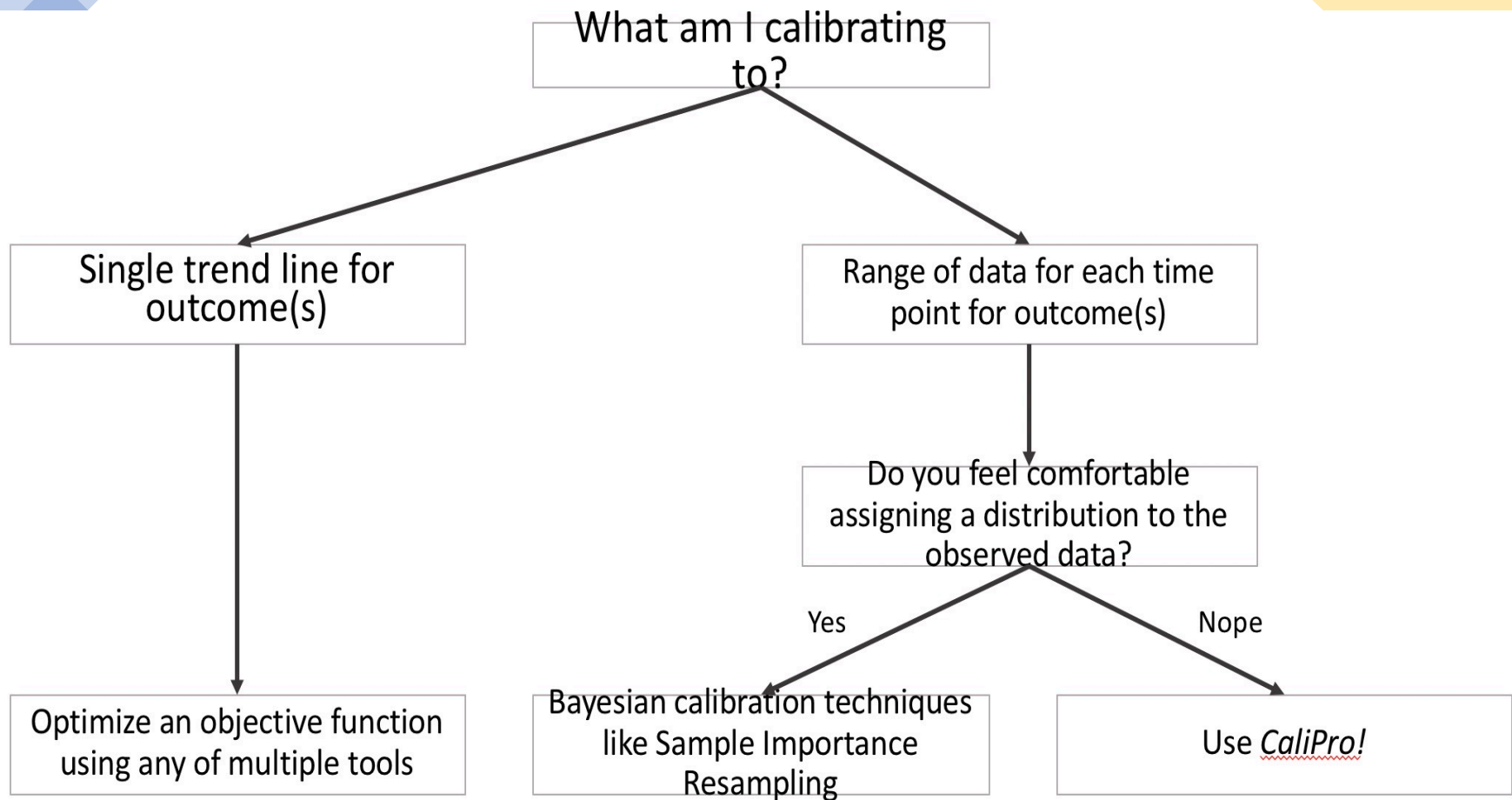


-Define $f(x)$ to be the p.d.f. for parameter x , where the area under each equiprobable interval is equal to $1/N$ (i.e. =integral of f).

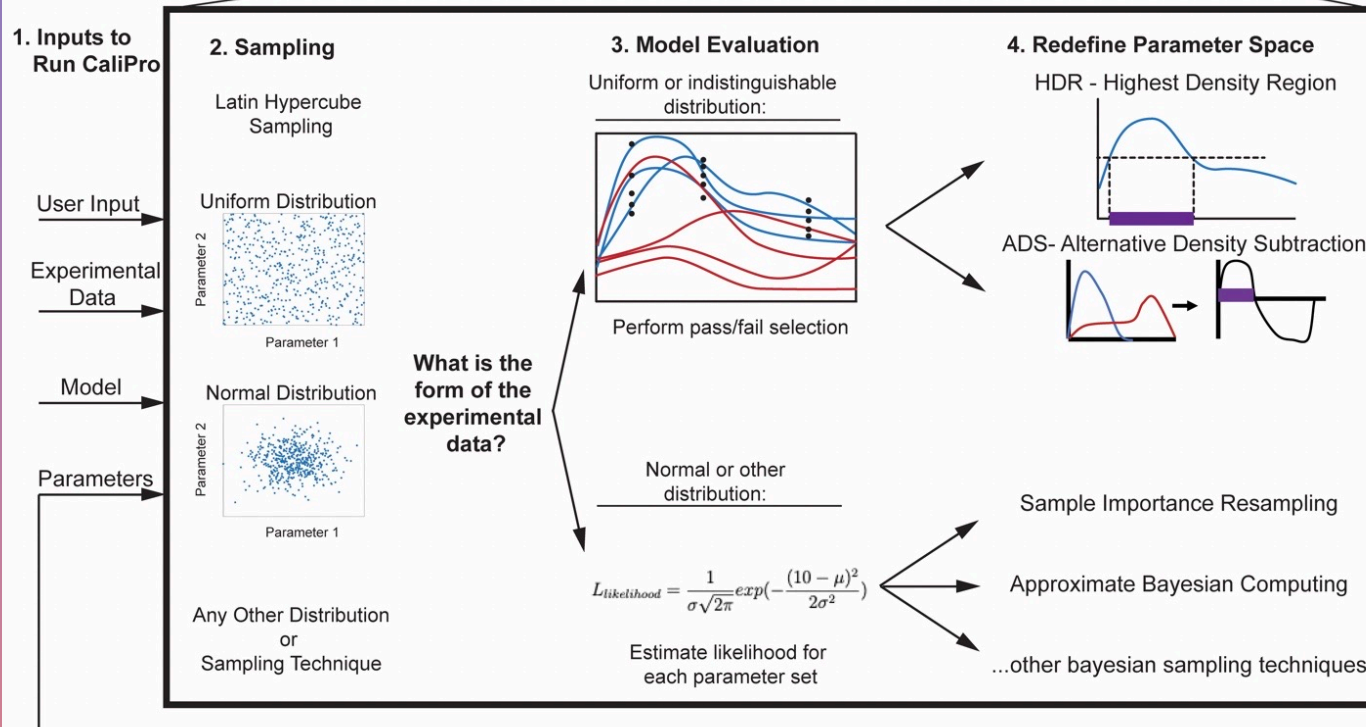
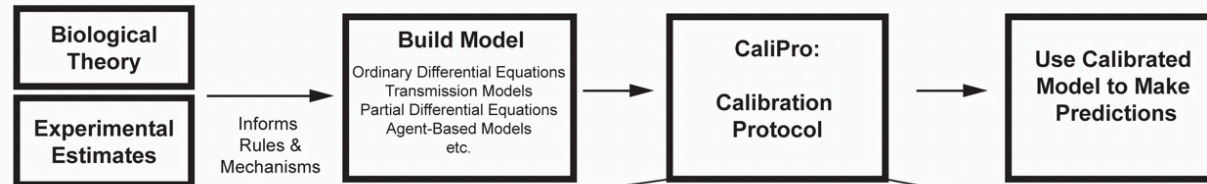
Model 'calibration': data versus model output



Model: curve, dashed lines (SEM)
NHP Data: Circles + SEM
(Data from Flynn Lab)

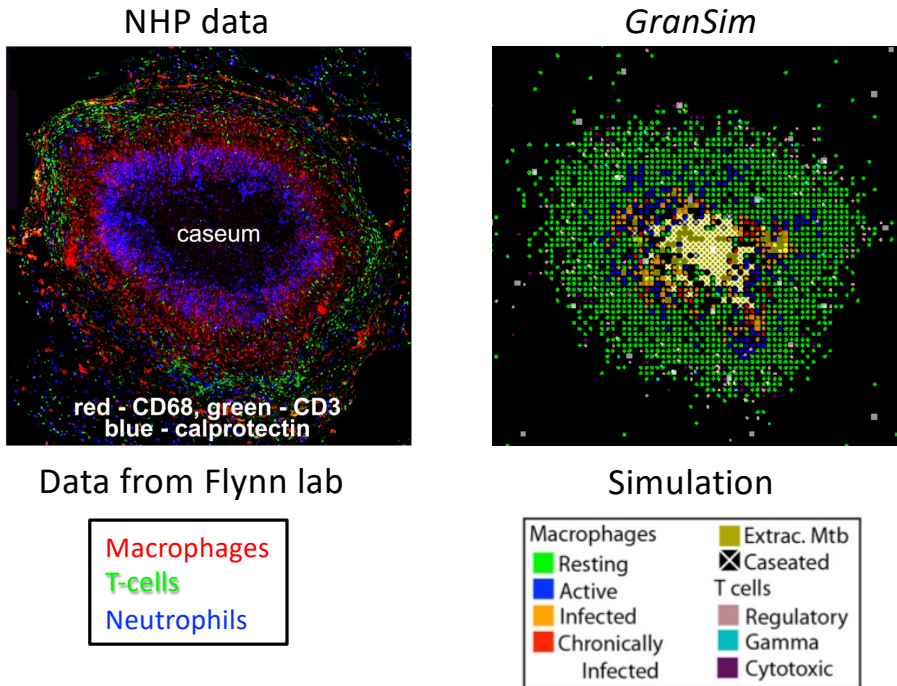


CaliPro: Calibration Protocol for complex models

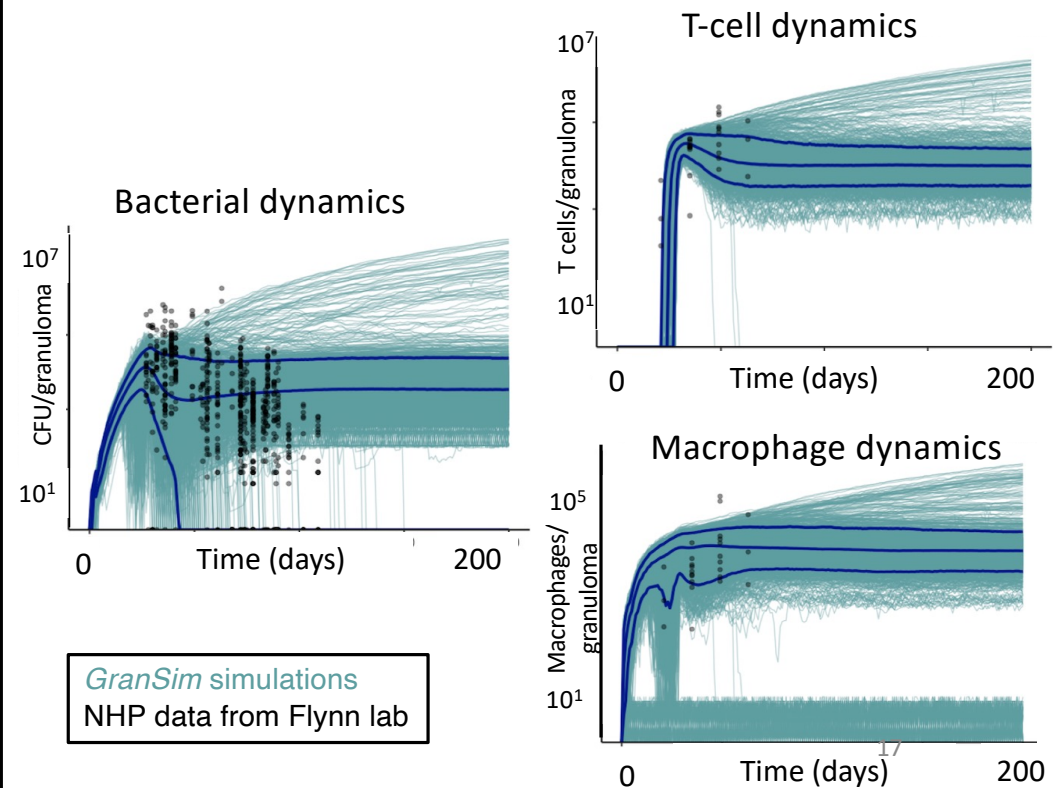


Simulations simultaneously match non-human primate data in both space and time

Spatial analysis



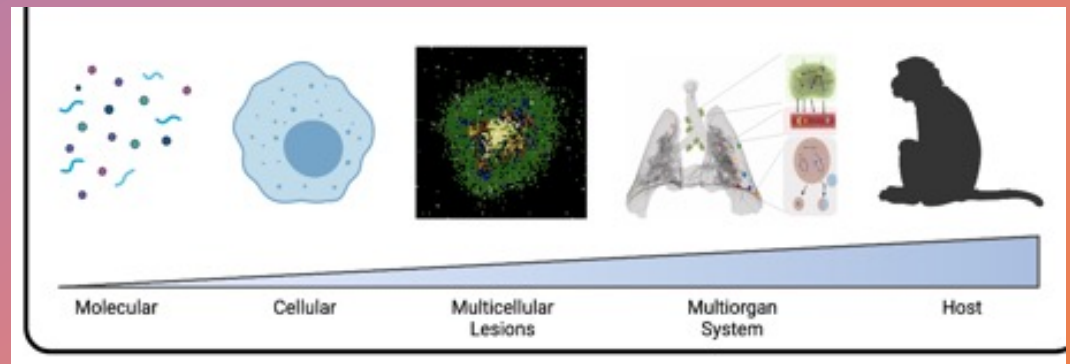
Temporal analysis



What about Bayesian approaches?

-See poster by Dr. Pariksheet Nanda here at MSM....

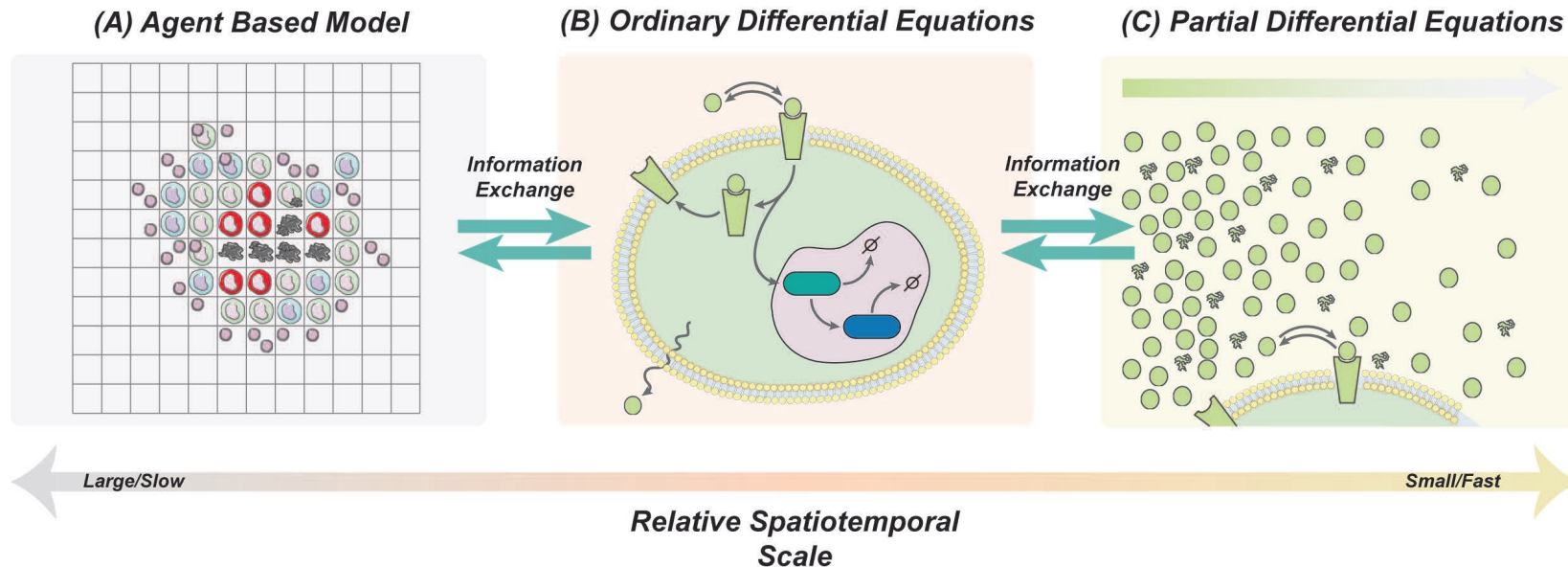
-Also he will show you our
Multi-scale Tissue Time
Machine



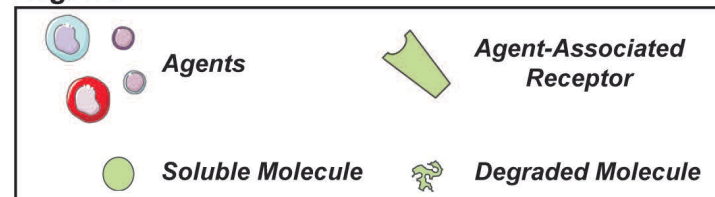


How do we simulate MSMs?

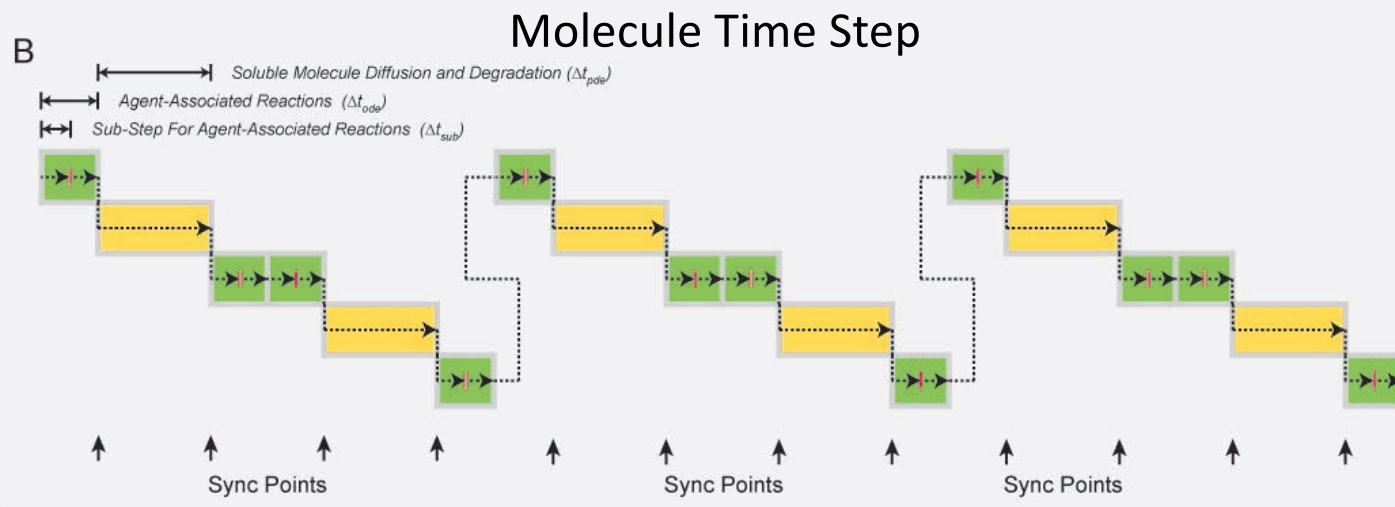
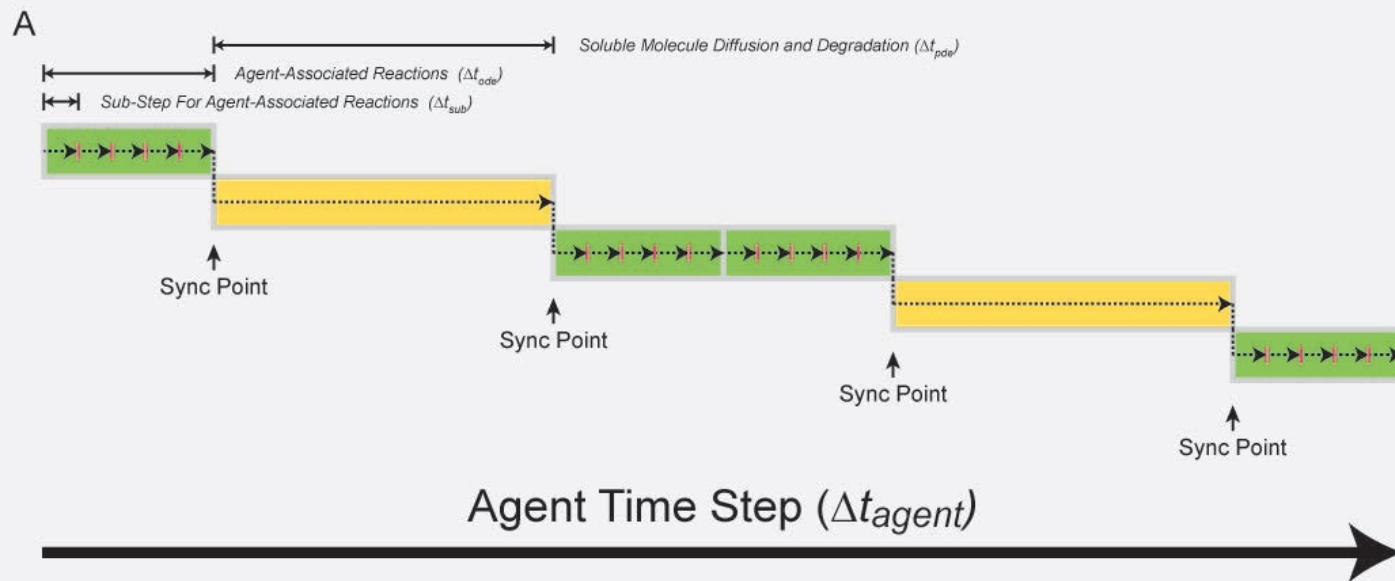
How do we simulate MSMs that are usually hybrid?



Legend



Cilfone, N, Kirschner, D and Linderman, JJ. Efficient numerical implementation of hybrid multi-scale agent-based models to describe biological systems *Cellular and Molecular Bioengineering*, 2014



Significant numerical challenges with hybrid MSMs

Significant numerical challenges with hybrid MSMs

- *linking*
- *speed*
- *numerical methods*

Diffusion methods for molecules

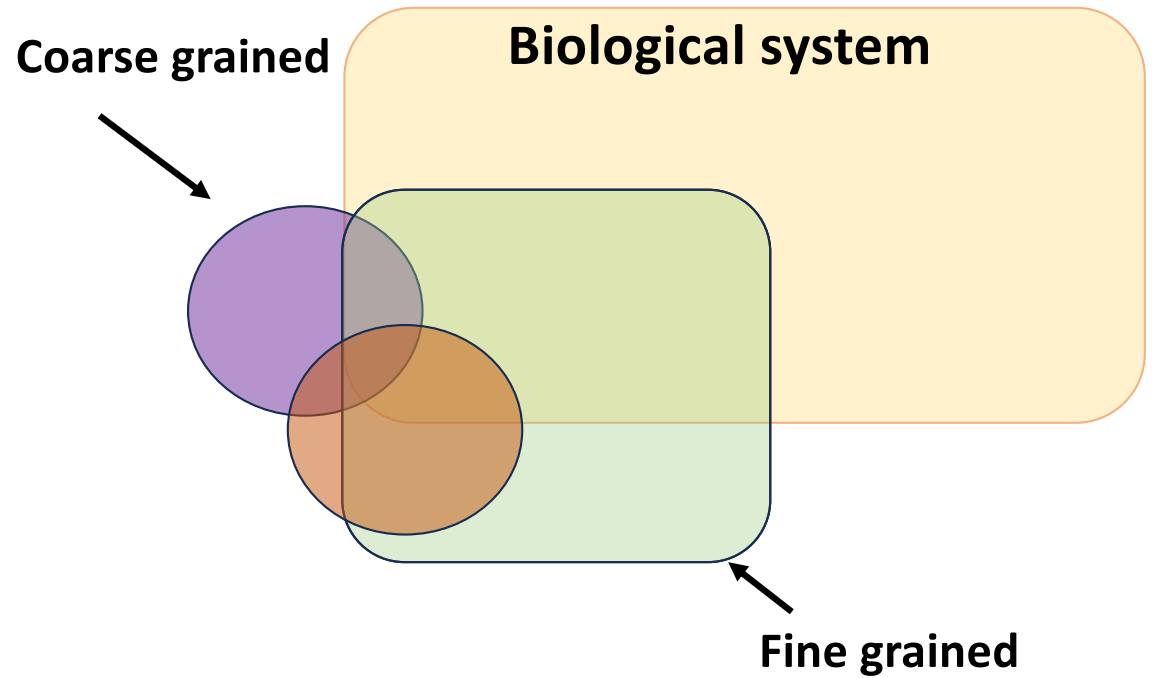
adi = alternating direction implicit, i.e. Crank-Nicholson
fft = fast fourier transform (explicit)
ade = alternating direction (explicit/implicit)

after 1 year we concluded the following:

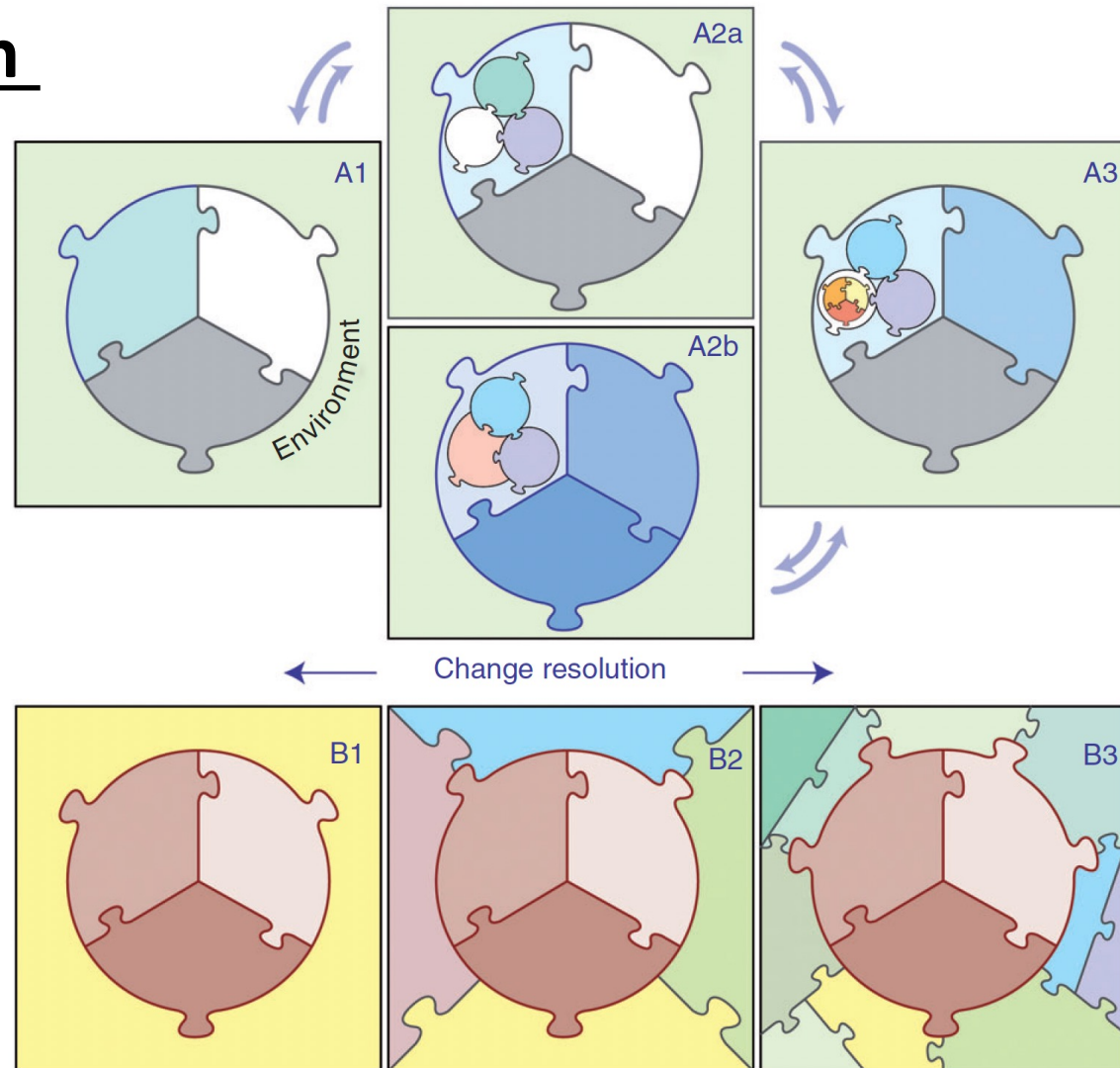
| Algorithm | dt (seconds) |
|-----------|--------------|
| adi | 30 |
| adi | 60 |
| adi | 120 |
| fft | 30 |
| fft | 60 |
| fft | 120 |
| fft | 200 |
| fft | 600 |
| ade | 30 |

CONCLUSION: ADI with a dt of 60 seconds.

Coarse-grain
versus
Fine-grain
Modeling
can help with
computation

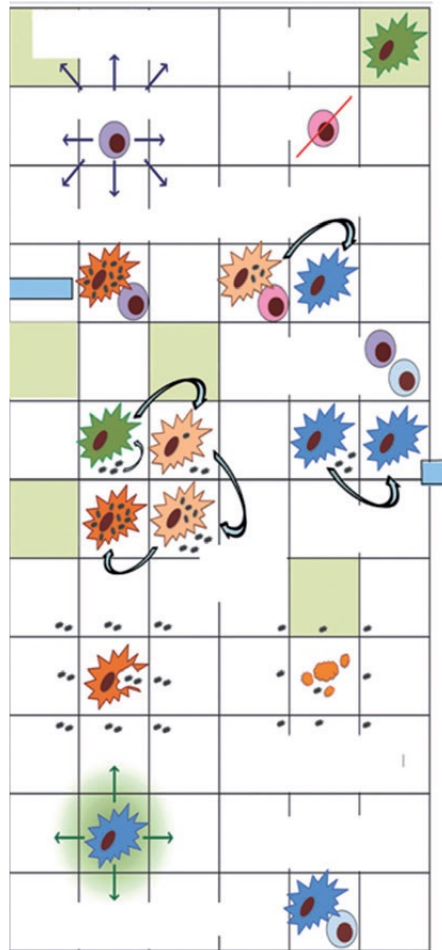


Tunable resolution



Kirschner et al, [Tunable resolution](#)
WIREs Syst Biol Med 2014, 6:289-309

Tunable resolution- how does it work?



Complex ABM

- grid
- agents
- rules
- timescales

How do we ensure MSMs are robust/credible?

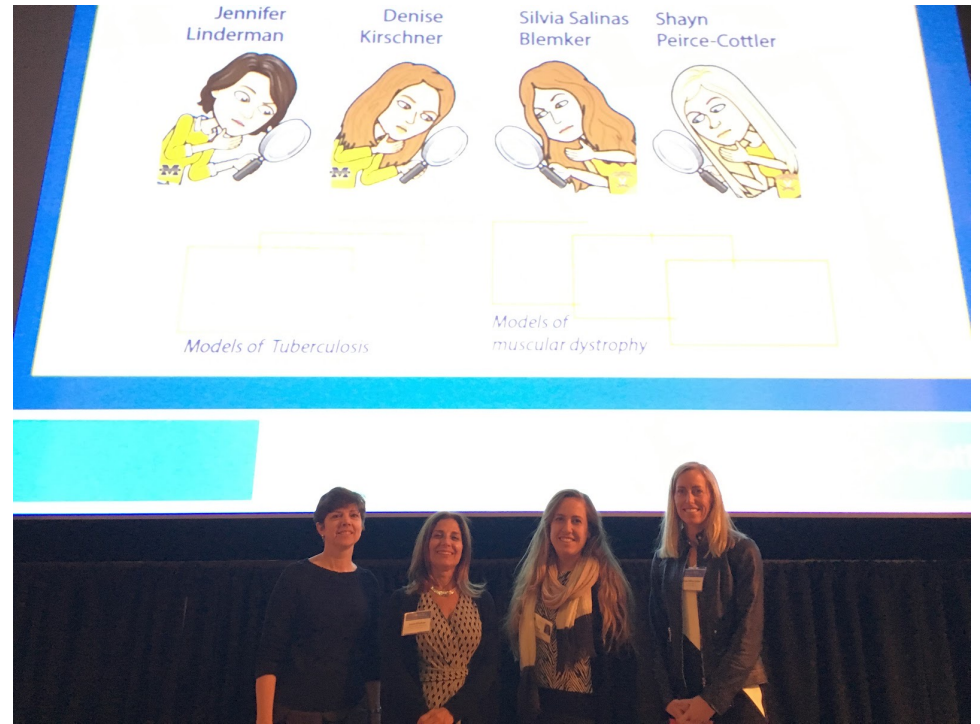
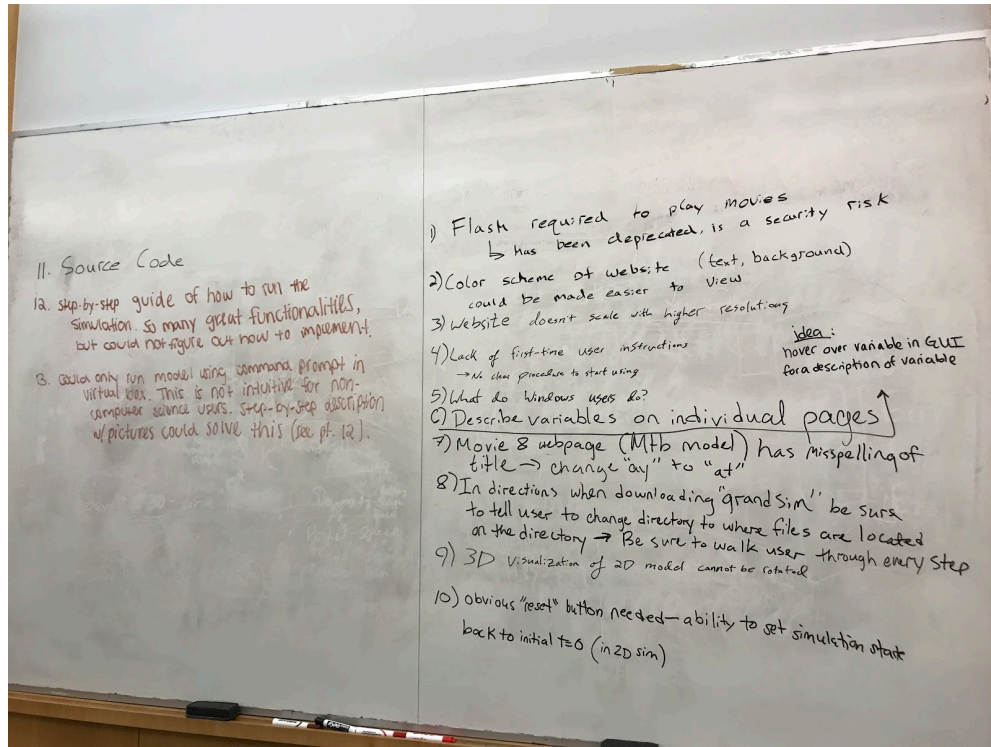


- See Session 1.2 today after the coffee break!

Ahmet Erdemir, Jerry Myer, Lealem Mulugeta, Herbert Sauro

- Created a team in Fall 2017 toward satisfying the 10 requirements of credibility:

-myself, Jennifer Linderman (UM)
w/ Shayne Peirce-Cottler and Silvia Blemker (UVA)



How do we analyze MSMs?

-
- Traditional equation-based analyses are not always available to us with hybrid MSMs

- Stability
- Bifurcation
- Correlations
- R_0
- Existence/uniqueness
- etc



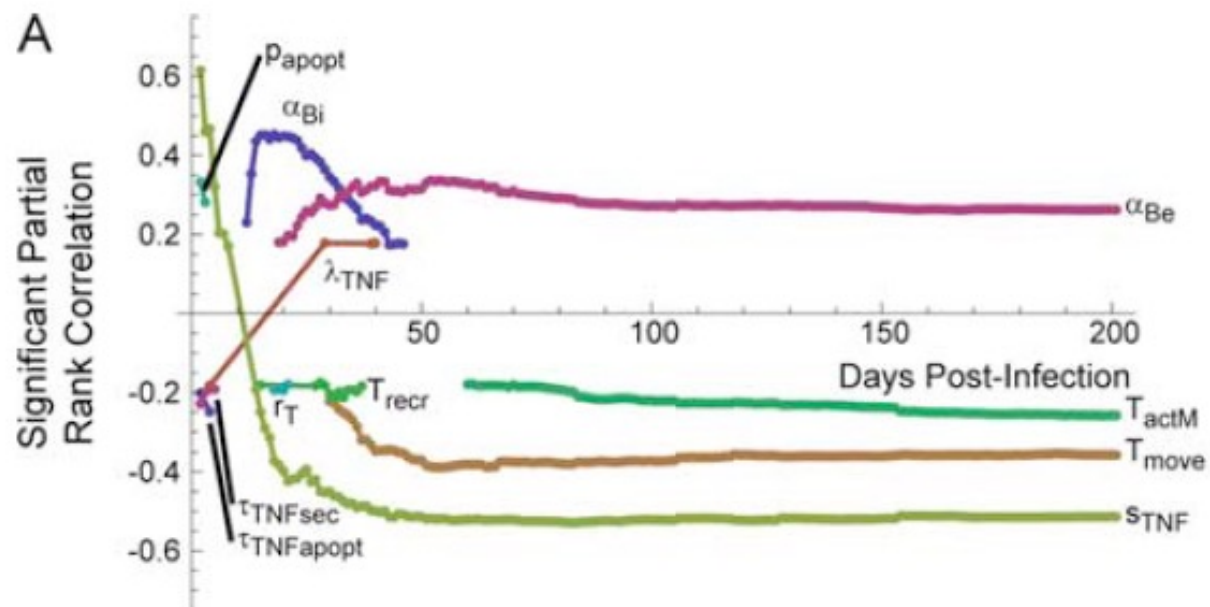
Key Analysis Tools

- **Uncertainty Analysis** - determines how much variability in outcome is induced by variability in parameter values
**Latin Hypercube Sampling (LHS) or Sobol*
- **Sensitivity Analysis**– measures which parameters induce this variability and ranks the correlations **Partial Rank Correlation (PRCC) and eFAST*
- **KEY FEATURE** - *can quantify relationships over time*
- *Simeone Marino, Ian B. Hogue, Christian J. Ray, Denise E. Kirschner. A Methodology For Performing Global Uncertainty and Sensitivity Analysis in Systems Biology Journal of Theoretical Biology, Vol 254, pp 178-196, 2008*

**programs available on our website in MATLAB and R*

Results of Sensitivity Analysis: Significant PRCCs

What factors distinguish different outcomes (CFU)?



How do we validate MSMs?



Part of credibility process



Ties to types of data available

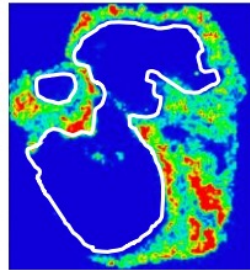
Ex: Validation to Pharmacokinetic data for a drug Bedaquiline

Spatial analysis

Granuloma
(white outline: caseum)



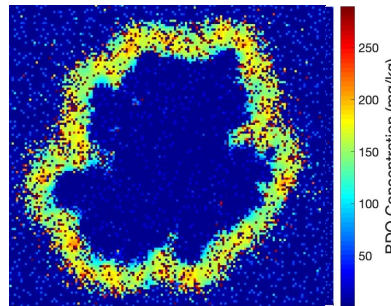
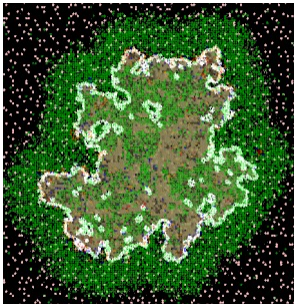
Drug distribution
within granuloma



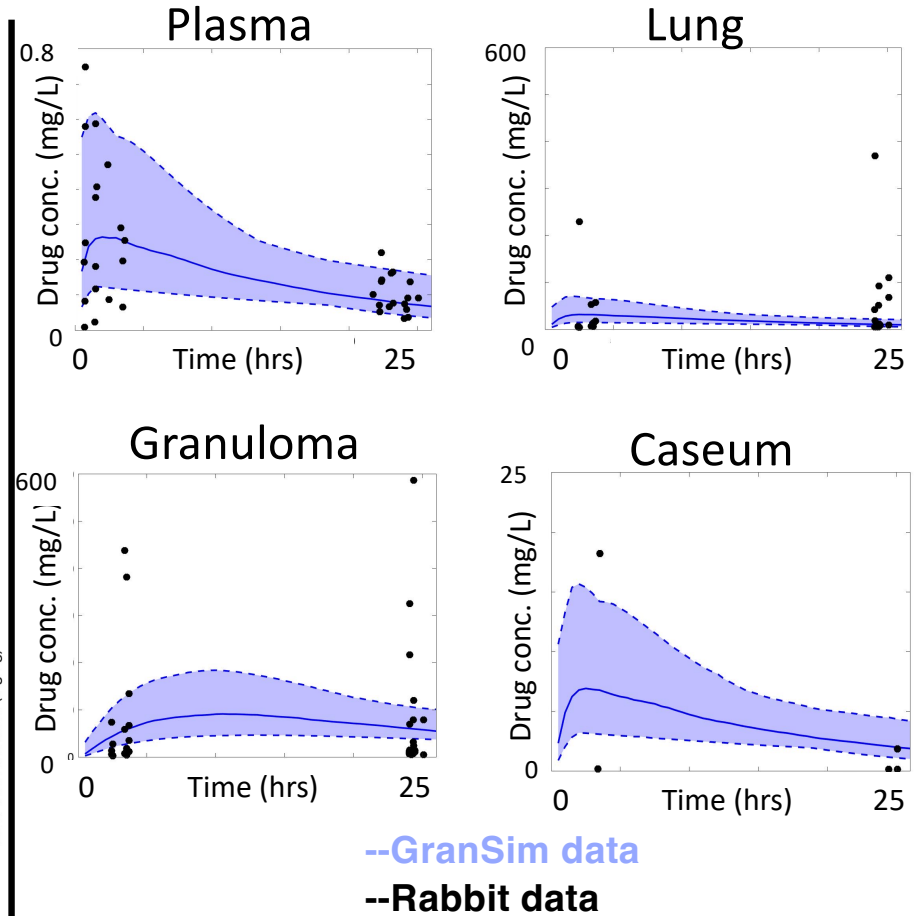
Human
data

Prideaux *et al.*
Nat. Med. (2015)

GranSim
data



Temporal analysis





2D vs. 3D issues in multi-scale modeling

- Most of biology is 3 dimensional
- Most people model in 2 dimensions
- HOW WRONG/OK IS THAT? In other words:
 - 1) When are we safe using a 2D model?
 - 2) We propose a methodology for scaling 2D model outputs to compare with 3D experimental datasets



Article

The Role of Dimensionality in Understanding Granuloma Formation

Simeone Marino^{1,2}, Caitlin Hult^{1,3} , Paul Wolberg^{1,3}, Jennifer J. Linderman³ and Denise E. Kirschner^{1,4,*} 

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Bulletin of Mathematical Biology
<https://doi.org/10.1007/s11538-019-00590-4>



METHODS AND SOFTWARE



Data Driven Model Validation Across Dimensions

Marissa Renardy¹ · Timothy Wessler^{1,2} · Silvia Blemker³ · Jennifer Linderman² · Shayn Peirce³ · Denise Kirschner¹ 

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How can MSMs be useful?

- ***Past and current applications from just our work-***

- Tuberculosis immune response in lungs
- Inner workings of the lymph nodes during health and infection
- Blood as a reflective compartment of lungs
- TB Drug regimens
- Vaccine efficacy
- Epidemiology of TB
- COVID-19 spin off
- Tumor modeling spin off
- Modeling tools for building and studying MSMs

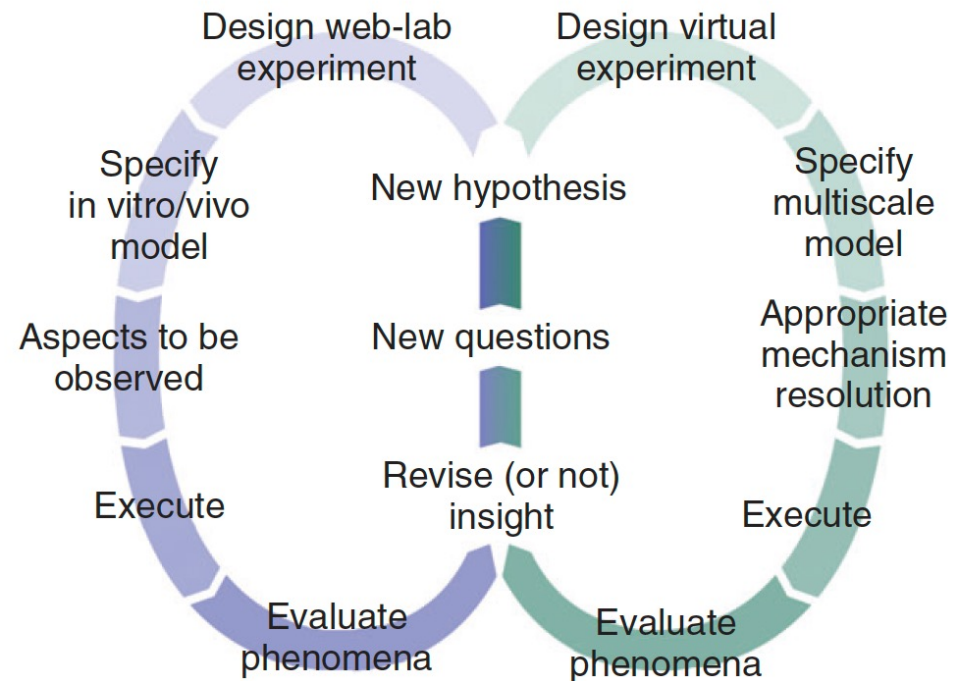
- ***Future applications of our work-***

- Creation of a Digital partner/twin
- Virtual City
- Other?

Yin and Yang of biological modeling

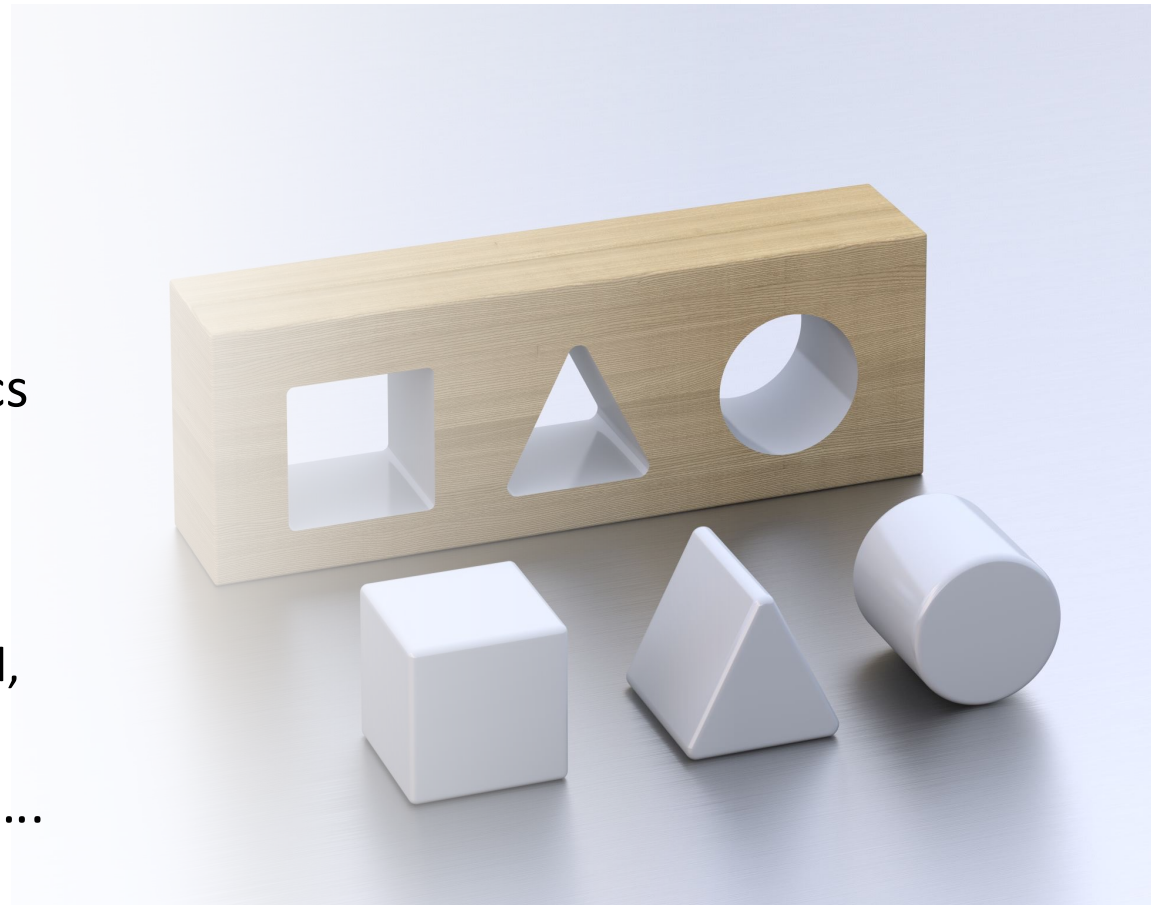
Coupled wet-lab and in silico studies for validation and prediction:

- Two cycles intersect to:
- *generate hypotheses*
- *pose new questions*
- *iteration is key!*



Where to go from here?? Now that we have tackled MSMs...

- Crosstalk with other projects to share ideas/models?
- Could be a big project consortium be next (e.g. digital twins) ?
- As a math person..are mathematics still interesting/needed?
- More advanced applications?
 - ..COVID-19, flu, HIV, TB, malaria, cancer, politics, climate, justice, food, antibiotic resistance, heart disease...
- Mechanistic modeling soap box.....
 - *Is AI/ML the next answer??.....*



Stop explaining black box machine learning models for high stakes decisions and use interpretable models instead

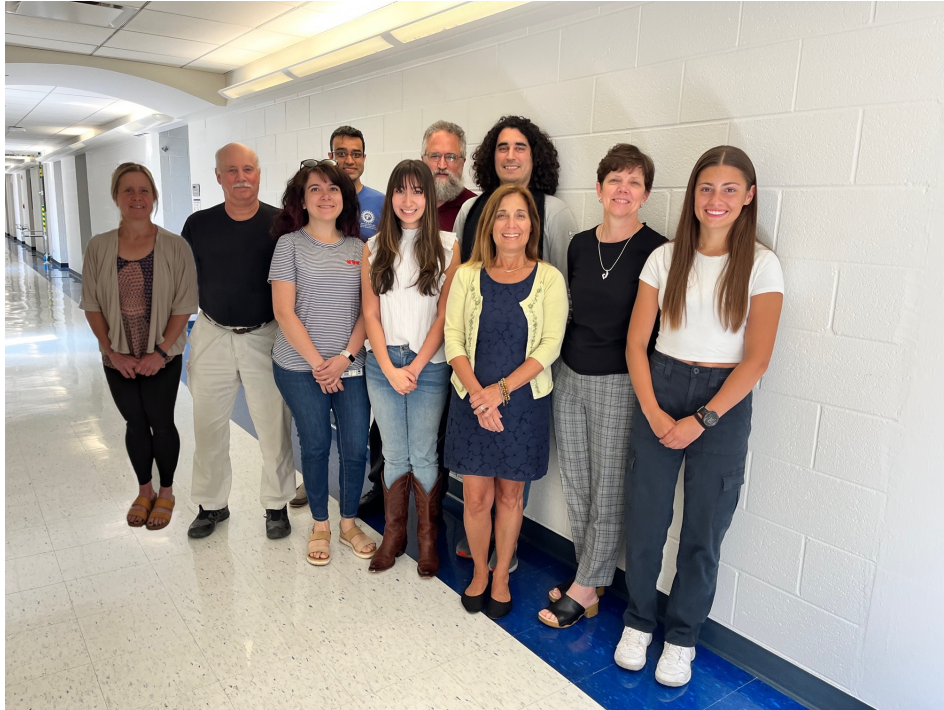
Cynthia Rudin 

Black box machine learning models are currently being used for high-stakes decision making throughout society, causing problems in healthcare, criminal justice and other domains. Some people hope that creating methods for explaining these black box models will alleviate some of the problems, but trying to explain black box models, rather than creating models that are interpretable in the first place, is likely to perpetuate bad practice and can potentially cause great harm to society. The way forward is to design models that are inherently interpretable. This Perspective clarifies the chasm between explaining black boxes and using inherently interpretable models, outlines several key reasons why explainable black boxes should be avoided in high-stakes decisions, identifies challenges to interpretable machine learning, and provides several example applications where interpretable models could potentially replace black box models in criminal justice, healthcare and computer vision.

Acknowledgements



• **Most of this MSM work done with co-PI
Dr. Jennifer Linderman**



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- Bree Aldridge (Tufts)
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- Khisi Mdluli (Gates)

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- Maral Budak, Pariksheet Nanda, Christian Michael
- Katy Krupinsky, Louis Joslyn, ETC..

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GATES foundation

