

## Rideout\_IndicatorDilution

This model simulates the human cardiovascular system. It simulates the following five scenarios:

- (1) Healthy Heart (with recirculation)
- (2) Ventricular Septal Defect (VSD)
- (3) Atrial Septal Defect (ASD)
- (4) Patent Ductus Arteriosus (PDA)
- (5) Open Loop (no recirculation)

The model is made of 10 compartments which combine perfect mixing and delay compartments. The anatomy represented by each compartment, as well as its volume and time constant are shown in the table above. This is a simple model which ignores capillary diffusion. An indicator bolus is injected into the pulmonary artery (compartment 1) and recirculates through the compartments in modes 1 through 4. However, mode 5, which is non-physiological, includes clearance through the right ventricle (compartment 0) and no recirculation.

For closed loop modes, by conservation of mass, the total amount of indicator in all compartments is fixed. Initially we expect to see the concentration peak in each compartment with the accumulated delays as shown in the table. The Transport Time around the loop is 40 sec. We therefore expect all compartments to show a peak-to-peak delay of ~40 sec (as long as the second peak can be distinguished). Eventually, the indicator concentrations will flatten into a unified concentration in all compartments.

In a healthy heart (mode 1) there are no internal loops. Blood flows from compartment to compartment in series. Figure 1 shows indicator concentrations in a healthy heart as computed by the JSim model. Note, for example, the indicator concentration at the small arteries (compartment 5). It peaks at ~15 sec, and again at ~52 sec. The peak-to-peak of ~37 sec is close to 40 sec as we expect. Also note that all concentrations flatten at ~0.00006 mM, the amount of injected indicator (0.25 umol) divided by total volume (4000 ml).

In a diseased heart (modes 2 through 4), there is an additional inner loop which flows in parallel to the outer loop and disrupts normal function. One or more of the conditions VSD, ASD or PDA can exist, although in this model we study the effect of each separately.

Two septal defects are studied in this model. Ventricular Septal Defect (mode 2), includes a shunt flow,  $F_{shunt}$ , from the left ventricle (compartment 3) to the right ventricle (compartment 0). Atrial Septal Defect (mode 3), includes a shunt flow,  $F_{shunt}$ , from the left atrium (compartment 2) to the right atrium (compartment 7). Figure 2 shows indicator concentrations in a heart with VSD as computed by the JSim model. Note the early peak in C0 due the shunt. In general, the effect of VSD or ASD is to generate lower peaks that occur later in time as the VSD or ASD aperture increases.

Rideout uses the pulmonary flow as a constant reference ( $F = 100$  ml/s by default). This poses a design limitation with VSD or ASD (modes 2 and 3). In both cases  $F_s = F - F_{shunt}$  and therefore  $F_{shunt}$  cannot exceed  $F$ . The code includes a protection mechanism which limits  $F_{shunt}$  to 99% of  $F$  in order to prevent near-zero or negative systemic flow.

Patent Ductus Arteriosus (mode 4), includes a shunt flow,  $F_{shunt}$ , from the aorta (compartment 4) to the pulmonary artery (compartment 1). In this mode the reference flow is the systemic flow, and there is no risk of negative flow. The pulmonary flow is  $F = F_s + F_{shunt}$ .

Open loop (mode 5) is a non-physiological form of the cardiovascular system in which the effects of recirculation are subtracted off in some way. The injected indicator will eventually be cleared from the system through compartment 0.

Open loop is useful for studying the cardiac output and system volume. By conservation of mass, the same amount of indicator will go through each compartment. The total area under the indicator injection pulse, as well as the area under each concentration curve (time integral at infinity) is a constant. Since the default amount of injected indicator is 0.25  $\mu\text{mol}$  and average flow is 100 ml/s, area default is 0.0025  $\text{mM}\cdot\text{s}$ . In open loop, we also compute Transport Functions,  $H_n(t)$ , which represent the fraction of solute arriving at the output of compartment  $n$  per unit of time. Finally, we compute Average Transit Times,  $T_{An}(t)$ , from compartment 1 to any compartment  $n$ . This is the first moment of the corresponding Transport Function  $H_n(t)$ . Multiplying the final value of the Average Transit Time by the flow  $F_0$  yields the aggregate volume of blood of the compartments 1 through  $n$ .

## Rideout\_IndicatorDilution\_Modified

This model simulates the human cardiovascular loop. It can simulate a healthy or diseased heart. Both Ventricular Septal Defect (VSD) and Atrial Septal Defect (ASD) are modeled. To simulate a healthy heart, set both shunt flows  $F_{vsd}$  and  $F_{asd}$  to zero. To investigate a diseased heart set either or both to a positive flow.

Unlike Rideout's original model (Rideout\_IndicatorDilution), this model keeps the systemic flow ( $F_s$ ) as constant reference. This is more analogous to real life and is needed to keep us alive. When the systemic flow  $F_s$  is held constant, intracardiac flows must rise when there is a shunt, and observations of pulmonary hypertension and heart failure are easy to understand.

The model is made of 10 compartments which combine perfect mixing and delay compartments. The anatomy represented by each compartment, as well as its volume and time constant are shown in the table above. This is a simple model which ignores capillary diffusion. An indicator bolus is injected into the pulmonary artery (compartment 1) and recirculates through the compartments. By conservation of mass, the total amount of indicator in all compartments is fixed. In a healthy heart there are no internal loops. Blood flows from compartment to compartment in series. We expect to see the concentration peak in each compartment with the accumulated delays as shown in the table. The Transport Time around the loop is 40 sec. We expect all compartments to show a peak-to-peak delay of ~40 sec (as long as the second peak can be distinguished). Indicator concentrations eventually flatten into a unified concentration in all compartments.

In a diseased heart, there is an additional inner loop which flows in parallel to the outer loop and disrupts normal function. Ventricular Septal Defect (VSD) includes a shunt from the left ventricle (compartment 3) to the right ventricle (compartment 0). Atrial Septal Defect (ASD) includes a shunt from the left atrium (compartment 2) to the right atrium (compartment 7). Figure 1 shows indicator dilution  $C_0$  when the VSD shunt aperture is swept from 0 to 60 ml/s, which is 60% of the default systemic reference flow (100 ml/s). Note that in VSD, an early peak in the right ventricle is visible and increases in amplitude as the shunt aperture is increased. ASD creates a similar effect, where indicator dilution  $C_7$  shows an early peak.

## Rideout\_PressureFlowLH

This model simulates the left heart using Pressure-Flow-Volume (or Pressure-Flow for short) modeling. This technique takes advantage of the analogy to RC or RLC circuits as shown here:

Pressure-Flow-Volume	Electrical Circuit Equivalent
-----	-----
F Flow (ml/s)	I Current (Amper)
P Pressure (mmHg or g/cm/s^2)	V Voltage (Volt)
Q Volume (ml)	Q Charge (Coulomb or Amper*s)
R Resistance (g/cm^4/s)	R Resistance (Ohm or Volt/Amper)
C Compliance (cm^4*s^2/g)	C Capacitance (Farad or s/Ohm)
L Inertance (g/cm^4)	L Inductance (Henry or s*Ohm)

Pressure-Flow components obey the same fundamental equations as their RLC circuit equivalents, i.e.:

$P = R * F$	$V = R * I$	(Eq. 1 or Ohm's Law)
$P = L * F:t$	$V = L * I:t$	(Eq. 2)
$P = Q / C$	$V = Q / C$	(Eq. 3)
$F = Q:t$	$I = Q:t$	(Eq. 4)

Blood flows from the left atrium to the left ventricle via the mitral valve and continues to the aorta via the aortic valve. The load consists of systemic and capillary arteries. Atrial pressure (PAT) is assumed fixed at 6 mmHg as is the central venous pressure (PSV) at 3 mmHg. These are equivalent to input and output electric potentials (voltages) which drive the flow (current) through the left heart. Mitral and aortic valves are modeled by limiting the flow to be positive and less than an upper bound.

There are three separate modes implemented in this model, corresponding to Rideout's ACSL programs:

- (1) LH-PF-1: Rectangular Actuator
- (2) LH-PF-2: Clipped Half-Sine
- (3) LH-PF-3: Skewed Half-Sine and Inertance

LH-PF-1 and LH-PF-2 use a basic RC circuit; LH-PF-3 uses an RLC circuit with additional components. The actuating signal for all modes is a variable periodic left ventricular stiffness SLV ( $SLV = 1/CLV$ ) which simulates a contracting and expanding left ventricle during the cardiac cycle. LH-PF-1 uses a rectangular SLV stiffness SLV waveform. LH-PF-2 uses a clipped half-sine. LH-PF-3 uses a clipped half-sine with a second harmonic term which adds some skew to the waveform.

The figures show some results when running the JSim model in LH-PF-3. Figure 1 is the ventricular stiffness, SLV. Stiffness changes between a maximum, SLS during systole which lasts 0.3 sec, and a minimum, SLD during diastole which last 0.5 sec. The pulse is periodic with a period of 0.8 sec (corresponding to 75 beats/min heart pulse). Four heart beats are simulated for a total run time of 3.2 sec. The left ventricle volume, QLV expands during diastole and contracts during systole.

Figure 2 shows the locus (path) of the left ventricular pressure, PLV, plotted versus volume, QLV. Values in this model were chosen so that the end-diastolic volume (EDV) is 120 ml and the end-systolic volume (ESV) is 48 ml. These volumes can be derived from Equation 3,  $P = Q / C$ , or  $Q = P / S$  and are typical in a healthy human adult. The ejection fraction  $(EDV - ESV) / EDV$  is 60% and stroke volume  $EDV - ESV$  is 72 ml. At a heart pulse of 0.8 sec, this corresponds to a cardiac output of 90 ml/sec (5.4 liter/min). The locus is traversed in counterclockwise direction. Note that it lies between the lines whose slopes are the diastolic (minimum) muscle stiffness SLD and the systolic (maximum) stiffness, SLS.

Figure 3 shows various flows in the model. Note that FAT, the atrial flow rises then decays exponentially at diastole. This represents the

diastolic inflow, which occurs when the walls of the left ventricle are relaxed and flow can pass through the mitral valve. As this chamber fills and expands, FAT decays. FLV, FAO and FSA have reverse activity, peaking and decaying during systole. FLV is the ventricular outflow and is limited by the aortic valve. FCA, capillary arteries flow, represents the systemic load and is much smaller and less pulsatile.

Figure 4 shows various pressures in the model. PLV, the ventricular pressure increases during systole, closing the mitral valve, and with further increase opens the aortic valve. Aortic pressure PAO follows ventricular pressure PLV during systole, while load pressure PCA is much more rounded. During diastole, PAO and PCA nearly coincide. The slow exponential decay has a time constant  $TCA = RCA * CCA$  of 2.53 sec. Note that some oscillations are visible in PAO starting at the end of systole.

## Rideout\_PressureFlow0

This model simulates the complete CV loop using Pressure-Flow modeling. The model is uncontrolled, i.e. does not include baroreceptor sensor connections to the central nervous system (CNS). Also, it does not consider blood diffusion from and to tissue. The model takes advantage of the analogy to RLC circuits as shown below:

Pressure-Flow-Volume	Electrical Circuit Equivalent
-----	-----
F Flow (ml/s)	I Current (Amper)
P Pressure (mmHg or g/cm/s <sup>2</sup> )	V Voltage (Volt)
Q Volume (ml)	Q Charge (Coulomb or Amper*s)
R Resistance (g/cm <sup>4</sup> /s)	R Resistance (Ohm or Volt/Amper)
C Compliance (cm <sup>4</sup> *s <sup>2</sup> /g)	C Capacitance (Farad or s/Ohm)
L Inertance (g/cm <sup>4</sup> )	L Inductance (Henry or s*Ohm)

Pressure-Flow components obey the same fundamental equations as their RLC circuit equivalents, i.e.:

$P = R * F$	$V = R * I$	(Eq. 1 or Ohm's Law)
$P = L * F:t$	$V = L * I:t$	(Eq. 2)
$P = Q / C$	$V = Q / C$	(Eq. 3)
$F = Q:t$	$I = Q:t$	(Eq. 4)

The right and left heart pathways are modeled with an RLC circuit similar to that used in Rideout's left heart model LH-PF-2 mode, ported to JSim in model Rideout\_PressureFlowLH. Alternatively, this model may be described as a compartmental representation of mass-transport, where each of the 12 compliances in the RLC circuit, corresponds to a perfect mixing chamber.

Circuit segment 0 corresponds to the right ventricle. Segments 1, 2 and 3 represent the pulmonary circulation. Segment 4 corresponds to the left ventricle. Oxygenated blood leaves the left ventricle and flows through ascending aorta (segment 5) and descending aorta (segment 6). There are two major arterial systemic paths: segment 7, which represent the abdominal aorta and segment 11, which represents the upper body arteries (fed through the common carotid). The abdominal aorta bifurcates into the common iliac arteries which feed internal organs and leg arteries (segment 8). The systemic venous system returns deoxygenated blood from the legs (segment 9), upper body (segment 12) and internal organs (segment 13). These veins drain into the vena cava (segment 10) and empty into the right atrium.

Unlike Rideout\_PressureFlowLH, this model has no fixed potentials (pressures). Both the left and right ventricles have time-varying compliance or stiffness ( $S = 1 / C$ ). The actuating signals are periodic half-sines S0 and S4 for the right and left ventricles stiffness respectively. Systole and diastole durations are both 0.4 sec, so that heart pulse is 0.8 sec (corresponding to 75 beats/min heart pulse). Peak systolic stiffness is chosen such that it is approximately four times larger in the left heart than in the right heart. Valves are simulated using flow limiters.

This model may be used to study the effect of Ventricular Septal Defect (VSD). This is done with an optional resistive shunt flow represented by  $R40 = 1 / GD$ , where GD is the VSD conductance. When GD is zero, R40 is infinite and there is no VSD flow.

Initial conditions in this model were chosen based on the steady state at the end of diastole. Note that these values are slightly different than the ones used in Rideout's ACSL program.

Figure 1 shows the left and right ventricular volumes, Q4 and Q0. As seen, the stroke volume pumped out of each ventricle is approximately 90 ml. At a heart pulse of 0.8 sec, this corresponds to a cardiac output of 112 ml/sec (6.7 liter/min). End-systolic volume (ESV) and

end-diastolic volume (EDV) are similar in each ventricle, around 160 ml. This means that the ejection fraction  $(EDV - ESV) / EDV$  is 56%.

Figure 2 shows the right and left ventricular pressures, P0 and P4. As seen, peak pressure is about four times larger in the left ventricle.

Figure 3 shows the loci on the Pressure-Volume plane of the right and left ventricles. Each systole-diastole cycle corresponds to one full counterclockwise traversal of the loci.

Figure 4 shows the effect of introducing VSD flow. In this case, the area under the aortic flow and VSD shunt flow are approximately the same. Thus, about half of the left ventricle output is returned to the right ventricle through the defect.

## Rideout\_PressureFlow1

This model simulates the complete CV loop using Pressure-Flow modeling. The model is uncontrolled, i.e. does not include baroreceptor sensor connections to the central nervous system (CNS). Also, it does not consider blood diffusion from and to tissue. The model takes advantage of the analogy to RLC circuits as shown below:

Pressure-Flow-Volume	Electrical Circuit Equivalent
-----	-----
F Flow (ml/s)	I Current (Amper)
P Pressure (mmHg or g/cm/s^2)	V Voltage (Volt)
Q Volume (ml)	Q Charge (Coulomb or Amper*s)
R Resistance (g/cm^4/s)	R Resistance (Ohm or Volt/Amper)
C Compliance (cm^4*s^2/g)	C Capacitance (Farad or s/Ohm)
L Inertance (g/cm^4)	L Inductance (Henry or s*Ohm)

Pressure-Flow components obey the same fundamental equations as their RLC circuit equivalents, i.e.:

$P = R * F$	$V = R * I$	(Eq. 1 or Ohm's Law)
$P = L * F:t$	$V = L * I:t$	(Eq. 2)
$P = Q / C$	$V = Q / C$	(Eq. 3)
$F = Q:t$	$I = Q:t$	(Eq. 4)

The venous segments of this model, both pulmonary and systemic, have a structure much like the RLC circuit used in the artery in Rideout's left heart model LH-PF-2, ported to JSim in model Rideout\_PressureFlowLH. The model has a single loop, but arteriovenous pathways may be easily added.

compliances are regarded as linear, but with unstressed volume (with zero pressure). This is different than Rideout's CV loop model PF-0, ported to JSim in model Rideout\_PressureFlow0, which assumed no unstressed volumes. In this model the initial condition in Eq. 4 above,  $Q(0)$ , consists of a stressed and unstressed components:

$$Q(0) = Q_U(0) + Q_S(0)$$

where  $Q_U = Q_U(0)$  is fixed. The pressure in Eq. 3 above, is obtained from the stressed portion:

$$P = Q_S / C = (Q - Q_U) / C$$

Left and right ventricle stiffnesses SLV and SRV ( $S = 1 / C$ ) in this model use a periodic half-sine with a second harmonic added to shape the actuator more realistically. Systole lasts 0.3 sec and diastole 0.5 sec, such that the heart pulse is 0.8 sec (corresponding to 75 beats/min heart pulse). Valves are simulated using flow limiters.

This model may be used to study the effect of myocardial infarction of one or both ventricles introduced at a chosen time. It also allows study of the effect of infusing or removing blood (bleeding) at the aorta at a chosen time. These conditions are modeled with a JSim choice variable.

Figure 1 shows the ventricular volumes, QLV and QRV. Stroke volume pumped out of each ventricle is 64 ml. At a heart pulse of 0.8 sec, this corresponds to a output of 80 ml/sec (4.8 liter/min), which is slightly low for an adult male.

Figure 2 shows the left ventricular locus on the Pressure-Volume plane. Each systole-diastole cycle corresponds to one full counterclockwise traversal of the loci. End-diastolic volume (EDV) is about 130 ml and end-systolic volume (ESV) is around 66 ml. This means that the ejection fraction  $(EDV - ESV) / EDV$  is about 50%.

Figure 3 shows the right ventricular and pulmonary artery pressures. Figure 4 shows the left ventricular and aortic pressures. Figure 5 shows the flow out of the first segments of the aorta (FA1) and left atrial



flow (mitral valve or left ventricular inflow). Oscillatory decay can be observed after the aortic valve close.

The rest of the figures show the effect of a myocardial infarction. At time 3.2 sec, systolic stiffness in both ventricles has been reduced by 25%, as seen in figures 6 and 7. Figure 8 shows the ventricular volumes. Stroke volume is suddenly decreased at infarction time. A slow recovery begins to occur as atrial average volumes and pressures increase. The right ventricle end-diastolic volume, in particular, is seen increasing and as stated by Starling's Law, stroke volume rises. This demonstrates that the CV system is stable to a certain extent, even without CNS control.

## Rideout\_PressureFlowReg

This Pressure-Flow model of the CV loop is regulated with baroreceptor feedback. It is similar to Rideout's uncontrolled CV loop model PF-1, ported to JSim in model Rideout\_PressureFlow1. Despite the uncontrolled nature of that model, the Frank-Starling mechanism ensures stability. More robust stability, however, requires regulation or feedback.

The present model simulates one of the body's important homeostatic mechanisms to maintain blood pressure. Known as baroreflex, it is a negative feedback loop with connections to the central nervous system (CNS). Pressure sensors called baroreceptors are located in the carotid (aortic) arch. Afferent nerves carry signals from these sensors to the CNS and efferent nerves carry signals back to the heart. There are two branches of efferent nerves with opposing effects: sympathetic which elevate blood pressure and parasympathetic which lower it.

Baroreceptor regulation can be described as follows:

- \* If blood pressure increases:
  - Baroreceptors activated
  - Parasympathetic nerves activated, sympathetic inactivated
  - Heart rate and strength of contraction decrease
  - Blood pressure drops (returns to normal)
- \* If blood pressure drops:
  - Baroreceptors inactivated
  - Parasympathetic nerves inactivated, sympathetic activated
  - Heart rate and strength of contraction increase
  - Blood pressure increases (returns to normal)

A JSim choice variable is used to switch between open-loop (without baroreceptor feedback) and closed-loop (with feedback). Left and right ventricle stiffnesses SLV and SRV ( $S = 1 / C$ ) in this model use a half-sine pulse with a second harmonic added to shape the actuator more realistically. With open-loop, these waveforms are periodic, with systole lasting  $TS = 0.3$  sec and diastole  $0.5$  sec, such that the heart period is  $TH = 0.8$  sec (corresponding to 75 beats/min). Peak amplitude is  $LS = 2500 \text{ g/cm}^4/\text{s}^2$  for the left ventricle and  $RS = 350 \text{ g/cm}^4/\text{s}^2$  for the right ventricle.

With closed-loop, a feedback signal  $Y$  is derived from PA3, corresponding approximately to carotid pressure. The following steps are taken:

- 1) Average PA3 using a low-pass filter. Filtered output, PA3F, tracks PA3, but changes less rapidly.
- 2) Calculate an error signal, DPA3F, as the difference between PA3F and a constant reference  $PREF = 72 \text{ mmHg}$ . Error signal may be positive or negative, according to whether the average carotid pressure is greater or less than  $PREF$ .
- 3) Scale the error signal with a constant gain  $KX = 0.2 \text{ 1/mmHg}$ . Scaled output, Z3, is dimensionless.
- 4) Apply an offset and limit the error Z3 to obtain the feedback signal  $Y$ . Offset is 1.0, lower limit is 0.1 and upper limit 1.9. Thus,  $Y$  is unity when there is no error and has a maximum allowed deviation of 0.9 about unity.

The goal of the feedback loop is to maintain the feedback signal  $Y$  as close as possible to unity.  $Y$  is used to control the systolic amplitudes  $LS$  and  $RS$ , heart period  $TH$  and systolic period  $TS$  using these equations:

$$LS = LSI / (0.5 + 0.5 Y) \quad (\text{Eq. 1})$$

$$RS = RSI / (0.5 + 0.5 Y) \quad (\text{Eq. 2})$$

$$TH = 0.2 + 0.6 Y \quad (\text{Eq. 3})$$

$$TS = 0.14 + 0.2 TH \quad (\text{Eq. 4})$$

With the feedback at unity, these values default to the open-loop values. An increase in  $Y$ , which might result from an increase in carotid pressure, will tend to increase heart period (decrease heart rate) and also decrease strengths of contraction of both ventricles. The result of

these changes will tend to return arterial pressures, and thus cardiac output, back to their original values.

This model may be used to study the effect of myocardial infarction of one or both ventricles introduced at a chosen time. The infarction is simulated by adding negative values DLS and DRS to the systolic ventricle stiffnesses LS and RS respectively at a chosen time. The model also allows study of arterial infusion or venous bleeding.

The figures examine open and closed loop behavior with total run time of 20 sec. A sudden myocardial infarction is introduced at time  $T_I = 11$  sec in the left ventricle. By setting  $DLS = 625$ , stiffness drops 25% from approximately  $2500 \text{ g/cm}^4/\text{s}^2$  to  $1875 \text{ g/cm}^4/\text{s}^2$ . Figures 1 and 2 are in open loop mode; the rest of the figures are closed loop.

Figure 1 shows ventricular volumes, QLV and QRV. Stroke volume from the left ventricle is decreased at infarction time from approx. 68 ml to 55 ml. A slow recovery begins to occur as average volumes and pressures increase. By Frank-Starling's Law, stroke volume rises and at  $t = 20$  sec it is approx. 63 ml.

Figure 2 demonstrates that without true feedback, some variables cannot return to their pre-infarction value. The carotid pressure, for example, drops from an approx. average of 72.5 to 70.5 mmHg.

Figures 3 and 4 show the feedback signal Y and heart period TH in closed loop. Both plots show a dip at 11 sec. Since the error signal DPA3F is negative, Y drops below unity. From feedback equations 3 and 4 above, heart period and systole period drop with Y (heart rate increases). Within approx. 4 sec, Y returns to near unity and TH returns to the open loop stable value of 0.8 sec. Thus the feedback loop was able to compensate for the infarction relatively rapidly.

Figures 5 and 6 show the left ventricle systolic stiffness LS and right ventricle systolic stiffness RS. From feedback equations 1 and 2 above, both increase when Y drops below unity. The increase in contraction strength contributes to the recovery. As Y returns to unity, LS and RS stabilize with means near  $1875 \text{ g/cm}^4/\text{s}^2$  and  $350 \text{ g/cm}^4/\text{s}^2$ .

Figure 7 shows ventricular volumes QLV and QRV. It is similar to the open-loop result of Figure 1, but recovery is faster.

Figure 8 shows the filtered carotid pressure in closed-loop. Unlike the corresponding open-loop result of Figure 2, PA3F returns near its value before infarction, centered at the reference point of  $PREF = 72 \text{ mmHg}$ .

## Rideout\_PressureFlowNP

Nonpulsatile models are useful for pharmacokinetic studies which typically have time constants in minutes. Ignoring nonlinearities, the ventricular pressure-volume locus is counterclockwise between two straight lines whose slopes are  $SD=1/CD$  and  $SS=1/CS$ .  $CD$  and  $CS$  are the diastolic and maximum systolic compliances of the myocardium. If we denote the end-diastolic pressure  $PED$  and end-systolic pressure  $PES$ , then the stroke volume for the ventricle is:

$$QSV = PED * CD - PES * CS$$

Multiplying by the heart rate  $H$ , gives the average outflow:

$$F = (CD * H) * PED - (CS * H) * PES$$

Assuming a direct relationship between average atrial ( $Pat$ ) pressure and  $PED$ , and between average arterial ( $Part$ ) pressure and  $PES$ , we get:

$$F = Gpre * Pat - Gafter * Part$$

Where  $Gpre$  and  $Gafter$  are the preload (prior to contraction) and afterload (during ejection) conductances, and are inversely proportional to the diastolic and systolic stiffness, respectively.

Denoting the left ventricle conductances  $G1$  and  $G2$ , and the right ventricle conductances  $G3$  and  $G4$ , the following equations describe the nonpulsatile ventricular flow:

$$\begin{aligned} FL &= G1 * PL - G2 * PS \\ FR &= G3 * PR - G4 * PP \quad (\text{Eqs. 1}) \end{aligned}$$

The pressure drops over the systemic and pulmonary peripheral resistances are given by Ohm's law:

$$\begin{aligned} PS - PR &= RS * FS \\ PP - PL &= RP * FP \quad (\text{Eqs. 2}) \end{aligned}$$

Assuming fixed compliances and unstressed volume (under zero pressure) for each of the four components:

$$\begin{aligned} PS &= (QS - QSU) / CS \\ PR &= (QR - QRU) / CR \\ PP &= (QP - QPU) / CP \\ PL &= (QL - QLU) / CL \quad (\text{Eqs. 3}) \end{aligned}$$

Finally, integrating the flow through each component give the volume.

$$\begin{aligned} QS:t &= FL - FS \\ QR:t &= FS - FR + FI \\ QP:t &= FR - FP \\ QL:t &= FP - FL \quad (\text{Eqs. 4}) \end{aligned}$$

Since this is a nonpulsatile model, the steady state is a unified constant flow through the loop. It is interesting to model a sudden change and the system response until a new steady state is obtained. Two such conditions are modeled with a JSim choice variable:

- (1) Infusion: Infusion flow pulse  $FI$  is added to systemic arteries
- (2) Left Ventricular Stiffness Change:  $G2$  is halved at time  $TCH$

In infusion mode, a flow pulse  $FI$  is added to the systemic arteries flow (second equation in Eqs. 4). The infusion pulse is rectangular, starting at time  $TSTT = 1$  sec and lasting  $WID = 2$  seconds. In this mode all conductances are fixed.

In Left Ventricular Stiffness Change mode, there is no infusion and total blood volume is constant. Left ventricular afterload conductance  $G2$  is halved (left systolic stiffness is doubled) at

TCH = 1 sec.

Figure 1 shows the flow pulse FI in infusion mode. Figure 2 shows an increase of 50 ml in total blood volume (integral of flow). Figure 3 shows the flows FR, FP, FL and FS in infusion mode. Figures 4 through 11 show the corresponding volumes and pressures.

Figure 12 shows the flows FR, FP, FL and FS in Left Ventricular Stiffness Change mode. Figures 13 through 16 show the corresponding pressures. The increase in systolic stiffness results in increased PS and QS (as evident from Eqs. 3). PR and QR also increase, but somewhat more slowly. As a result of these increases, the variables PP, QP, PL, and QL decrease (total blood volume must remain constant). All flows settle to the same increased value because of the stronger left heart.