

Electrical and Biochemical Properties of an Enzyme Model of the Sodium Pump

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Summary. The electrochemical properties of a widely accepted six-step reaction scheme for the Na^+, K^+ -ATPase have been studied by computer simulation. Rate coefficients were chosen to fit the nonvectorial biochemical data for the isolated enzyme and a current-voltage (I - V) relation consistent with physiological observations was obtained with voltage dependence restricted to one (but not both) of the two translocational steps. The vectorial properties resulting from these choices were consistent with physiological activation of the electrogenic sodium pump by intracellular and extracellular sodium (Na^+) and potassium (K^+) ions. The model exhibited K^+/K^+ exchange but little Na^+/Na^+ exchange unless the energy available from the splitting of adenosine triphosphate (ATP) was reduced, mimicking the behavior seen in squid giant axon. The vectorial ionic activation curves were voltage dependent, resulting in large shifts in apparent K_m 's with depolarization. At potentials more negative than the equilibrium or reversal potential transport was greatly diminished unless the free energy of ATP splitting was reduced. While the pump reversal potential is at least 100 mV hyperpolarized relative to the resting potential of most cells, the voltage-dependent distribution of intermediate forms of the enzyme allows the possibility of considerable slope conductance of the pump I - V relation in the physiological range of membrane potentials. Some of the vectorial properties of an electrogenic sodium pump appear to be inescapable consequences of the nonvectorial properties of the isolated enzyme. Future application of this approach should allow rigorous quantitative testing of interpretative ideas concerning the mechanism and stoichiometry of the sodium pump.

Key Words Na^+, K^+ -ATPase · sodium pump · electrogenic · computer simulation · enzyme kinetics · thermodynamics

Introduction

In tissues where a large fraction of time is spent generating action potentials, the net instantaneous active and passive ion fluxes during these action potentials must be comparable in magnitude (Chapman, Kootsey & Johnson, 1979). Although there have been some attempts to explore theoretically the physiological consequences of electrogenic Na^+/K^+ transport in such circumstances, the transport models that were used incorporated purely arbitrary functions to account for the experi-

mentally observed voltage and chemical dependency of the overall transport reaction. Linear dependence on one or more chemical components has been assumed either on the basis of experimental data of limited range (Attwell, Cohen & Eisner, 1979; Brown, Di Francesco, Noble & Noble, 1980; Jakobsson, 1980) or on the basis of the assumptions of irreversible thermodynamics (Rapoport, 1970; Chapman, 1980). Scriven (1981) made the ionic dependences nonlinear in accordance with experimental observation. Chapman et al. (1979) and Johnson, Chapman and Kootsey (1980) treated the pump as an 'elementary-complex' reaction (Keizer, 1975). They also included nonlinear ionic dependences, but constrained them thermodynamically and included the voltage dependence required by thermodynamics.

It is clear that electrogenic Na^+/K^+ transport plays an important role in the electrophysiology of muscle and nerve cells. If that role is to be properly understood, a more accurate description of the transport process is necessary – preferably, one based on a knowledge of the actual mechanism rather than empirical fits or unrealistic treatment as an 'elementary-complex' reaction. Biochemical knowledge of the details of the reaction mechanism underlying Na^+/K^+ transport is sufficiently far advanced to begin to treat the process more realistically as a multi-step enzyme reaction. Biochemical studies give information concerning the number and chemical nature of the individual steps in the transport reaction and the value or approximate magnitude of the rate constants governing these steps.

An enzyme that catalyzes an electrogenic vectorial reaction across a membrane differs from other enzymes in that the equilibrium constant of the overall process depends on the transmembrane potential as well as on the chemical constituents.

tants in the scheme of Fig. 1. It can be seen that Na_{in}^+ and K_{in}^+ compete for one form of the enzyme ($\text{E} \cdot \text{ATP}$), and Na_{out}^+ and K_{out}^+ compete for another form ($\text{E}' - \text{P}$). In each case, however, the consequences of the competition depend on whether Na^+ or K^+ succeeds in reacting with the enzyme. For example, if Na_{out}^+ reacts with $\text{E}' - \text{P}$, the reaction proceeds backwards through step 3 whereas if K_{out}^+ reacts then the reaction proceeds forwards through step 4. There is no possibility admitted in this scheme for the kind of competition where either Na_{out}^+ or K_{out}^+ can react backwards in step 3 or forwards in step 4. That is to say, for example, only K_{out}^+ can dephosphorylate the enzyme. Although no form of the enzyme can display simultaneous reactivity towards Na_{in}^+ and K_{out}^+ , or to Na_{out}^+ and K_{in}^+ , a kind of competition between intracellular and extracellular ions can occur because the total amount of enzyme available is limited. An extracellular ion present in large quantities can commandeer the enzyme in such a way as to reduce ("inhibit") the rates of other steps requiring reaction between intracellular ions and other forms of the enzyme. In this manner, it is theoretically possible for "competitive inhibitory" behavior to be exhibited by all of the reactants in the scheme of Fig. 1. The simulations will show that whether or not such behavior is manifest for any particular reactant depends upon the choice of rate coefficients for the individual steps and upon the free energy available from ATP splitting.

Voltage Dependence

Because the Na^+, K^+ -ATPase transport mechanism is electrogenic, one or more of the elementary steps in the overall reaction process must be voltage-dependent. In the absence of experimental evidence the number and location of the voltage-dependent steps must be decided arbitrarily. It seems reasonable to presume that the voltage dependence occurs at one or both of the translocational steps (i.e., steps 3 and 5) since it is there that movement of charge may occur. Three possibilities will be explored:

1. translocation of a trivalent intermediate at step 3 followed by return translocation of a divalent intermediate at step 5.
2. translocation of a univalent intermediate at step 3.
3. translocation of a univalent intermediate at step 5.

The first possibility is conceptually straightforward and involves the assumption that the 3 Na^+

ions and 2 K^+ ions undergo their respective translocations unbalanced by any neutralizing charges.

For the second possibility the 3 Na^+ ions could be translocated by symport with two negative ions, these being returned electroneutrally in association with K^+ ion translocation at step 5. Symport of anions might be achieved by translocation, across the voltage gradient, of negatively charged binding sites on the enzyme.

Similarly, the third possibility could arise from electroneutral translocation of 3 Na^+ ions at step 3 by symport with three balancing charges, these charges being returned in association with K^+ ion translocation at step 5, making step 5 equivalent to the extrusion of one unbalanced positive charge.

For reasons clarified in the results illustrated in Fig. 3 we are inclined to exclude the first as a realistic possibility. Of the remaining two we have chosen the translocation of a univalent charge at step 5. This choice relates to the history of our heuristic approach rather than to any requirement from experimental data.

In either case, the question arises as to the manner in which voltage influences the unidirectional rate coefficients of the elementary reaction step. The fundamental law governing charge transfer reactions is expressed through the Butler-Volmer electrodic equation for a one-step, single charge transfer reaction. This equation may be arranged into a direct, physically representational form given by:

$$i = k_f \cdot a_{\text{in}} \cdot \exp((1-\beta)FV/RT)$$

$$-k_b \cdot a_{\text{out}} \cdot \exp(-\beta FV/RT)$$

where i is the current carried by the elementary process $A_{\text{in}}^+ \rightleftharpoons A_{\text{out}}^+$, k_f and k_b are its forward and reverse rate coefficients, a_{in} and a_{out} are the respective chemical activities of A_{in}^+ and A_{out}^+ , V is the electric potential difference between state A_{in}^+ and state A_{out}^+ , ($V_{\text{in}} - V_{\text{out}}$); F , R and T have their usual meanings, and β is the so-called symmetry factor (cf. Bockris & Reddy, 1970).

The factor β arises from the fact that the electric field modifies an already existent potential energy barrier – the activation energy of the elementary chemical reaction causing the charge movement – thereby imparting voltage dependence to both forward and reverse unidirectional reaction rates. The modification is such that only a fraction $(1-\beta)$ of the input electrical energy appears as a change in activation energy for the forward reaction and, hence, in the forward rate expression;

Reaction Rate Laws

The following mass action rate laws were used for each of the six elementary steps of the scheme of Fig. 1:

$$\begin{aligned}rf_1 &= f_1 [E \cdot ATP] \cdot [Na^+]_{in}^3 \\rb_1 &= b_1 [Na_3E \cdot ATP] \\rf_2 &= f_2 [Na_3E \cdot ATP] \\rb_2 &= b_2 [Na_3E \sim P] \cdot [ADP] \\rf_3 &= f_3 [Na_3E \sim P] \\rb_3 &= b_3 [E' - P] \cdot [Na^+]_{out}^3 \\rf_4 &= f_4 [E' - P] \cdot [K^+]_{out}^2 \\rb_4 &= b_4 [K_2E'] \cdot [P] \\rf_5 &= f_5 [K_2E'] \cdot [ATP] \\rb_5 &= b_5 [K_2E \cdot ATP] \\rf_6 &= f_6 [K_2E \cdot ATP] \\rb_6 &= b_6 [E \cdot ATP] \cdot [K^+]_{in}^2\end{aligned}$$

where rf_i , rb_i are the forward and reverse rates and f_i , b_i are the forward and reverse rate coefficients of the i^{th} step.

The dimensions of the rate coefficients listed in the Table are those appropriate to yield rates of reaction in mol/cm²/sec. Given that each mole of overall reaction extrudes one Faraday of charge, transport rates in the vectorial situation are expressed as pump current per unit area of membrane. In order to allow a direct quantitative comparison of nonvectorial with vectorial results we have expressed all fluxes (unidirectional or net), transport rates and ATPase activity in the same electrical units. Net ATPase activity is related to the electrical units by noting that pump current (A/cm²) is given by the pump site density (mol/cm²) times the Faraday equivalent times the number of molecular turnovers per second. Thus, for a pump site density of 0.125 pmol/cm² or 753 sites/μm² (Michael et al., 1979; Daut & Rudel, 1981) 1 μA/cm² of net pump current corresponds to 82.9 molecular turnovers per second. This means that the constraint on the maximum molecular turnover rate of the enzyme restricts ATPase activity to a maximum equivalent value of 2.01 μA/cm².

The set of reactions in Fig. 1 has a total of 12 rate coefficients, of which 11 are independent since the equilibrium constant for the overall reaction is known. It is possible, in principle, to determine values for these rate coefficients by fitting a sufficiently large body of data. In practice and certainly with the limited data available, such a unique set of rate coefficients cannot be determined. Our aim was to find one set of rate coefficients that was consistent with a limited set of experimental data, recognizing that there are other sets that would have also fitted the data. Our findings and conclusions, therefore, must not be considered exhaustive but preliminary. The experimental data were fitted by eye, the choice of rate coefficient(s) to be adjusted to improve the fit being made on the basis of experience.

For voltage-dependent steps, the voltage-dependent rate coefficients were obtained by multiplying the respective rate coefficients by functions of membrane potential, assuming a symmetry factor of 0.5 (see above, The Model – Voltage Dependence).

Steady-state solutions for the concentrations of intermediates were obtained by Gaussian elimination and used to solve for the unidirectional rates of each step in the reaction sequence. All equations were solved on a Digital Equipment Corporation

VAX 11/780 digital computer with graphical results displayed either on a Tektronix 4006-1 Graphics Display terminal or on a Hewlett-Packard 7221A Graphics Plotter. As a safety check on the computations a 0.01% tolerance was placed on the required agreement between the following pairs of quantities:

1. The sum of the computed enzyme intermediates and the set parameter for total enzyme per unit area of membrane;
2. The overall steady-state rate of reaction defined by Boudart (1976; and see footnote 1 on page 148) and the steady-state rate of reaction through step 1;
3. The ratio of the overall unidirectional forward rate of reaction to the overall unidirectional reverse rate of reaction and the ratio predicted thermodynamically from the net free energy dissipation of the overall reaction (Boudart, 1976; Chapman & McKinnon, 1978).

Simulations were performed either vectorially (i.e., true transport across a membrane separating two compartments of different electrochemical composition) or nonvectorially (i.e., isolated enzyme in solution). For the latter case the vectorial computer programs were used with equal concentrations for intracellular and extracellular ionic species and with the membrane potential set equal to zero.

In cases where the effects of varying the ionic concentrations were studied all other electrochemical conditions were held constant unless otherwise stated.

Unidirectional ionic fluxes were calculated by using the method of Boudart (1976) to define unidirectional rates of reaction across steps 1 to 3 of Fig. 1 for Na⁺ movements, and across steps 4 to 6 for K⁺ movements (cf. Chapman, 1982).

Results and Discussion

Nonvectorial ATPase Activity

The behavior of the isolated enzyme in the nonvectorial situation is independent of the choice of voltage-dependent step (see The Model – Voltage Dependence) because there is no influence of voltage comparable to the physiological situation in the membrane. There is also no distinction between intracellular and extracellular forms of the ionic species; the two forms of the enzyme capable of reacting with each ionic species are therefore exposed simultaneously to the same bulk concentrations of Na⁺ and K⁺. Of the available kinetic data we chose to fit those of Skou (1957; 1975) for the activation of the Na⁺,K⁺-ATPase by Na⁺ and K⁺ in the presence of saturating levels of ATP. The resulting simulations are shown in Fig. 2A (Na⁺ activation), 2B (K⁺ activation), and 2C (simultaneous variation of [Na⁺] and [K⁺]). These Figures should be compared with Figs. 6 and 5 of Skou (1957) and Fig. 1 of Skou (1975), respectively. While certain details of Skou's data cannot be fitted by our scheme (e.g., the Na⁺ activation of ATPase in the presence of zero [K⁺]), in general the fit is reasonably satisfactory for establishing a working set of rate coefficients.

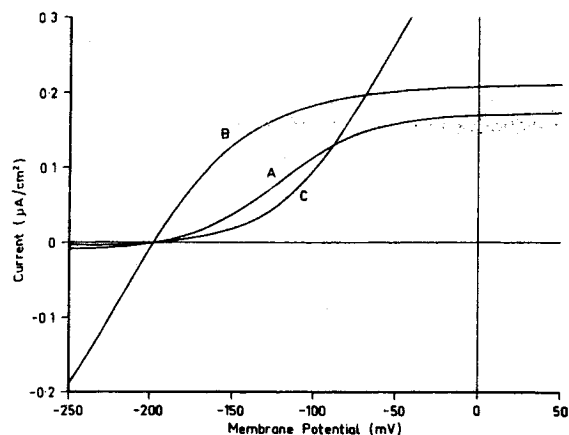


Fig. 4. Pump current-voltage relations with voltage dependence on step 5 of reaction scheme of Fig. 1 as in Fig. 3B. A: Control. B: Rate coefficients adjusted to increase the voltage-dependent reversibility exhibited by curve A, $b_2 = 10^7 \text{ liter mol}^{-1} \text{ sec}^{-1}$, $f_3 = 1000 \text{ sec}^{-1}$, $b_3 = 5 \times 10^4 \text{ liter}^3 \text{ mol}^{-3} \text{ sec}^{-1}$, $f_4 = 10^8 \text{ liter}^2 \text{ mol}^{-2} \text{ sec}^{-1}$, $b_4 = 1.33 \times 10^6 \text{ liter mol}^{-1} \text{ sec}^{-1}$, $b_5 = \exp(-FV/2RT) \text{ sec}^{-1}$, $f_6 = 1.91 \times 10^4 \text{ sec}^{-1}$, all other rate coefficients as in the Table. C: Rate coefficients adjusted to reduce the reversibility; $f_3 = 2 \times 10^5 \exp(FV/2RT) \text{ liter mol}^{-1} \text{ sec}^{-1}$, $f_6 = 115 \text{ sec}^{-1}$, $b_6 = 6 \times 10^5 \text{ liter}^2 \text{ mol}^{-2} \text{ sec}^{-1}$

conductance in the physiological range than evident in Fig. 3B. However, there are two interacting properties to be weighed against each other: the relative slope conductance in the physiological range versus the relative reversibility of the pump beyond the reversal potential. By the latter we mean the relative magnitude of the pump current at potentials beyond (more negative than) the reversal potential compared to that at potentials positive to the reversal potential. As is illustrated in Fig. 4, we found that the condition of less physiological slope conductance (curve B) is associated with a relatively high degree of voltage-dependent reversal; conversely, a larger physiological slope conductance (curve C) is associated with relatively little voltage-dependent reversal. Although we have pointed out before that a pump reversal potential must exist on thermodynamic grounds (Chapman & Johnson, 1978), no significant reversal of electrogenic transport currents has been reported. For this reason we have chosen the compromise relation (Fig. 4A or 3B) as our control in subsequent simulations.

Moreover, the choices of rate coefficients yielding the I - V curves of Fig. 4B and C result in significant alterations to the nonvectorial activation behavior of the isolated ATPase as shown in Fig. 5B and C, respectively. Although the rate coefficients for Fig. 4B fall within the constraints listed earlier (see Materials and Methods) the maximum turnover number of the isolated enzyme has become unacceptably large in Fig. 5B. On the other hand,

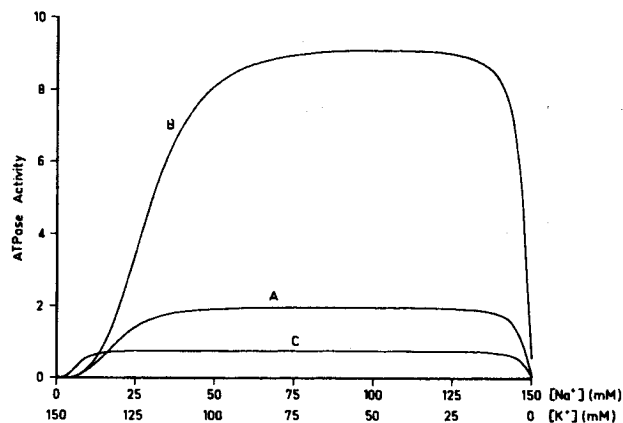


Fig. 5. Simultaneous activation of nonvectorial ATPase activity by Na^+ and K^+ ions constrained to sum to 150 mM, using the rate coefficients yielding the current-voltage relations of Figs. 4A, B and C, respectively. ATPase activity expressed in $\mu\text{A}/\text{cm}^2$; $1 \mu\text{A}/\text{cm}^2 = 82.9 \text{ molecular turnovers per second}$

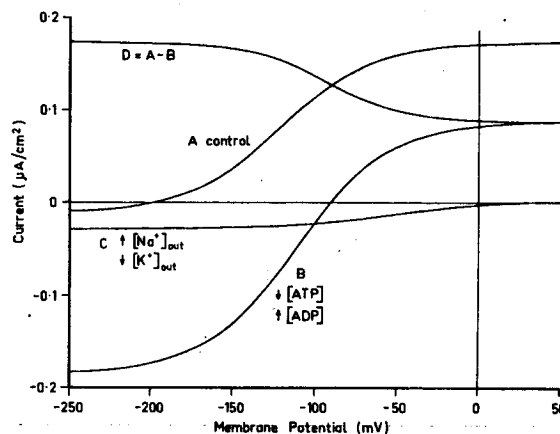


Fig. 6. Effect of altered chemical conditions on the pump current-voltage relation. A: Control; rate coefficients and parameters as in the Table. B: Effect of reducing $[\text{ATP}]$ from 4.99 mM (control) to 3.0 mM with corresponding increase in $[\text{ADP}]$; other rate coefficients and parameters as in the Table. C: Effect of increased ionic concentration gradients; extracellular $[\text{Na}^+]$ increased to 200 mM and extracellular $[\text{K}^+]$ lowered to 0.1 mM; all other rate coefficients and parameters as in the Table. D: The difference between curve A (control) and curve B (reduced free energy available from ATP splitting)

the rate coefficients for Fig. 4C produce an unacceptable diminution and change in shape of the enzymatic activation curve in Fig. 5C. This suggests that the seemingly unlimited freedom in choosing appropriate rate coefficients for the six steps of Fig. 1 might become quite restricted when all known physiological and biochemical requirements are taken into account.

Gradman et al. (1981) have suggested that an I - V curve which exhibits little voltage-dependent reversal, such as that of Fig. 4A, reflects the possibility that voltage may be kinetically incompetent to synthesize ATP. This is not necessarily true:

tivation of electrogenic pump current over the physiological range of intracellular $[\text{Na}^+]$ (approximately 10 to 20 mM) in dog Purkinje fibers (Gadsby & Cranefield, 1979a). Keynes and Swan (1959) and Mullins and Frumento (1963) reported a saturating cubic activation by intracellular Na^+ in frog muscle, corresponding to the wider range of intracellular $[\text{Na}^+]$ shown in the curves of Fig. 7A. Similar activation by $[\text{Na}^+]_{\text{in}}$ was found in red cells by Garay and Garrahan (1973). Brinley and Mullins (1968) found a linear activation of unidirectional transport-mediated Na^+ efflux in squid axon over a wide range of intracellular $[\text{Na}^+]$, a finding not in accord with Fig. 7A. However, measurement of unidirectional fluxes can be an unreliable measure of net transport (Chapman, 1982) as discussed below.

A K_m of about 1 mM for activation of electrogenic pump current by extracellular K^+ has been reported by Gadsby and Cranefield (1979b) for dog Purkinje fibers with the membrane potential held at around -30 mV. Garrahan and Glynn (1967a) found a K_m for the extracellular K^+ -activated Na^+/K^+ exchange in red cells of just over 1 mM $[\text{K}^+]$. These findings accord with the behavior of our model with little or no membrane potential but not with a membrane potential of the order of -85 mV (see Fig. 7B).

The relative insensitivity of net Na^+/K^+ transport to extracellular Na^+ is consistent with a wide range of physiological observations. Lowering external $[\text{Na}^+]$ has little effect on Na^+ efflux from red cells into normal K^+ -containing medium (Garrahan & Glynn, 1967a). The absence of marked hyperpolarization in excitable cells in low $[\text{Na}^+]$ media is also in keeping with the relatively weak influence of extracellular Na^+ on Na^+/K^+ pump current. Such insensitivity is one of the more important differences between the present model and the one used previously (Chapman et al., 1979). In that model, transport was treated as an 'elementary-complex' reaction, where an assumed saturation of the reverse rate of reaction by external Na^+ forced an inverse third-order dependence of the forward rate. As a consequence, relatively mild reductions of external $[\text{Na}^+]$ produced enormous increases in pump current with unrealistic hyperpolarizations of the membrane potential.

The strong inhibitory effect of intracellular K^+ on net transport (Fig. 7D) is a direct consequence of fitting the nonvectorial K^+ activation behavior to that described by Skou (1957). In the present model the inhibition by intracellular K^+ is due to competition with intracellular Na^+ for combination with the $\text{E} \cdot \text{ATP}$ form of the enzyme. The reason that extracellular Na^+ does not show an

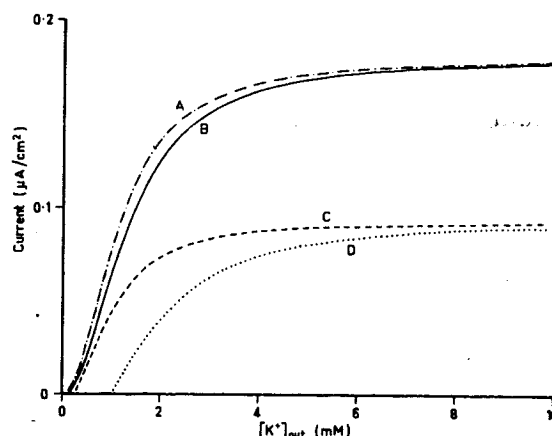


Fig. 8. Activation of Na^+/K^+ transport by K^+_{out} with $[\text{ATP}]$ set at 4.99 mM (A and B) or 3.0 mM (C and D) and $[\text{Na}^+]_{\text{out}}$ set at 140 mM (B and D) or 50 mM (A and C). All other rate coefficients and parameters as in the Table with $[\text{ATP}] + [\text{ADP}]$ constrained to sum to 5.05 mM

equal inhibitory effect by competing with extracellular K^+ for combination with the $\text{E}' - \text{P}$ form of the enzyme is a consequence of our choices of rate coefficients for the first three steps which cause the the model to exhibit little Na^+/Na^+ exchange at normal ATP levels. Consequently, the behavior of the present model is unlike that of the sodium pump of red cells but more like that of squid axon, where Na^+/Na^+ exchange appears only when the energy available from ATP is reduced (Caldwell, Hodgkin, Keynes & Shaw, 1960; see also Fig. 9). In that case the steps involving Na^+ extrusion become more reversible and the model now exhibits competition between extracellular Na^+ and K^+ for combination with the $\text{E}' - \text{P}$ form of the enzyme. Figure 8 shows activation of Na^+/K^+ transport by extracellular K^+ at normal (B and D) and reduced (A and C) extracellular $[\text{Na}^+]$, for normal (A and B) and reduced (C and D) energy available from ATP. Reduction of $[\text{ATP}]$ by 40% reduces the maximum rate of transport but also has a striking effect on the kinetics of activation by K^+_{out} , greatly increasing the 'inhibition' by Na^+_{out} at low $[\text{ATP}]$.

Unidirectional Fluxes

It has been shown previously that unidirectional fluxes, such as can be measured isotopically in rapid dialysis experiments, are generally useless for establishing the stoichiometry of a transport reaction involving a sequence of elementary steps (Chapman, 1982). Furthermore, the unidirectional flux of isotope through such a sequence of steps is not a measure of the steady-state overall unidirectional rate of reaction as defined by Boudart

sary to determine and subtract the pump 'exchange' fluxes before using unidirectional pump flux data to estimate overall reaction velocities.

Saturation of Enzyme and Reaction Rates

Since we have assumed, to begin with, that all of the enzyme is complexed with one or more of the reactants and products, the nearest analogy to 'free' enzyme would be the complex we have designated 'E·ATP'. Thus, the fraction of total enzyme not in the form of E·ATP might be taken to represent the degree of 'saturation' of the total amount of enzyme available. Figures 10A, B and C are plots of intermediate composition corresponding to the voltage and chemical dependences illustrated in Figs. 3B, 7A and 7B, respectively. The dependences of net transport on voltage and chemical composition are certainly not the result of changes in the amount of E·ATP available which, for the parameters yielding these Figures, is negligible at all voltages and ionic concentrations.

The only other form of the enzyme not complexed with Na^+ or K^+ , i.e., $\text{E}'\text{-P}$, shows a decline in concentration as the transport rate is activated by voltage (Fig. 10A) or K_{out}^+ (Fig. 10C), but shows an increase in concentration for activation by Na_{in}^+ (Fig. 10B).

In the classic treatment of an enzyme reaction as a single reversible elementary step to form an enzyme-substrate complex, followed by an irreversible formation of products, saturation of the forward rate of reaction is identical with, and due to, saturation of the enzyme. No such simple relation obtains, however, for a sequence of reversible elementary steps, such as those of Fig. 1. As the results of Fig. 10 clearly show, the voltage and chemical dependences of the reaction rates that are illustrated in Figs. 2 through 9 arise, not from a changing degree of saturation of the total amount of enzyme, but from a shifting balance between the various enzyme forms represented by the six intermediates.

Voltage-Dependent Binding of Na^+ and K^+

The distributions of intermediates shown in Fig. 10 contain information about the proportions of enzyme binding Na^+ and K^+ ions. With all of the voltage dependence assigned to step 5 of the scheme of Fig. 1 it follows that no step involving binding or dissociation between Na^+ or K^+ and the enzyme is directly influenced by voltage. However, there is a considerable indirect effect of voltage on the binding of Na^+ or K^+ to the enzyme, owing to the voltage-dependent distribution of intermediates. Figure 11 illustrates how the relative

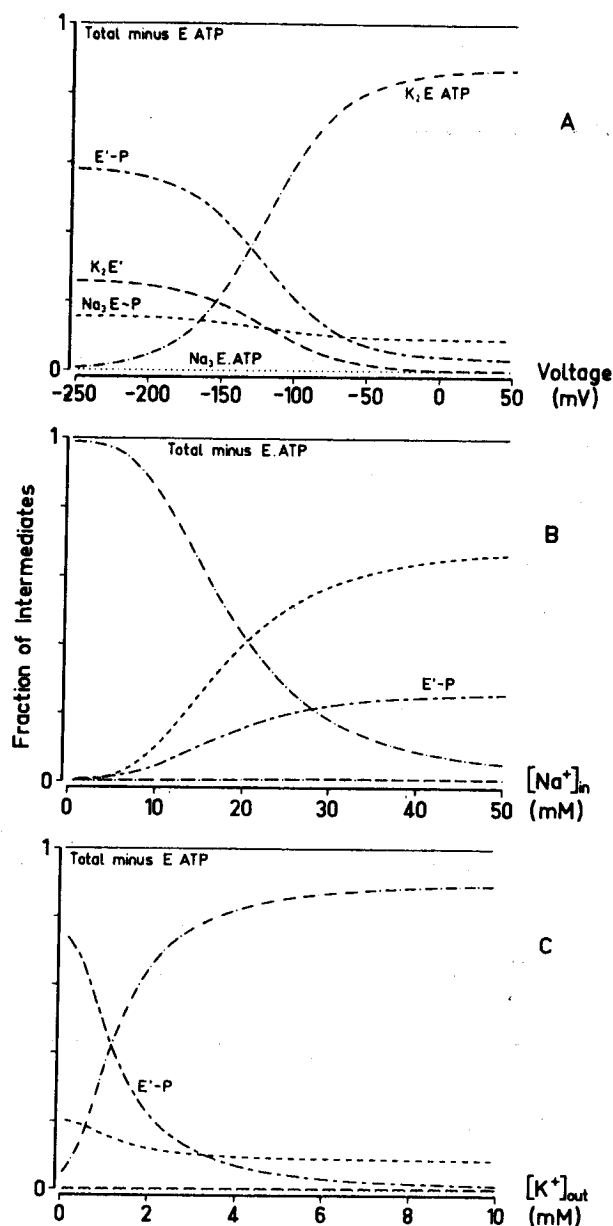


Fig. 10. Distribution of concentrations of enzyme intermediates as fractions of total enzyme versus membrane potential (A), intracellular $[\text{Na}^+]$ (B) and extracellular $[\text{K}^+]$ (C). All rate coefficients and parameters as in the Table

proportions of enzyme to which Na^+ and K^+ are bound change as the membrane potential is varied.

Free Energy Dissipation and Conservation

The free energy available from the splitting of ATP is the potential energy difference that drives net transport of Na^+ and K^+ ions. Some of this energy is conserved in the electrochemical work of ion translocation; the remainder is dissipated in producing net reaction at each of the six reaction steps. For example, Fig. 12A shows that the free energy

and ionic species, there must be a range of membrane potentials over which the pump mechanism displays considerable slope conductance. The fact that no reports of such a contribution by the pump to the total membrane slope conductance exist in the literature indicates that this range of membrane potentials lies normally beyond the limits of hyperpolarization in electrophysiological experiments. On the other hand, as we have suggested previously (Chapman & Johnson, 1978), this behavior might well be brought into the experimental range of membrane potentials by reducing the free energy available from ATP splitting (see Fig. 6).

In our previous model (Chapman et al., 1979) the high degree of pump reversibility immediately beyond the resting potential (hyperpolarizing) led to a high pump contribution to the membrane slope conductance. This was due to two factors: (a) our use of older values from the literature for the free energy available from ATP splitting (magnitude less than -50 kJ/mol ATP) and (b) our forcing all of the voltage dependence on to the reverse rate of a single 'elementary-complex' reaction (see above, The Model - Voltage Dependence). Using more modern estimates of the free energy of ATP splitting (Hassinen & Hiltunen, 1975; Veech et al., 1979) places the pump reversal potential around 100 mV more negative than the resting potential. With our earlier treatment of the pump as a single 'elementary-complex' reaction this would have removed any possibility of the pump contributing to the membrane slope conductance in the physiological range. However, the effects of redistribution of intermediates in the present multi-step enzymatic model with changes in membrane potential (Fig. 11) cause the voltage dependence of net transport to be spread to potentials far distant from the reversal potential.

Indeed, the inclusion of several intermediate steps in the pump mechanism allows a single voltage-dependent step to result in a wide range of possible $I-V$ curves of potentially complex shape, some of which have been explored by Gradmann et al. (1981) and Hansen et al. (1981). Therefore, it would seem of paramount importance to our understanding of the contribution of electrogenic transport to electrophysiology that the pump $I-V$ relation should be determined accurately. Unfortunately, the geometry and morphology of most cellular preparations make it impossible to control adequately the chemical composition of intracellular and extracellular space before and after the pharmacological or metabolic blockades usually

employed to separate active Na^+/K^+ transport current from passive and other transport/exchange currents.

Moreover, the experimental technique of poisoning the ATP supply system is wholly inadequate as a means of eradicating the contribution of active electrogenic transport to the membrane $I-V$ relationship. This is because the pump is likely to become highly reversible when ATP is depleted and ADP accumulates, resulting in 'difference' $I-V$ curves (i.e., before and after metabolic blockade) that have no reversal potential (see curve *D* of Fig. 6). While it must be admitted that the adenylate kinase system, together with deamination of adenosine monophosphate, would tend to buffer the accumulation of ADP in poisoned cells (Atkinson, 1977), the fact remains that any increase at all in ADP concentration would enhance the reverse rate of electrogenic transport beyond the reversal potential and thereby render invalid the subtraction of membrane $I-V$ curves before and after poisoning.

Transient Responses. All of the simulations presented here have been steady-state solutions of the differential equations describing rates of changes of enzyme intermediates. Clearly, the response to a step change in transmembrane potential will not be instantaneous. Time will be required for the intermediates to change from one steady-state distribution to another (e.g., see voltage-dependent distribution of intermediates shown in Fig. 10 A). If more than one rate-limiting step exists in the overall sequence, then the time constants of those reactions will determine the time-dependence of the pump current in response to a change in membrane potential. For the normal physiological values in the present scheme at a resting potential of -85 mV the pseudo first-order time constants of the slowest steps are 4.6, 0.7 and 0.5 msec for steps 3, 4 and 5, respectively. For the assumed pump site density of 0.125 pmol/cm² the total charge transferred per unit of membrane capacitance (1 $\mu\text{F}/\text{cm}^2$) amounts to 12 mV per cycle of overall reaction. Consequently, one might expect the charged forms of the Na^+/K^+ -ATPase to contribute significantly to experimentally observable charge displacement or pseudo 'gating' currents on a time scale similar to those that might be observed in connection with the fast Na^+ conductance responsible for the upstroke of the cardiac action potential following steps in membrane voltage.

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Received 25 August 1982; revised 3 January 1983